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(54) **FILTERING CONTROL METHOD FOR IMPROVING IMAGE QUALITY OF BI-LINEAR INTERPOLATED IMAGE**

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G06T 5/20 (2006.01)

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CPC **G06T 3/4007** (2013.01); **G06T 5/003** (2013.01); **G06T 5/20** (2013.01)

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G06T 5/20

USPC 382/260-264, 298-300; 358/525
See application file for complete search history.

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(57) **ABSTRACT**

The present invention relates to an interpolation method for enlarging a digital image or predicting a moving vector of a compressed image system as a sub-pixel unit when the image digitized through a CCD (Charge Coupled Device) camera ect. has a low resolution in a video phone or video conference or general digital video system, particularly the present invention can be adapted to a post processor of a compressed digital image in order to improve the image quality, and can be used for finding a moving vector of a moving picture compressed type, accordingly the present invention is capable of improving the image quality.

20 Claims, 4 Drawing Sheets

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|--|----------|---|--|
| $\begin{bmatrix} A \\ B \\ C \\ D \\ E \\ F \\ G \\ H \\ I \\ J \\ K \\ L \\ M \\ N \\ O \\ P \\ Q \\ R \\ S \\ T \\ U \\ V \\ W \\ X \end{bmatrix}$ | $=1/512$ | $\begin{bmatrix} -7 & 81 & -14 & 0 & 52 & 405 & 24 & 0 & -13 & -2 & -14 & 0 & 0 & 0 & 0 & 0 \\ -6 & 23 & 52 & -12 & -9 & 201 & 302 & -12 & -3 & -5 & -13 & -6 & 0 & 0 & 0 & 0 \\ -8 & 43 & -16 & 0 & 99 & 382 & -9 & 0 & -3 & 38 & -14 & 0 & 0 & 0 & 0 & 0 \\ -10 & 38 & -20 & 0 & 54 & 397 & 27 & 0 & -7 & 49 & -16 & 0 & 0 & 0 & 0 & 0 \\ -13 & 33 & -23 & 0 & 10 & 413 & 62 & 0 & -12 & 59 & -17 & 0 & 0 & 0 & 0 & 0 \\ -12 & 26 & -15 & -3 & -4 & 354 & 142 & -5 & -11 & 48 & -4 & -4 & 0 & 0 & 0 & 0 \\ -10 & 17 & -8 & -7 & -13 & 295 & 221 & -9 & -10 & 36 & 9 & -9 & 0 & 0 & 0 & 0 \\ -5 & 4 & 18 & -11 & -9 & 197 & 302 & -9 & -5 & 17 & 24 & -11 & 0 & 0 & 0 & 0 \\ -14 & -6 & -21 & 0 & 56 & 338 & 29 & 0 & -2 & 99 & -17 & 0 & 0 & 0 & 0 & 0 \\ -10 & -7 & -24 & -3 & -5 & 344 & 145 & -5 & -12 & 88 & 7 & -6 & 0 & 0 & 0 & 0 \\ -4 & -13 & -16 & -11 & -10 & 194 & 301 & -6 & -6 & 39 & 60 & -16 & 0 & 0 & 0 & 0 \\ -12 & -13 & -9 & 0 & 53 & 363 & 26 & 0 & 1 & 111 & -8 & 0 & 0 & 0 & 0 & 0 \\ -9 & -14 & -11 & 0 & 19 & 356 & 67 & 0 & -6 & 109 & 1 & 0 & 0 & 0 & 0 & 0 \\ -9 & -9 & -14 & -2 & -9 & 261 & 195 & -5 & -9 & 74 & 45 & -6 & 0 & 0 & 0 & 0 \\ -12 & -5 & -13 & -4 & -5 & 174 & 282 & -9 & -5 & 42 & 79 & -12 & 0 & 0 & 0 & 0 \\ -6 & -10 & -8 & 0 & 19 & 219 & 18 & 0 & 37 & 271 & 6 & 0 & -9 & -16 & -9 & 0 \\ -8 & -9 & -6 & 1 & -11 & 193 & 78 & -4 & -7 & 243 & 83 & -4 & -4 & -14 & -14 & -1 \\ -1 & -8 & -11 & -4 & -8 & 102 & 156 & -13 & -8 & 142 & 206 & -10 & -1 & -11 & -15 & -4 \\ -4 & -5 & -3 & 0 & 23 & 153 & -16 & 0 & 83 & 330 & -13 & 0 & -13 & -16 & -7 & 0 \\ -3 & -5 & -4 & 0 & 6 & 151 & 0 & 0 & 45 & 338 & 15 & 0 & -11 & -9 & -11 & 0 \\ -2 & -5 & -5 & 0 & -10 & 149 & 15 & 0 & 7 & 347 & 43 & 0 & -9 & -2 & -16 & 0 \\ -2 & -4 & -6 & -1 & -12 & 125 & 35 & -4 & -5 & 304 & 111 & -4 & -6 & -3 & -14 & -2 \\ -1 & -4 & -6 & -1 & -14 & 102 & 55 & -8 & -16 & 260 & 179 & -9 & -4 & -4 & -13 & -4 \\ -1 & -4 & -6 & -2 & -7 & 62 & 104 & -12 & -8 & 172 & 255 & -11 & -2 & -9 & -14 & -5 \end{bmatrix}$ | $\begin{bmatrix} a \\ b \\ c \\ d \\ e \\ f \\ g \\ h \\ i \\ j \\ k \\ l \\ m \\ n \\ o \\ p \end{bmatrix}$ |
|--|----------|---|--|

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FIG. 1

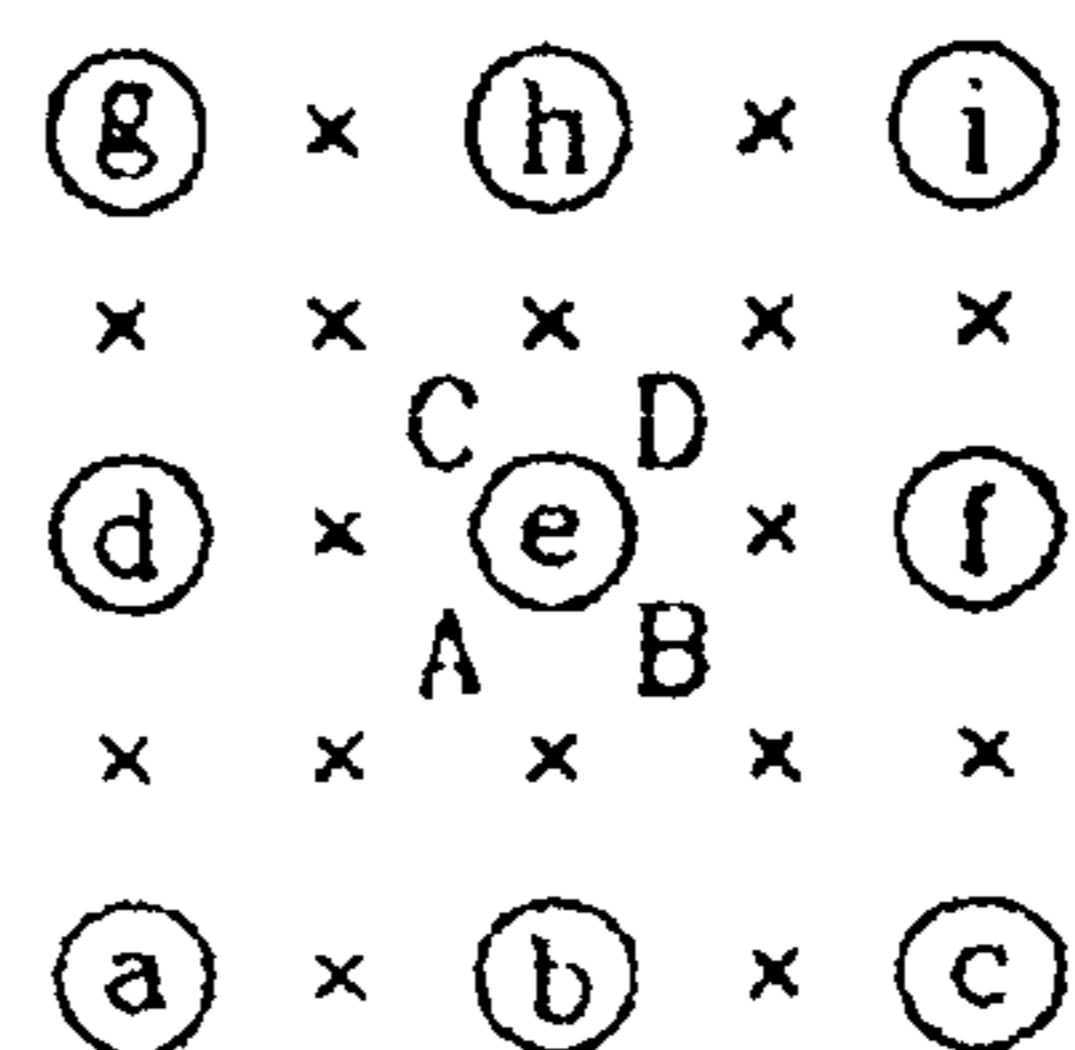


FIG. 2

$$\begin{bmatrix} A \\ B \\ C \\ D \end{bmatrix} = 1/512 \begin{bmatrix} 1 & 94 & -15 & 94 & 391 & -15 & -15 & -15 & -8 \\ -15 & 86 & -9 & -13 & 370 & 113 & -6 & -14 & -18 \\ -15 & -13 & -6 & 86 & 370 & -14 & 9 & 113 & -18 \\ 6 & -14 & -14 & -14 & 349 & 107 & -14 & 107 & 11 \end{bmatrix} \begin{bmatrix} a \\ b \\ c \\ d \\ e \\ f \\ g \\ h \\ i \end{bmatrix}$$

FIG. 3

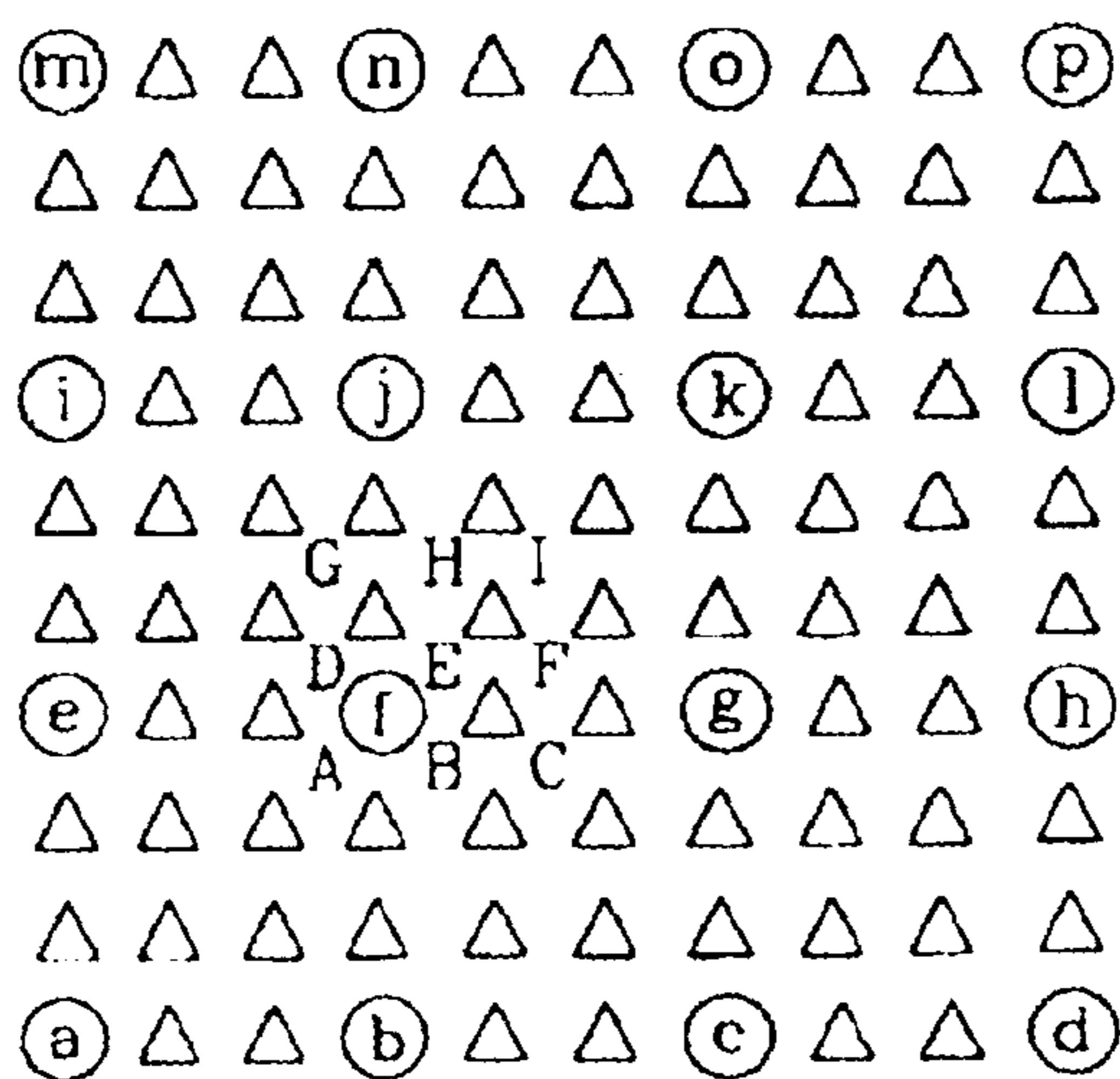
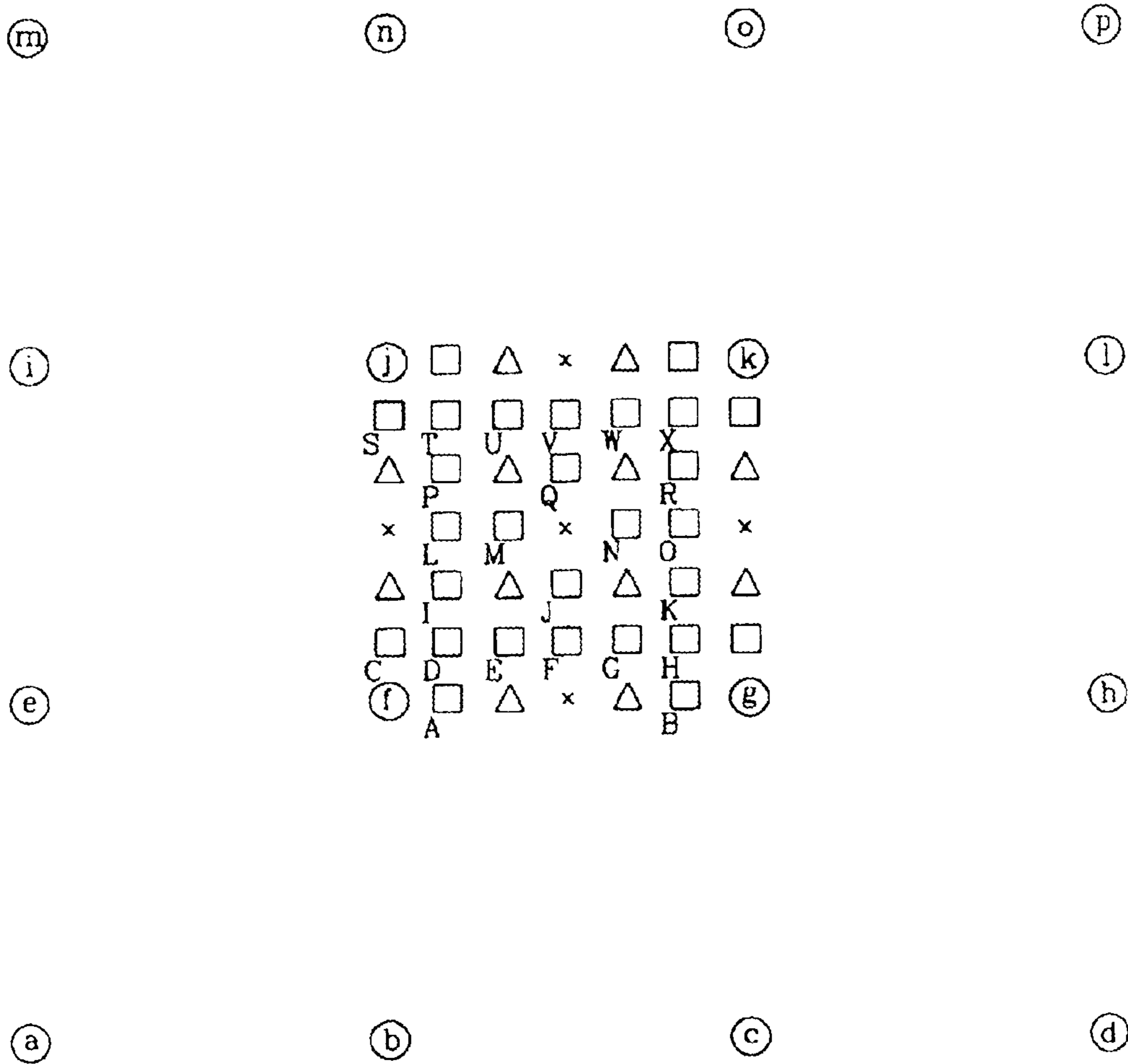


FIG. 5



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FILTERING CONTROL METHOD FOR IMPROVING IMAGE QUALITY OF BI-LINEAR INTERPOLATED IMAGE

Matter enclosed in heavy brackets [] appears in the original patent but forms no part of the first and this reissue specification; matter printed in italics indicates the additions made by the first reissue. Matter enclosed in double heavy brackets [[]] appears in the first reissue patent but forms no part of this reissue specification; matter printed in bold face indicates the additions made by this reissue; a claim printed with strikethrough indicates that the claim was canceled, disclaimed, or held invalid by a prior post-patent action or proceeding.

CROSS-REFERENCE TO RELATED APPLICATIONS

This is a reissue of U.S. Pat. No. RE42,045, issued on Jan. 18, 2011, which is a reissue of U.S. Pat. No. 6,803,954 issued Oct. 12, 2004. More than one reissue application has been filed for the reissue of U.S. Pat. No. 6,803,954. U.S. patent application Ser. No. 11/546,484 is a reissue of U.S. Pat. No. 6,803,954; U.S. patent application Ser. No. 12/024,408, now abandoned, is a divisional reissue of U.S. Pat. No. 6,803,954; and U.S. patent application Ser. No. 12/424,927 is a continuation reissue of U.S. patent application Ser. No. 11/546,484, the entire contents of each are hereby incorporated by refer-

BACKGROUND OF THE INVENTION

1. Field of the Invention

The present invention relates to an interpolation method adapted to enlargement of a low resolution image when the image digitized through a CCD (Charged-Coupled Device) has the low resolution, in particular to a filtering control method for improving the image quality of a bi-linear interpolated image which is capable of restoring a requested interpolated high resolution image from a low resolution image by finding a coefficient of a two-dimensional filter on the basis of a regularization image restoration method.

2. Description of the Prior Art

In the conventional technology, a still picture or a moving picture has or transmits a low resolution image because it can not physically satisfy a sensor having the low resolution or a nyquist value.

In addition, a compressed moving picture has or transmits the low resolution image due to its bit value problem.

For example, when the compressed moving picture having the low bit value is transmitted to a receiver and the receiver enlarges the transmitted moving picture, the resolution of the transmitted moving picture lowers due to a degradation phenomenon ect.

Accordingly, a method for getting a high resolution image from a low resolution image is required.

In the meantime, the method for getting the high resolution image from the low resolution image is largely divided into an image expansion type method and an image enhancement type method.

First, the image expansion type method converts the size of the low resolution image into a requested size. The bi-linear interpolation method, a zero order expansion method, and a cubic spline method are comprised in the image expansion type method.

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However, as described above, the image expansion type method has an image visibility lowering problem because when the image is interpolation-restored by the above-mentioned method such as the bi-linear interpolation method, zero order hold expansion method, cubic spline method, the outlines of the image is over-blurred.

Meanwhile, the image enhancement type method comprises many methods, but the image enhancement type method causes a computational complexity, accordingly the method is not suited to a real-time processing due to the its computational complexity.

In addition, when the image enhancement type method is used for getting the high resolution image from the low resolution image, setting of each parameter is not adaptable.

For example, there is a POCS (Projection Onto Convex Set) method for increasing the resolution of an image. In the POCS method, in use of time region information, it is assumed as correlation between the images is uniformly same, but actually the correlation between the images is not uniform.

In addition, there is a mapping method for mapping a non-uniform sample of the low resolution image into a uniform sample of the high resolution image by using moving information and segmentation information of the image. However, the mapping method has the computational complexity problem, accordingly the mapping method is not suited to the real-time image data processing of the image processing system.

SUMMARY OF THE INVENTION

The object of the present invention is to provide a filtering control method for improving the image quality of a bi-linear interpolated image which is capable of improving the image quality of the interpolated image by using an interpolation method considering a real-time processing, a computational complexity and an efficiency when the digital video system seeks the interpolated image from the low resolution image.

The other object of the present invention is to provide the filtering control method for improving the image quality of the bi-linear interpolated image which is capable of finding a two-dimensional filter coefficient for getting the interpolated image from the low resolution image on the basis of a regularization image restoration method.

The other object of the present invention is to provide the filtering control method for improving the image quality of the bi-linear interpolated image which can approximate and find a PSF (Point Spread Function) for the bi-linear interpolated image from a modeling of the degraded image in the frequency region.

The other object of the present invention is to provide the filtering control method for improving the image quality of the bi-linear interpolated image which is capable of performing a real-time adaptive processing by finding a filter coefficient from the bi-linear interpolated image and approximated PSF.

In the present invention, in order to find a filter coefficient for finding the interpolated image from the low resolution image on the basis of the regularization image restoration method, when H is the PSF (Point Spread Function), f is a requested high resolution image, Z is the low resolution image, g is the high resolution image gotten from the bi-linear interpolation method, an added function $M(f) = \|g - Hf\|^2 + \alpha \|Cf\|^2$ for finding the PSF(H) from an equation $g = Bz = Hf + n$ (B, H are bi-linear interpolated filters, n is a noise component generated by the assumed H) is defined.

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The filtering control method for improving the image quality of the bi-linear interpolated image can be implemented by finding the PSF(H) from the added function M(f) by using an equation

$$H(k, l) = \frac{G(k, l)}{F(k, l)}$$

The filtering control method for improving the image quality of the bi-linear interpolated image can be implemented by finding a PSF(P) of a $f=Pg$ function by using an equation

$$P(k, l) = \frac{H^*(k, l)}{H^*(k, l)H(k, l) + C^*(k, l)C(k, l)}$$

after finding the PSF(H).

The filtering control method for improving the image quality of the bi-linear interpolated image can restore the requested high resolution image(f) by finding an added filter coefficient Q of the PSF(P) and interpolation filter B from the equation $f=Pg=PBz=Qz$.

BRIEF DESCRIPTION OF THE DRAWINGS

FIG. 1 illustrates an image sample for getting a twice enlarged high resolution image according to the embodiment of the present invention.

FIG. 2 illustrates an interpolation filter coefficient for getting the twice enlarged image according to the embodiment of the present invention.

FIG. 3 illustrates an image sample for getting a three times enlarged high resolution image according to the other embodiment of the present invention.

FIG. 4 illustrates the interpolation filter coefficient for getting the three times enlarged image according to the other embodiment of the present invention.

FIG. 5 illustrates an image sample for getting a six times enlarged high resolution image according to the another embodiment of the present invention.

FIG. 6 illustrates the interpolation filter coefficient for getting the six times enlarged image according to the another embodiment of the present invention.

DETAILED DESCRIPTION OF THE PREFERRED EMBODIMENT

FIG. 1 illustrates an image sample for getting a twice enlarged high resolution image according to the embodiment of the present invention.

As depicted in FIG. 1, a~i illustrate low resolution pixels, A~D illustrate high resolution pixels. In addition, pixels depicted as 'x' illustrate pixels interpolated as twice by a twice interpolation filter coefficient.

FIG. 2 illustrates the interpolation filter coefficient for getting a twice enlarged image according to the embodiment of the present invention. In other words, the interpolation filter coefficient for interpolating the twice enlarged image of FIG. 1 is depicted in FIG. 2.

As depicted in FIG. 2, the high resolution image is gotten from the low resolution pixels a~i (3x3 pixels) inside of a circle of FIG. 1 by using the interpolation filter coefficient.

FIG. 3 illustrates an image sample for getting a three times enlarged high resolution image according to the other embodiment of the present invention.

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As depicted in FIG. 3, a~p illustrate the low resolution pixels, A~I illustrate the high resolution pixels using the filter according to the present invention.

FIG. 4 illustrates the interpolation filter coefficient for getting the three times enlarged image according to the other embodiment of the present invention.

As depicted in FIG. 4, three times enlarged pixels which are newly generated illustrated as triangles in FIG. 3 are gotten from the low resolution pixels a~p (4x4 pixels) by using the interpolation filter coefficient of FIG. 4.

FIG. 5 illustrates the image sample for getting a six times enlarged high resolution image according to the another embodiment of the present invention. In other words, it illustrates the image sample for getting the six times enlarged high resolution image from the twice and three times interpolation filter coefficients by using the bi-linear interpolation method.

As depicted in FIG. 5, pixels illustrated as a 'X' can be gotten by using the twice interpolation filter of FIG. 2, and pixels illustrated as a triangle can be gotten by using the three times interpolation filter coefficient of FIG. 4.

In addition, pixels illustrated as a quadrilateral can be gotten from the pixels generated by the twice and three times interpolation filter coefficients by using the bi-linear interpolation method.

FIG. 6 illustrates the interpolation filter coefficient for getting the six times enlarged image according to the another embodiment of the present invention. In other words, the interpolation filter coefficient for getting the six times enlarged image of FIG. 5 is depicted in FIG. 6.

Meanwhile, as depicted in FIG. 2, FIG. 4 and FIG. 6, the value found by using the interpolation filter coefficient of the present invention has an integer value.

In addition, a 9 bit shift is performed to the value calculated by the interpolation filter coefficient, accordingly there is no need to perform a floating point operation processing.

The twice, three times, six times interpolated images are depicted in FIG. 1~FIG. 6, however the present invention is not limited by that, it can be adapted freely to a certain interpolation value.

Hereinafter, the filtering control method for improving the image quality of the bi-linear interpolated image will be described in more detail.

First, a spatially invariant PSF (Point Spread Function) for finding the interpolation filter coefficient according to the each interpolation value can be easily analyzed and approximated in the frequency region, accordingly the spatially invariant PSF (Point Spread Function) is considered from the bi-linear interpolated image.

After that, when it is assumed as the low resolution image is z, high resolution image gotten by the bi-linear interpolation method is g, high resolution image to be restored is f, the relation between the each image can be described as below.

$$g=Bz=Hf+n \quad \text{[Equation 1]}$$

Herein, the B, H, n are the bi-linear interpolation filters, H is the spatially invariant PSF defining the relation between the original high resolution image and high resolution image gotten by the interpolation method, and the n is a noise component generated by the assumed H.

Herein, when the noise component is neglected and a direct inverse is used in order to find the PSF(H), the PSF(H) can be described as below equation 2 in the frequency region.

$$H(k, l) = \frac{G(k, l)}{F(k, l)} \quad [\text{Equation 2}]$$

Herein, the $H(k,l)$ is the component in the k,l frequency region of the PSF(H), the $G(k,l)$ is the component in the k,l frequency region of the bi-linear interpolated image. In addition, the $F(k,l)$ is the component in the k,l frequency region of the high resolution image.

Meanwhile, the high resolution image f to be restored is unknown, the PSF(H) can be gotten from the bi-linear interpolated high resolution image through a statistical processing after performing an under-sample processing of various images as various value.

Herein, the high resolution image is gotten by using the PSF(H) found from the direct inverse. In other words, there is a system stabilization problem because the high resolution image gotten from the PSF(H) by using the direct inverse is overshoot in the region where the k,l have '0' value (in general, high frequency region) in the frequency region, accordingly the regularization image restoration for improving the system stabilization is used to solve the problem.

The regularization image restoration method is used for restoring the image or finding a certain PSF, an added function $M(f)$ for finding the PSF(H) by using the regularization image restoration method can be described as below equation 3.

$$M(f) = \|g - Hf\|^2 + \alpha \|Cf\|^2 \quad [\text{Equation 3}]$$

Herein, the first term of the right side of Equation 3 illustrates the credibility of the bi-linear interpolated image, the second term of the right side illustrates increase of the stability of the system by providing the mitigation to the restored image.

In addition, the $\|\cdot\|$ means a norm, the α is a regularization parameter for determining the credibility and mitigation of the original image. In addition, the C is the two-dimensional high frequency filter for determining the mitigation of the original image, in the present invention a two-dimensional Gaussian filter is used as the C .

When a gradient operator is adapted to Equation 3 in order to get the high resolution image, it can be described as below equation 4.

$$\square M(f) = -2H^T(g - Hf) + 2\alpha C^T Cf = 0 \quad [\text{Equation 4}]$$

Herein, the T means a transpose of a matrix.

Meanwhile, conventionally a repetition method is used in order to get the high resolution image and regularization parameter, but it is not suited to the moving picture processing because the method causes lots of computational complexity.

Accordingly, in the present invention, the regularization parameter α is fixed as '1', and the high resolution image f can be found as below equation 5.

$$f = \frac{H^T g}{(H^T H + C^T C)} = Pg \quad [\text{Equation 5}]$$

When the PSF(P) is found by Equation 5, $PSF(P) = H / (H^T H + C^T C)$ requires the lots of computational complexity for calculating an inverse matrix, however the PSF(P) in Equation 5 is a block-circulant matrix, accordingly it can be easily calculated in the frequency region.

Accordingly, the PSF(P) can be found finally as below Equation 6.

$$P(k, l) = \frac{H^*(k, l)}{H^*(k, l)H(k, l) + C^*(k, l)C(k, l)} \quad [\text{Equation 6}]$$

Herein, the '*' means a complex-conjugate.

The PSF(P) can be found by using an IFT (Inverse Fourier Transform) from Equation 6.

The requested high resolution image f can be found as below Equation 7 by using the found PSF(P) and Equation 1.

$$f = Pg = PBz = Qz \quad [\text{Equation 7}]$$

The PSF(P) is the spatially invariant function, the bi-linear interpolation filter B can be easily found by the conventional technology, accordingly the added filter coefficient Q of the PSF(P) and bi-linear interpolation filter B can be found.

Herein, in order to reduce the computational complexity, the number of a kernel of the PSF(P) is set in accordance with the up-sampling value.

When the up-sampling value is 2 in the present invention, the number of the kernel is limited as 3, when the up-sampling value is 3, the number of the kernel is limited as 4.

When the up-sampling value is 2, it can be used in an application segment for enlarging the size of the image as twice at a post processor of the compressed digital image and in finding of a sub-pixel moving vector in a H.263 moving picture compressed method.

In addition, when the up-sampling value is 3, it can be used in using of a $1/3$ unit moving vector in a H.261, moving picture compressed method.

Herein, the H.263 and H.261 are moving picture compressed standards presented in the ITU-T (International Telecommunications Union-Telecommunication).

As described above, the present invention can be used for improving the image quality at the post processor of the compressed digital image by using the interpolation method for getting the interpolated high resolution image from the low resolution image when the resolution of the digital image lowers due to the low resolution image sensor.

In addition, the interpolation method of the present invention can improve the image quality by finding the moving vector of the moving picture compressed type.

What is claimed is:

1. A filtering control method for improving the image quality of a bi-linear interpolated image when recovering a high resolution image from a low resolution image, the method comprising performing operations using at least one processor, the operations comprising:

restoring a requested high resolution image f by finding an added filter coefficient Q of a PSF(P) and a bi-linear interpolation filter B from an equation $f = Pg = PBz = Qz$, wherein f is the high resolution image as requested, P is the PSF (Point Spread Function), g is the high resolution image found by the bi-linear interpolation method, and z is the low resolution image;

wherein the high resolution image f [can be] is restored by performing an added function $M(f)$ definition process for finding the PSF(H) from an equation $g = Bz = Hf + n$, wherein B , H are bi-linear interpolation filters, and n is a noise component generated by the assumed H ; and wherein the added function $M(f)$ is defined as $M(f) = \|g - Hf\|^2 + \alpha \|Cf\|^2$, wherein α is a regularization parameter, and C is a two-dimensional high frequency filter for finding mitigation of the original image.

2. The filtering control method for improving the image quality of the bi-linear interpolated image according to claim

1, wherein the regularization parameter α is fixed as '1' in order to reduce a computational complexity.

3. The filtering control method for improving image quality of the bi-linear interpolated image according to claim 1, wherein a two-dimensional gaussian filter is used as the two-dimensional high frequency filter C in order to determine the mitigation of the original image.

4. A filtering control method for improving the image quality of a bi-linear interpolated image when recovering a high resolution image from a low resolution image, the method comprising performing operations using at least one processor, the operations comprising:

restoring a requested high resolution image f by finding an added filter coefficient Q of a PSF(P) and a bi-linear interpolation filter B from an equation $f=Pg=PBz=Qz$, wherein f is the high resolution image as requested, P is the PSF (Point Spread Function), g is the high resolution image found by the bi-linear interpolation method, and z is the low resolution image;

wherein the high resolution image f [can be] is restored by performing an added function M(f) definition process for finding the PSF(H) from an equation $g=Bz=Hf+n$, wherein B, H are bi-linear interpolation filters, and n is a noise component generated by the assumed H;

wherein the high resolution image f is restored by finding a PSF(P) of a $f=Pg$ function after finding the PSF(H) from the added function M(f); and

wherein the PSF(H) is found by using an equation

$$H(k, l) = \frac{G(k, l)}{F(k, l)},$$

G(k,l) is the component in the k,l frequency region of the bi-linear interpolated image, and F(k,l) is the component in the k,l frequency region of the high resolution image.

5. A filtering control method for improving the image quality of a bi-linear interpolated image when recovering a high resolution image from a low resolution image, the method comprising performing operations using at least one processor, the operations comprising:

restoring a requested high resolution image f by finding an added filter coefficient Q of a PSF(P) and a bi-linear interpolation filter B from an equation $f=Pg=PBz=Qz$, wherein f is the high resolution image as requested, P is the PSF (Point Spread Function), g is the high resolution image found by the bi-linear interpolation method, and z is the low resolution image;

wherein the PSF(P) [can be] is found by getting an IFT (Inverse Fourier Transform) by an equation

$$P(k, l) = \frac{H^*(k, l)}{H^*(k, l)H(k, l) + C^*(k, l)C(k, l)}.$$

H(k,l) is a component in the k,l frequency region of the PSF(H), and C is a two-dimensional high frequency filter.

6. The filtering control method for improving the image quality of the bi-linear interpolated image according to claim 5, wherein the number of a [kernel] kernel of the PSF(P) is set in accordance with an up-sampling value of the image.

7. A filtering control method for improving the image quality of a bi-linear interpolated image when recovering a high resolution image from a low resolution image, the method

comprising performing operations using at least one processor the operations comprising:

defining an added function M(f) for finding a PSF(H) from an equation $g=Bz=Hf+n$ (wherein B, H are bi-linear filters, n is a noise component generated by an assumed H when the H is a PSF (Point Spread Function), f is a requested high resolution image, z is a low resolution image, and g is a high resolution image gotten by the bi-linear interpolation method);

finding a PSF(P) of a $f=Pg$ function after finding the PSF (H) from the defined added function M(f); and

restoring the requested high resolution image f by finding an added filter coefficient Q of the PSF(P) and interpolation filter B from the equation $f=Pg=PBz=Qz$;

wherein the added function M(f) is defined as $M(f)=\|g-Hf\|^2+\alpha\|Cf\|^2$, wherein α is a regularization parameter, and C is a two-dimensional high frequency filter for finding the mitigation of the original image.

8. The filtering control method for improving the image quality a of the bi-linear interpolated image according to claim 7, wherein the regularization parameter α is fixed as '1' in order to reduce a computational complexity.

9. The filtering control method for improving image quality of the bi-linear interpolated image according to claim 7, wherein a two-dimensional gaussian filter is used as the two-dimensional high frequency filter C in order to determine the mitigation of the original image.

10. A filtering control method for improving the image quality of a bi-linear interpolated image when recovering a high resolution image from a low resolution image, the method comprising performing operations using at least one processor the operations comprising:

defining an added function M(f) for finding a PSF(H) from an equation $g=Bz=Hf+n$ (wherein B, H are bi-linear filters, n is a noise component generated by an assumed H when the H is a PSF (Point Spread Function), f is a requested high resolution image, z is a low resolution image, and g is a high resolution image gotten by the bi-linear interpolation method);

finding a PSF(P) of a $f=Pg$ function after finding the PSF (H) from the defined added function M(f); and

restoring the requested high resolution image f by finding an added filter coefficient Q of the PSF(P) and interpolation filter B from the equation $f=Pg=PBz=Qz$;

wherein the PSF(H) is found by an equation

$$H(k,l)=(G(k,l)/F(-k,l)),$$

wherein G(k,l) is the component in the k,l frequency region of the bi-linear interpolated image, and F(k,l) is the component in the k,l frequency region of the high resolution image.

11. A filtering control method for improving the image quality of a bi-linear interpolated image when recovering a high resolution image from a low resolution image, the method comprising performing operations using at least one processor, the operations comprising:

defining an added function M(f) for finding a PSF(H) from an equation $g=Bz=Hf+n$ (wherein B, H are bi-linear filters, n is a noise component generated by an assumed H when the H is a PSF (Point Spread Function), f is a requested high resolution image, z is a low resolution image, and g is a high resolution image gotten by the bi-linear interpolation method);

finding a PSF(P) of a $f=Pg$ function after finding the PSF (H) from the defined added function M(f); and

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restoring the requested high resolution image f by finding an added filter coefficient Q of the PSF(P) and interpolation filter B from the equation $f=Pg=PBZ=Qz$; wherein the PSF(P) is found by using an IFT (Inverse Fourier Transform) by an equation

$$P(k, l) = \frac{H^*(k, l)}{H^*(k, l)H(k, l) + C^*(k, l)C(k, l)}$$

$H(k,l)$ is a component in the k,l frequency region of the PSF(H), and C is a two-dimensional high frequency filter.

12. The filtering control method for improving the image quality of the bi-linear interpolated image according to claim 11, wherein the number of a [kernel] *kernel* of the PSF(P) is differently set in accordance with an up-sampling value of the image.

13. A method for generating an interpolated pixel data *in a digital video system including a processor*, the method comprising generating a set of [the] interpolated pixel data from a set of original pixel data from an original image *using the processor*, wherein interpolated pixel data for a particular pixel is generated by performing operations using [at least one] *the processor*, the operations comprising:

selecting, *with the processor*, original pixel data [for] *including* more than three pixels of the original image; obtaining, *with the processor*, at least a first filter coefficient and a second filter coefficient, the first filter coefficient and the second filter coefficient being configured to interpolate the original pixel data; applying, *with the processor*, the first filter coefficient to the selected original pixel data to produce first interpolated pixel data, the first filter coefficient including weighting factors having at least three different numerical values, wherein *said* applying the first filter coefficient to the selected original pixel data comprises:

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multiplying each of the weighting factors and the selected original pixel data to produce weighted pixel data, and

summing the weighted pixel data to produce the first interpolated pixel data;

multiplying, *with the processor*, the second filter coefficient and the first interpolated pixel data to produce second interpolated pixel data; and

identifying, *with the processor*, the interpolated pixel data *for the particular pixel* as the second interpolated pixel data.

14. The method of claim 13, wherein the second filter coefficient is a matrix that includes one or more individual numeric values.

15. The method of claim 13, wherein the first filter coefficient and the second filter coefficient each comprise at least one integer value.

16. The method of claim 13, wherein a value of the first filter coefficient and a value of the second filter coefficient are one.

17. The method of claim 13, wherein a value of the second filter coefficient is one.

18. The method of claim 13, wherein the original image is obtained from a low-resolution imaging system.

19. The method of claim 13, wherein the second filter coefficient is a point spread function (P) and the first filter coefficient is a bi-linear interpolation filter (B).

20. *The method of claim 13, wherein the operations used for generating the interpolated pixel data for the particular pixel are represented by the following equation:*

$$f=PBz$$

where f represents the interpolated pixel data for the particular pixel, P represents the second filter coefficient, B represents the first filter coefficient, and z represents the original pixel data.

* * * * *

UNITED STATES PATENT AND TRADEMARK OFFICE
CERTIFICATE OF CORRECTION

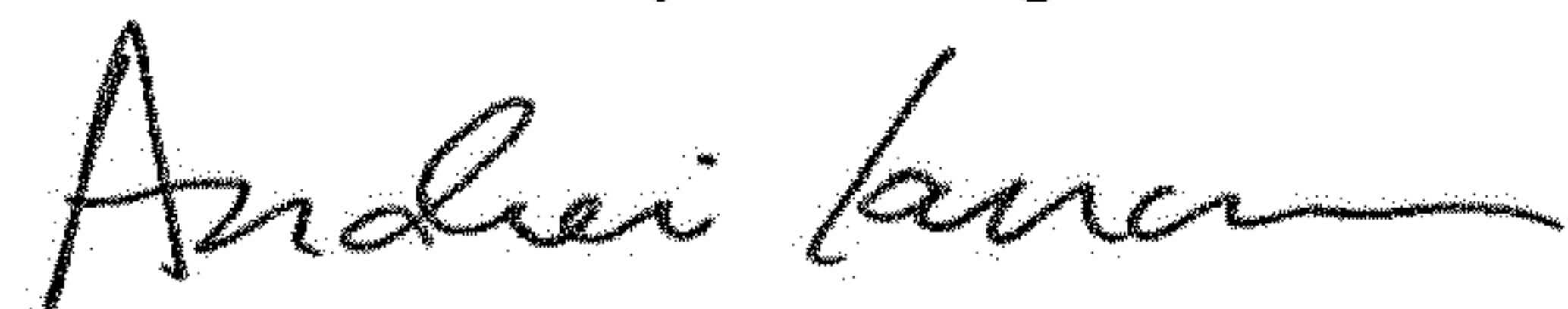
PATENT NO. : RE45,859 E
APPLICATION NO. : 14/472205
DATED : January 19, 2016
INVENTOR(S) : Min-Cheol Hong and Yoon-Seong Soh

Page 1 of 12

It is certified that error appears in the above-identified patent and that said Letters Patent is hereby corrected as shown below:

Please delete Pat. No. RE45859 E in its entirety and insert Pat. No. RE45859 E in its entirety as shown on the attached sheets.

Signed and Sealed this
Seventh Day of August, 2018



Andrei Iancu
Director of the United States Patent and Trademark Office

(19) **United States**
 (12) **Reissued Patent**
Hong et al.

(10) **Patent Number:** **US RE45,859 E**
 (45) **Date of Reissued Patent:** ***Jan. 19, 2016**

(54) **FILTERING CONTROL METHOD FOR IMPROVING IMAGE QUALITY OF BI-LINEAR INTERPOLATED IMAGE**

(58) **Field of Classification Search**
 CPC G06T 3/4007; G06T 3/4053; G06T 5/003; G06T 5/20
 USPC 382/260-264, 298-300; 358/525
 See application file for complete search history.

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(73) Assignee: **LG ELECTRONICS INC., Seoul (JP)**

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(*) Notice: This patent is subject to a terminal disclaimer.

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(21) Appl. No.: **14/472,205**

(22) Filed: **Aug. 28, 2014**

(Continued)

Related U.S. Patent Documents

Reissue of:

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 Issued: **Jan. 18, 2011**
 Appl. No.: **11/546,484**
 Filed: **Oct. 12, 2006**

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Office Action for U.S. Appl. No. 12/024,408, mailed Jun. 29, 2009, 7 pages.

(Continued)

Which is a Reissue of:

(64) Patent No.: **6,803,954**
 Issued: **Oct. 12, 2004**
 Appl. No.: **09/692,156**
 Filed: **Oct. 20, 2000**

Primary Examiner — Adam L Basehoar

(74) *Attorney, Agent, or Firm* — Dentons US LLP

(57) **ABSTRACT**

The present invention relates to an interpolation method for enlarging a digital image or predicting a moving vector of a compressed image system as a sub-pixel unit when the image digitized through a CCD (Charge Coupled Device) camera ect. has a low resolution in a video phone or video conference or general digital video system, particularly the present invention can be adapted to a post processor of a compressed digital image in order to improve the image quality, and can be used for finding a moving vector of a moving picture compressed type, accordingly the present invention is capable of improving the image quality.

(30) **Foreign Application Priority Data**

Oct. 21, 1999 (KR) 1999/45805

(51) **Int. Cl.**
G06K 9/40 (2006.01)
G06T 3/40 (2006.01)
G06T 5/00 (2006.01)
G06T 5/20 (2006.01)

(52) **U.S. Cl.**
 CPC **G06T 3/4007** (2013.01); **G06T 5/003** (2013.01); **G06T 5/20** (2013.01)

20 Claims, 4 Drawing Sheets

| | | | |
|--|----------|---|--|
| $\begin{bmatrix} A \\ B \\ C \\ D \\ E \\ F \\ G \\ H \\ I \\ J \\ K \\ L \\ M \\ N \\ O \\ P \\ Q \\ R \\ S \\ T \\ U \\ V \\ W \\ X \end{bmatrix}$ | $=1/512$ | $\begin{bmatrix} -7 & 81 & -14 & 0 & 52 & 405 & 24 & 0 & -13 & -2 & -14 & 0 & 0 & 0 & 0 & 0 \\ -8 & 23 & 52 & -12 & -9 & 201 & 302 & -12 & -3 & -5 & -13 & -6 & 0 & 0 & 0 & 0 \\ -8 & 43 & -16 & 0 & 99 & 382 & -9 & 0 & -3 & 38 & -14 & 0 & 0 & 0 & 0 & 0 \\ -10 & 38 & -20 & 0 & 54 & 397 & 27 & 0 & -7 & 49 & -16 & 0 & 0 & 0 & 0 & 0 \\ -13 & 33 & -23 & 0 & 10 & 413 & 62 & 0 & -12 & 59 & -17 & 0 & 0 & 0 & 0 & 0 \\ -12 & 26 & -15 & -3 & -4 & 354 & 142 & -5 & -11 & 48 & -4 & -4 & 0 & 0 & 0 & 0 \\ -10 & 17 & -8 & -7 & -13 & 295 & 221 & -9 & -10 & 36 & 9 & -9 & 0 & 0 & 0 & 0 \\ -5 & 4 & 18 & -11 & -9 & 197 & 302 & -9 & -5 & 17 & 24 & -11 & 0 & 0 & 0 & 0 \\ -14 & -6 & -21 & 0 & 56 & 338 & 29 & 0 & -2 & 99 & -17 & 0 & 0 & 0 & 0 & 0 \\ -10 & -7 & -24 & -3 & -5 & 344 & 145 & -5 & -12 & 88 & 7 & -6 & 0 & 0 & 0 & 0 \\ -4 & -13 & -18 & -11 & -10 & 194 & 301 & -6 & -6 & 39 & 60 & -16 & 0 & 0 & 0 & 0 \\ -12 & -13 & -9 & 0 & 53 & 363 & 26 & 0 & 1 & 111 & -8 & 0 & 0 & 0 & 0 & 0 \\ -9 & -14 & -11 & 0 & 19 & 356 & 87 & 0 & -6 & 109 & 1 & 0 & 0 & 0 & 0 & 0 \\ -9 & -9 & -14 & -2 & -9 & 261 & 195 & -5 & -9 & 74 & 45 & -6 & 0 & 0 & 0 & 0 \\ -12 & -5 & -13 & -4 & -5 & 174 & 282 & -9 & -5 & 42 & 79 & -12 & 0 & 0 & 0 & 0 \\ -6 & -10 & -8 & 0 & 19 & 219 & 18 & 0 & 37 & 271 & 6 & 0 & -9 & -16 & -9 & 0 \\ -8 & -9 & -6 & 1 & -11 & 193 & 78 & -4 & -7 & 243 & 83 & -4 & -4 & -14 & -14 & -1 \\ -1 & -8 & -11 & -4 & -8 & 102 & 156 & -13 & -8 & 142 & 206 & -10 & -1 & -11 & -15 & -4 \\ -4 & -5 & -3 & 0 & 23 & 153 & -16 & 0 & 83 & 330 & -13 & 0 & -13 & -16 & -7 & 0 \\ -3 & -5 & -4 & 0 & 6 & 151 & 0 & 0 & 45 & 338 & 15 & 0 & -11 & -9 & -11 & 0 \\ -2 & -5 & -5 & 0 & -10 & 149 & 15 & 0 & 7 & 347 & 43 & 0 & -9 & -2 & -16 & 0 \\ -2 & -4 & -6 & -1 & -12 & 125 & 35 & -4 & -5 & 304 & 111 & -4 & -6 & -3 & -14 & -2 \\ -1 & -4 & -6 & -1 & -14 & 102 & 55 & -8 & -16 & 260 & 179 & -9 & -4 & -4 & -13 & -4 \\ -1 & -4 & -6 & -2 & -7 & 82 & 104 & -12 & -8 & 172 & 255 & -11 & -2 & -9 & -14 & -5 \end{bmatrix}$ | $\begin{bmatrix} a \\ b \\ c \\ d \\ e \\ f \\ g \\ h \\ i \\ j \\ k \\ l \\ m \\ n \\ o \\ p \end{bmatrix}$ |
|--|----------|---|--|

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10 pages.

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FIG. 1

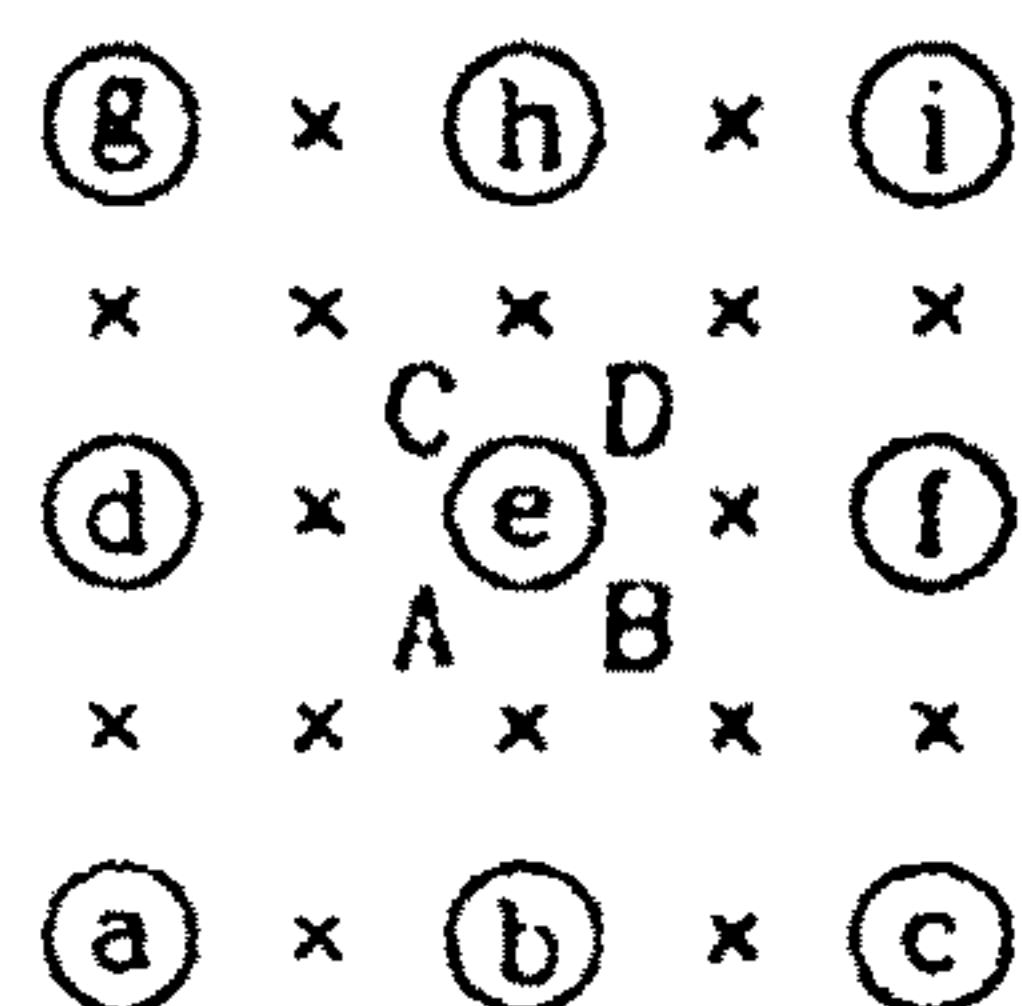


FIG. 2

$$\begin{bmatrix} A \\ B \\ C \\ D \end{bmatrix} = 1/512 \begin{bmatrix} 1 & 94 & -15 & 94 & 391 & -15 & -15 & -15 & -8 \\ -15 & 86 & -9 & -13 & 370 & 113 & -6 & -14 & -18 \\ -15 & -13 & -6 & 86 & 370 & -14 & 9 & 113 & -18 \\ 6 & -14 & -14 & -14 & 349 & 107 & -14 & 107 & 11 \end{bmatrix} \begin{bmatrix} a \\ b \\ c \\ d \\ e \\ f \\ g \\ h \\ i \end{bmatrix}$$

FIG. 3

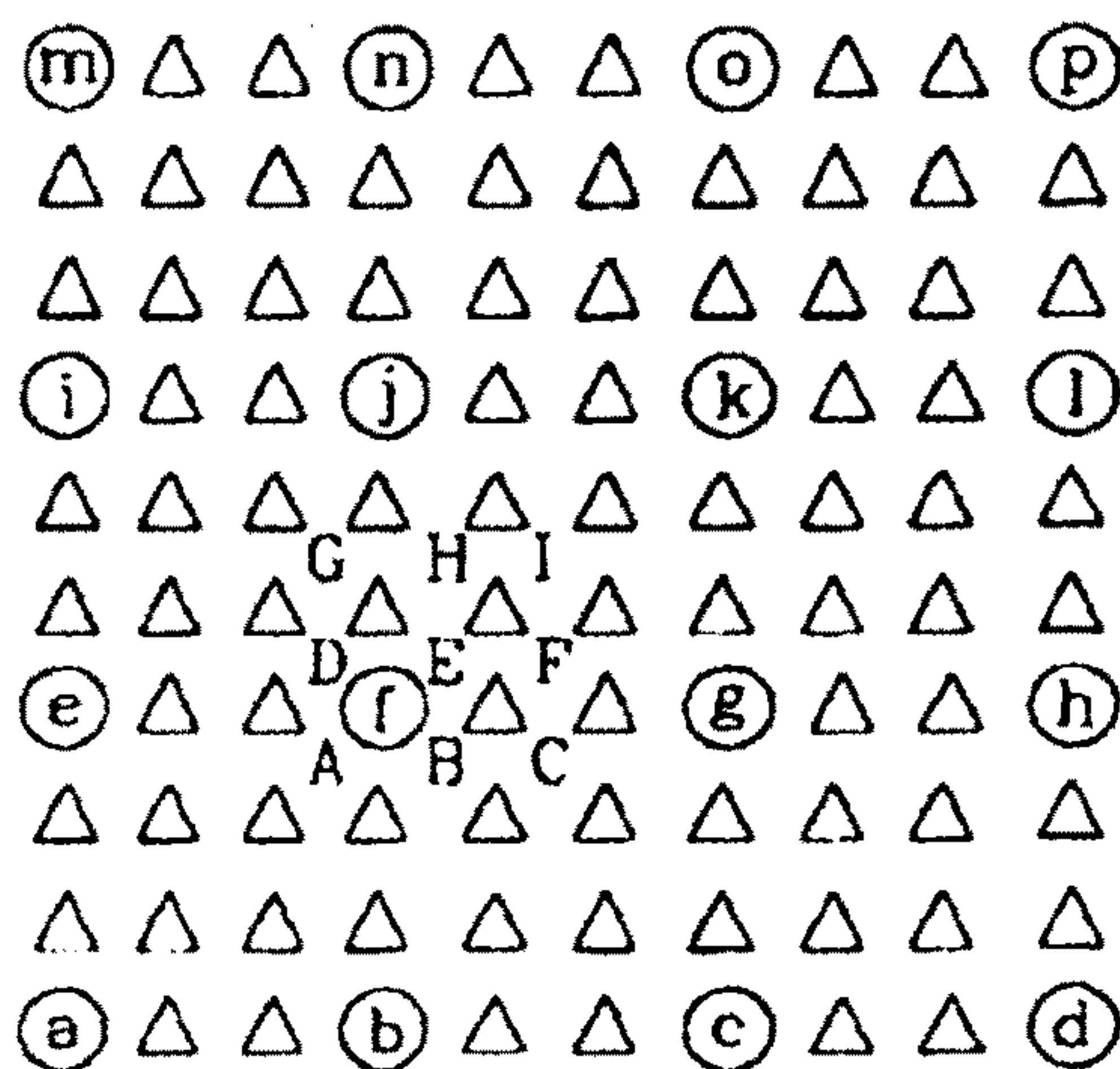


FIG. 4

| | | | | | | | | | | | | | | | | |
|---|-----|-----|-----|----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|----|
| | a | b | c | d | e | f | g | h | i | j | k | l | m | n | o | p |
| A | -4 | 60 | -22 | 0 | 104 | 387 | -3 | 0 | -4 | 7 | -13 | 0 | 0 | 0 | 0 | 0 |
| B | -15 | 71 | -22 | 0 | 11 | 422 | 63 | 0 | -11 | 12 | -19 | 0 | 0 | 0 | 0 | 0 |
| C | -12 | 44 | 9 | -8 | -17 | 307 | 215 | -8 | -6 | 4 | -11 | -5 | 0 | 0 | 0 | 0 |
| D | -16 | -8 | -16 | 0 | 103 | 372 | -3 | 0 | 9 | 91 | -20 | 0 | 0 | 0 | 0 | 0 |
| E | -12 | -4 | -25 | 0 | 9 | 403 | 61 | 0 | -12 | 107 | -15 | 0 | 0 | 0 | 0 | 0 |
| F | -8 | -9 | -23 | -5 | -19 | 284 | 229 | -10 | -13 | 69 | 29 | -12 | 0 | 0 | 0 | 0 |
| G | -8 | -10 | -6 | 0 | 44 | 212 | -16 | 0 | 71 | 269 | -11 | 0 | -11 | -16 | -16 | 0 |
| H | -4 | -9 | -10 | 0 | -6 | 226 | 52 | 0 | 2 | 272 | 22 | 0 | -6 | -15 | -12 | 0 |
| I | -2 | -8 | -12 | -2 | -16 | 160 | 100 | -9 | -15 | 213 | 143 | -2 | -9 | -12 | -15 | -2 |

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FIG. 5

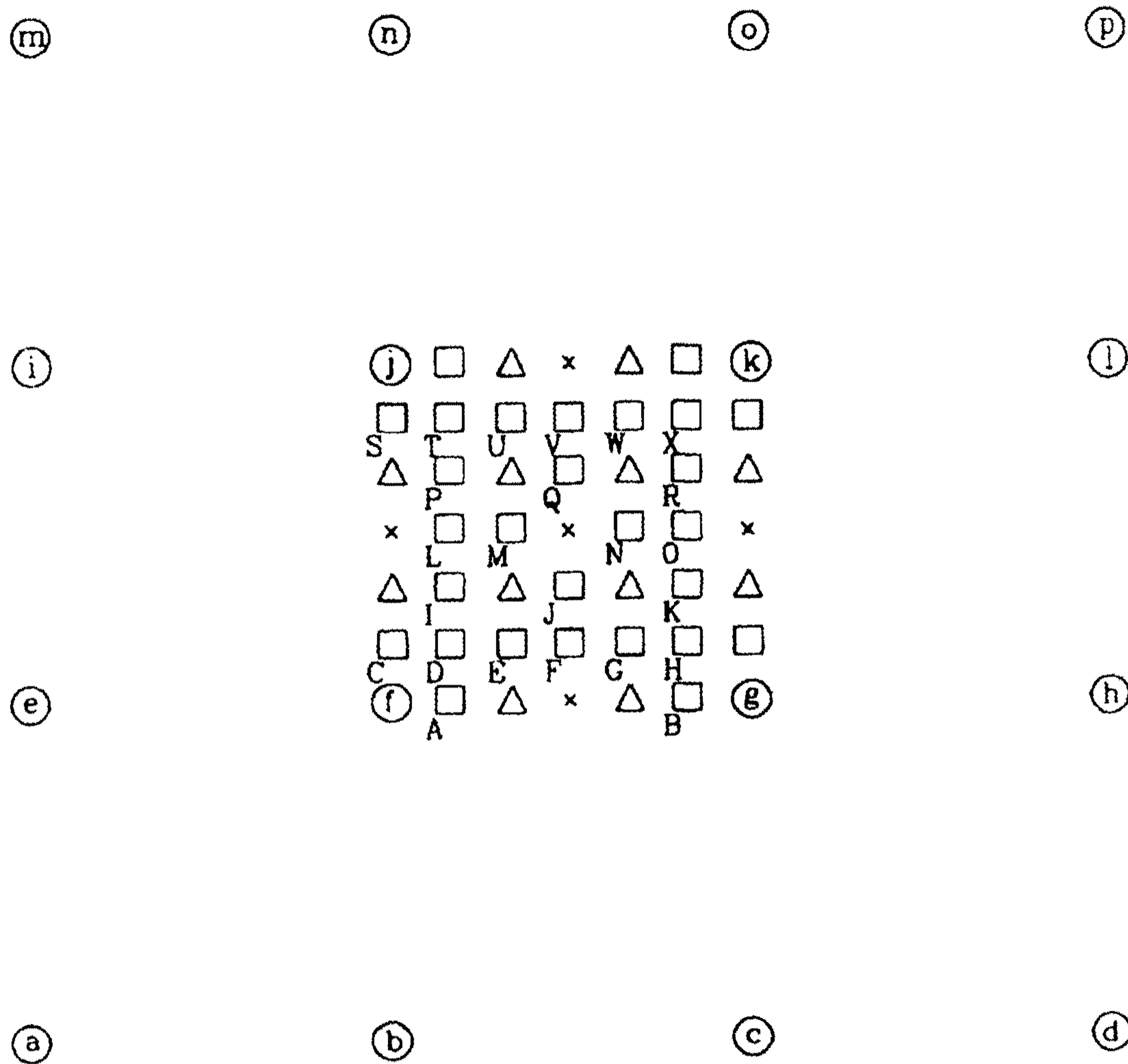


FIG. 6

| | a | b | c | d | e | f | g | h | i | j | k | l | m | n | o | p |
|---|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|----|
| A | -7 | 81 | -14 | 0 | 52 | 405 | 24 | 0 | -13 | -2 | -14 | 0 | 0 | 0 | 0 | 0 |
| B | -6 | 23 | 52 | -12 | -9 | 201 | 302 | -12 | -3 | -5 | -13 | 0 | 0 | 0 | 0 | 0 |
| C | -8 | 43 | -16 | 0 | 99 | 382 | -9 | 0 | -3 | 38 | -14 | 0 | 0 | 0 | 0 | 0 |
| D | -10 | 38 | -20 | 0 | 54 | 397 | 27 | 0 | -7 | 49 | -16 | 0 | 0 | 0 | 0 | 0 |
| E | -13 | 33 | -23 | 0 | 10 | 413 | 62 | 0 | -12 | 59 | -17 | 0 | 0 | 0 | 0 | 0 |
| F | -12 | 26 | -15 | -3 | -4 | 354 | 142 | -5 | -11 | 48 | -4 | -4 | 0 | 0 | 0 | 0 |
| G | -10 | 17 | -8 | -7 | -13 | 295 | 221 | -9 | -10 | 36 | 9 | -9 | 0 | 0 | 0 | 0 |
| H | -5 | 4 | 18 | -11 | -9 | 197 | 302 | -9 | -5 | 17 | 24 | -11 | 0 | 0 | 0 | 0 |
| I | -14 | -6 | -21 | 0 | 56 | 338 | 29 | 0 | -2 | 99 | -17 | 0 | 0 | 0 | 0 | 0 |
| J | -10 | -7 | -24 | -3 | -5 | 344 | 145 | -5 | -12 | 88 | 7 | -6 | 0 | 0 | 0 | 0 |
| K | -4 | -13 | -16 | -11 | -10 | 194 | 301 | -6 | -6 | 39 | 60 | -16 | 0 | 0 | 0 | 0 |
| L | -12 | -13 | -9 | 0 | 53 | 363 | 26 | 0 | 1 | 111 | -8 | 0 | 0 | 0 | 0 | 0 |
| M | -9 | -14 | -11 | 0 | 18 | 356 | 67 | 0 | -6 | 109 | 1 | 0 | 0 | 0 | 0 | 0 |
| N | -9 | -9 | -14 | -2 | -9 | 261 | 195 | -5 | -9 | 74 | 45 | -6 | 0 | 0 | 0 | 0 |
| O | -12 | -5 | -13 | -4 | -5 | 174 | 282 | -9 | -5 | 42 | 79 | -12 | 0 | 0 | 0 | 0 |
| P | -6 | -10 | -8 | 0 | 19 | 219 | 18 | 0 | 37 | 271 | 6 | 0 | -16 | -9 | -14 | -1 |
| Q | -8 | -9 | -6 | 1 | -11 | 193 | 76 | -4 | -7 | 243 | 83 | -4 | -14 | -14 | -15 | -4 |
| R | -1 | -8 | -11 | -4 | -8 | 102 | 156 | -13 | -8 | 142 | 208 | -10 | -11 | -11 | -7 | 0 |
| S | -4 | -5 | -3 | 0 | 23 | 153 | -16 | 0 | 83 | 330 | -13 | 0 | -16 | -9 | -11 | 0 |
| T | -3 | -5 | -4 | 0 | 6 | 151 | 0 | 0 | 45 | 338 | 15 | 0 | -9 | -2 | -16 | 0 |
| U | -2 | -5 | -5 | 0 | -10 | 149 | 15 | 0 | 7 | 347 | 43 | 0 | -3 | -14 | -2 | 0 |
| V | -2 | -4 | -6 | -1 | -12 | 125 | 35 | -4 | -5 | 304 | 111 | -4 | -6 | -14 | -4 | -2 |
| W | -1 | -4 | -6 | -1 | -14 | 102 | 55 | -8 | -16 | 260 | 179 | -9 | -4 | -13 | -4 | -4 |
| X | -1 | -4 | -6 | -2 | -7 | 62 | 104 | -12 | -8 | 172 | 255 | -11 | -9 | -14 | -5 | -5 |

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FILTERING CONTROL METHOD FOR IMPROVING IMAGE QUALITY OF BI-LINEAR INTERPOLATED IMAGE

Matter enclosed in heavy brackets [] appears in the original patent but forms no part of the first and this reissue specification; matter printed in italics indicates the additions made by the first reissue. Matter enclosed in double heavy brackets [[]] appears in the first reissue patent but forms no part of this reissue specification; matter printed in bold face indicates the additions made by this reissue; a claim printed with strikethrough indicates that the claim was canceled, disclaimed, or held invalid by a prior post-patent action or proceeding.

CROSS-REFERENCE TO RELATED APPLICATIONS

This is a reissue of U.S. Pat. No. RE42,045, issued on Jan. 18, 2011, which is a reissue of U.S. Pat. No. 6,803,954 issued Oct. 12, 2004. More than one reissue application has been filed for the reissue of U.S. Pat. No. 6,803,954. U.S. patent application Ser. No. 11/546,484 is a reissue of U.S. Pat. No. 6,803,954; U.S. patent application Ser. No. 12/024,408, now abandoned, is a divisional reissue of U.S. Pat. No. 6,803,954; and U.S. patent application Ser. No. 12/424,927 is a continuation reissue of U.S. patent application Ser. No. 11/546,484, the entire contents of each are hereby incorporated by reference.

BACKGROUND OF THE INVENTION

1. Field of the Invention

The present invention relates to an interpolation method adapted to enlargement of a low resolution image when the image digitized through a CCD (Charged-Coupled Device) has the low resolution, in particular to a filtering control method for improving the image quality of a bi-linear interpolated image which is capable of restoring a requested interpolated high resolution image from a low resolution image by finding a coefficient of a two-dimensional filter on the basis of a regularization image restoration method.

2. Description of the Prior Art

In the conventional technology, a still picture or a moving picture has or transmits a low resolution image because it can not physically satisfy a sensor having the low resolution or a nyquist value.

In addition, a compressed moving picture has or transmits the low resolution image due to its bit value problem.

For example, when the compressed moving picture having the low bit value is transmitted to a receiver and the receiver enlarges the transmitted moving picture, the resolution of the transmitted moving picture lowers due to a degradation phenomenon ect.

Accordingly, a method for getting a high resolution image from a low resolution image is required.

In the meantime, the method for getting the high resolution image from the low resolution image is largely divided into an image expansion type method and an image enhancement type method.

First, the image expansion type method converts the size of the low resolution image into a requested size. The bi-linear interpolation method, a zero order expansion method, and a cubic spline method are comprised in the image expansion type method.

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However, as described above, the image expansion type method has an image visibility lowering problem because when the image is interpolation-restored by the above-mentioned method such as the bi-linear interpolation method, zero order hold expansion method, cubic spline method, the outlines of the image is over-blurred.

Meanwhile, the image enhancement type method comprises many methods, but the image enhancement type method causes a computational complexity, accordingly the method is not suited to a real-time processing due to the its computational complexity.

In addition, when the image enhancement type method is used for getting the high resolution image from the low resolution image, setting of each parameter is not adaptable.

For example, there is a POCS (Projection Onto Convex Set) method for increasing the resolution of an image. In the POCS method, in use of time region information, it is assumed as correlation between the images is uniformly same, but actually the correlation between the images is not uniform.

In addition, there is a mapping method for mapping a non-uniform sample of the low resolution image into a uniform sample of the high resolution image by using moving information and segmentation information of the image. However, the mapping method has the computational complexity problem, accordingly the mapping method is not suited to the real-time image data processing of the image processing system.

SUMMARY OF THE INVENTION

The object of the present invention is to provide a filtering control method for improving the image quality of a bi-linear interpolated image which is capable of improving the image quality of the interpolated image by using an interpolation method considering a real-time processing, a computational complexity and an efficiency when the digital video system seeks the interpolated image from the low resolution image.

The other object of the present invention is to provide the filtering control method for improving the image quality of the bi-linear interpolated image which is capable of finding a two-dimensional filter coefficient for getting the interpolated image from the low resolution image on the basis of a regularization image restoration method.

The other object of the present invention is to provide the filtering control method for improving the image quality of the bi-linear interpolated image which can approximate and find a PSF (Point Spread Function) for the bi-linear interpolated image from a modeling of the degraded image in the frequency region.

The other object of the present invention is to provide the filtering control method for improving the image quality of the bi-linear interpolated image which is capable of performing a real-time adaptive processing by finding a filter coefficient from the bi-linear interpolated image and approximated PSF.

In the present invention, in order to find a filter coefficient for finding the interpolated image from the low resolution image on the basis of the regularization image restoration method, when H is the PSF (Point Spread Function), f is a requested high resolution image, Z is the low resolution image, g is the high resolution image gotten from the bi-linear interpolation method, an added function $M(f) = \|g - Hf\|^2 + \alpha \|Cf\|^2$ for finding the PSF(H) from an equation $g = Bz = Hf + n$ (B, H are bi-linear interpolated filters, n is a noise component generated by the assumed H) is defined.

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The filtering control method for improving the image quality of the bi-linear interpolated image can be implemented by finding the PSF(H) from the added function M(f) by using an equation

$$H(k, l) = \frac{G(k, l)}{F(k, l)}$$

The filtering control method for improving the image quality of the bi-linear interpolated image can be implemented by finding a PSF(P) of a f=Pg function by using an equation

$$P(k, l) = \frac{H*(k, l)}{H*(k, l)H(k, l) + C*(k, l)C(k, l)}$$

after finding the PSF(H).

The filtering control method for improving the image quality of the bi-linear interpolated image can restore the requested high resolution image(f) by finding an added filter coefficient Q of the PSF(P) and interpolation filter B from the equation f=Pg=PBz=Qz.

BRIEF DESCRIPTION OF THE DRAWINGS

FIG. 1 illustrates an image sample for getting a twice enlarged high resolution image according to the embodiment of the present invention.

FIG. 2 illustrates an interpolation filter coefficient for getting the twice enlarged image according to the embodiment of the present invention.

FIG. 3 illustrates an image sample for getting a three times enlarged high resolution image according to the other embodiment of the present invention.

FIG. 4 illustrates the interpolation filter coefficient for getting the three times enlarged image according to the other embodiment of the present invention.

FIG. 5 illustrates an image sample for getting a six times enlarged high resolution image according to the another embodiment of the present invention.

FIG. 6 illustrates the interpolation filter coefficient for getting the six times enlarged image according to the another embodiment of the present invention.

DETAILED DESCRIPTION OF THE PREFERRED EMBODIMENT

FIG. 1 illustrates an image sample for getting a twice enlarged high resolution image according to the embodiment of the present invention.

As depicted in FIG. 1, a~i illustrate low resolution pixels, A~D illustrate high resolution pixels. In addition, pixels depicted as 'x' illustrate pixels interpolated as twice by a twice interpolation filter coefficient.

FIG. 2 illustrates the interpolation filter coefficient for getting a twice enlarged image according to the embodiment of the present invention. In other words, the interpolation filter coefficient for interpolating the twice enlarged image of FIG. 1 is depicted in FIG. 2.

As depicted in FIG. 2, the high resolution image is gotten from the low resolution pixels a~i (3x3 pixels) inside of a circle of FIG. 1 by using the interpolation filter coefficient.

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FIG. 3 illustrates an image sample for getting a three times enlarged high resolution image according to the other embodiment of the present invention.

As depicted in FIG. 3, a~p illustrate the low resolution pixels, A~I illustrate the high resolution pixels using the filter according to the present invention.

FIG. 4 illustrates the interpolation filter coefficient for getting the three times enlarged image according to the other embodiment of the present invention.

As depicted in FIG. 4, three times enlarged pixels which are newly generated illustrated as triangles in FIG. 3 are gotten from the low resolution pixels a~p (4x4 pixels) by using the interpolation filter coefficient of FIG. 4.

FIG. 5 illustrates the image sample for getting a six times enlarged high resolution image according to the another embodiment of the present invention. In other words, it illustrates the image sample for getting the six times enlarged high resolution image from the twice and three times interpolation filter coefficients by using the bi-linear interpolation method.

As depicted in FIG. 5, pixels illustrated as a 'X' can be gotten by using the twice interpolation filter of FIG. 2, and pixels illustrated as a triangle can be gotten by using the three times interpolation filter coefficient of FIG. 4.

In addition, pixels illustrated as a quadrilateral can be gotten from the pixels generated by the twice and three times interpolation filter coefficients by using the bi-linear interpolation method.

FIG. 6 illustrates the interpolation filter coefficient for getting the six times enlarged image according to the another embodiment of the present invention. In other words, the interpolation filter coefficient for getting the six times enlarged image of FIG. 5 is depicted in FIG. 6.

Meanwhile, as depicted in FIG. 2, FIG. 4 and FIG. 6, the value found by using the interpolation filter coefficient of the present invention has an integer value.

In addition, a 9 bit shift is performed to the value calculated by the interpolation filter coefficient, accordingly there is no need to perform a floating point operation processing.

The twice, three times, six times interpolated images are depicted in FIG. 1~FIG. 6, however the present invention is not limited by that, it can be adapted freely to a certain interpolation value.

Hereinafter, the filtering control method for improving the image quality of the bi-linear interpolated image will be described in more detail.

First, a spatially invariant PSF (Point Spread Function) for finding the interpolation filter coefficient according to the each interpolation value can be easily analyzed and approximated in the frequency region, accordingly the spatially invariant PSF (Point Spread Function) is considered from the bi-linear interpolated image.

After that, when it is assumed as the low resolution image is z, high resolution image gotten by the bi-linear interpolation method is g, high resolution image to be restored is f, the relation between the each image can be described as below.

$$g=Bz=Hf+n \quad \text{[Equation 1]}$$

Herein, the B, H, n are the bi-linear interpolation filters, H is the spatially invariant PSF defining the relation between the original high resolution image and high resolution image gotten by the interpolation method, and the n is a noise component generated by the assumed H.

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Herein, when the noise component is neglected and a direct inverse is used in order to find the PSF(H), the PSF(H) can be described as below equation 2 in the frequency region.

$$H(k, l) = \frac{G(k, l)}{F(k, l)} \quad \text{[Equation 2]}$$

Herein, the H(k,l) is the component in the k,l frequency region of the PSF(H), the G (k,l) is the component in the k,l frequency region of the bi-linear interpolated image. In addition, the F (k,l) is the component in the k,l frequency region of the high resolution image.

Meanwhile, the high resolution image f to be restored is unknown, the PSF(H) can be gotten from the bi-linear interpolated high resolution image through a statistical processing after performing an under-sample processing of various images as various value.

Herein, the high resolution image is gotten by using the PSF(H) found from the direct inverse. In other words, there is a system stabilization problem because the high resolution image gotten from the PSF(H) by using the direct inverse is overshoot in the region where the k,l have '0' value (in general, high frequency region) in the frequency region, accordingly the regularization image restoration for improving the system stabilization is used to solve the problem.

The regularization image restoration method is used for restoring the image or finding a certain PSF, an added function M(f) for finding the PSF(H) by using the regularization image restoration method can be described as below equation 3.

$$M(f) = \|g - Hf\|^2 + \alpha \|Cf\|^2 \quad \text{[Equation 3]}$$

Herein, the first term of the right side of Equation 3 illustrates the credibility of the bi-linear interpolated image, the second term of the right side illustrates increase of the stability of the system by providing the mitigation to the restored image.

In addition, the $\|\cdot\|$ means a norm, the α is a regularization parameter for determining the credibility and mitigation of the original image. In addition, the C is the two-dimensional high frequency filter for determining the mitigation of the original image, in the present invention a two-dimensional Gaussian filter is used as the C.

When a gradient operator is adapted to Equation 3 in order to get the high resolution image, it can be described as below equation 4.

$$\square M(f) = -2H^T(g - Hf) + 2\alpha C^T Cf = 0 \quad \text{[Equation 4]}$$

Herein, the T means a transpose of a matrix.

Meanwhile, conventionally a repetition method is used in order to get the high resolution image and regularization parameter, but it is not suited to the moving picture processing because the method causes lots of computational complexity.

Accordingly, in the present invention, the regularization parameter α is fixed as '1', and the high resolution image f can be found as below equation 5.

$$f = \frac{H^T g}{(H^T H + C^T C)} = Pg \quad \text{[Equation 5]}$$

When the PSF(P) is found by Equation 5, PSF(P)=H/(H^TH+C^TC) requires the lots of computational complexity

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for calculating an inverse matrix, however the PSF(P) in Equation 5 is a block-circulant matrix, accordingly it can be easily calculated in the frequency region.

Accordingly, the PSF(P) can be found finally as below Equation 6.

$$P(k, l) = \frac{H^*(k, l)}{H^*(k, l)H(k, l) + C^*(k, l)C(k, l)} \quad \text{[Equation 6]}$$

Herein, the '*' means a complex-conjugate.

The PSF(P) can be found by using an IFT (Inverse Fourier Transform) from Equation 6.

The requested high resolution image f can be found as below Equation 7 by using the found PSF(P) and Equation 1.

$$f = Pg = PBz = Qz \quad \text{[Equation 7]}$$

The PSF(P) is the spatially invariant function, the bi-linear interpolation filter B can be easily found by the conventional technology, accordingly the added filter coefficient Q of the PSF(P) and bi-linear interpolation filter B can be found.

Herein, in order to reduce the computational complexity, the number of a kernel of the PSF(P) is set in accordance with the up-sampling value.

When the up-sampling value is 2 in the present invention, the number of the kernel is limited as 3, when the up-sampling value is 3, the number of the kernel is limited as 4.

When the up-sampling value is 2, it can be used in an application segment for enlarging the size of the image as twice at a post processor of the compressed digital image and in finding of a sub-pixel moving vector in a H.263 moving picture compressed method.

In addition, when the up-sampling value is 3, it can be used in using of a 1/3 unit moving vector in a H.261, moving picture compressed method.

Herein, the H.263 and H.261 are moving picture compressed standards presented in the ITU-T (International Telecommunications Union-Telecommunication).

As described above, the present invention can be used for improving the image quality at the post processor of the compressed digital image by using the interpolation method for getting the interpolated high resolution image from the low resolution image when the resolution of the digital image lowers due to the low resolution image sensor.

In addition, the interpolation method of the present invention can improve the image quality by finding the moving vector of the moving picture compressed type.

What is claimed is:

1. A filtering control method for improving the image quality of a bi-linear interpolated image when recovering a high resolution image from a low resolution image, the method comprising performing operations using at least one processor, the operations comprising:

restoring a requested high resolution image f by finding an added filter coefficient Q of a PSF(P) and a bi-linear interpolation filter B from an equation $f = Pg = PBz = Qz$, wherein f is the high resolution image as requested, P is the PSF (Point Spread Function), g is the high resolution image found by the bi-linear interpolation method, and z is the low resolution image;

wherein the high resolution image f [can be] is restored by performing an added function M(f) definition process for finding the PSF(H) from an equation

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$g=Bz=Hf+n$, wherein B, H are bi-linear interpolation filters, and n is a noise component generated by the assumed H; and

wherein the added function M(f) is defined as $M(f)=\|g-Hf\|^2+\alpha\|Cf\|^2$, wherein α is a regularization parameter, and C is a two-dimensional high frequency filter for finding mitigation of the original image.

2. The filtering control method for improving the image quality of the bi-linear interpolated image according to claim 1, wherein the regularization parameter α is fixed as '1' in order to reduce a computational complexity.

3. The filtering control method for improving image quality of the bi-linear interpolated image according to claim 1, wherein a two-dimensional gaussian filter is used as the two-dimensional high frequency filter C in order to determine the mitigation of the original image.

4. A filtering control method for improving the image quality of a bi-linear interpolated image when recovering a high resolution image from a low resolution image, *the method comprising performing operations using at least one processor, the operations comprising:*

restoring a requested high resolution image f by finding an added filter coefficient Q of a PSF(P) and a bi-linear interpolation filter B from an equation $f=Pg=PBz=Qz$, wherein f is the high resolution image as requested, P is the PSF (Point Spread Function), g is the high resolution image found by the bi-linear interpolation method, and z is the low resolution image;

wherein the high resolution image f **[[can be]]** is restored by performing an added function M(f) definition process for finding the PSF(H) from an equation $g=Bz=Hf+n$, wherein B, H are bi-linear interpolation filters, and n is a noise component generated by the assumed H;

wherein the high resolution image f is restored by finding a PSF(P) of a $f=Pg$ function after finding the PSF(H) from the added function M(f); and

wherein the PSF(H) is found by using an equation

$$H(k, l) = \frac{G(k, l)}{F(k, l)}$$

G(k,l) is the component in the k,l frequency region of the bi-linear interpolated image, and F(k,l) is the component in the k,l frequency region of the high resolution image.

5. A filtering control method for improving the image quality of a bi-linear interpolated image when recovering a high resolution image from a low resolution image, *the method comprising performing operations using at least one processor, the operations comprising:*

restoring a requested high resolution image f by finding an added filter coefficient Q of a PSF(P) and a bi-linear interpolation filter B from an equation $f=Pg=PBz=Qz$, wherein f is the high resolution image as requested, P is the PSF (Point Spread Function), g is the high resolution image found by the bi-linear interpolation method, and z is the low resolution image;

wherein the PSF(P) **[[can be]]** is found by getting an IFT (Inverse Fourier Transform) by an equation

$$P(k, l) = \frac{H^*(k, l)}{H^*(k, l)H(k, l) + C^*(k, l)C(k, l)}$$

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H(k,l) is a component in the k,l frequency region of the PSF(H), and C is a two-dimensional high frequency filter.

6. The filtering control method for improving the image quality of the bi-linear interpolated image according to claim 5, wherein the number of a **[[kernel]]** kernel of the PSF(P) is set in accordance with an up-sampling value of the image.

7. A filtering control method for improving the image quality of a bi-linear interpolated image when recovering a high resolution image from a low resolution image, *the method comprising performing operations using at least one processor the operations comprising:*

defining an added function M(f) for finding a PSF(H) from an equation $g=Bz=Hf+n$ (wherein B, H are bi-linear filters, n is a noise component generated by an assumed H when the H is a PSF (Point Spread Function), f is a requested high resolution image, z is a low resolution image, and g is a high resolution image gotten by the bi-linear interpolation method);

finding a PSF(P) of a $f=Pg$ function after finding the PSF (H) from the defined added function M(f); and

restoring the requested high resolution image f by finding an added filter coefficient Q of the PSF(P) and interpolation filter B from the equation $f=Pg=PBz=Qz$;

wherein the added function M(f) is defined as $M(f)=\|g-Hf\|^2+\alpha\|Cf\|^2$, wherein α is a regularization parameter, and C is a two-dimensional high frequency filter for finding the mitigation of the original image.

8. The filtering control method for improving the image quality a of the bi-linear interpolated image according to claim 7, wherein the regularization parameter α is fixed as '1' in order to reduce a computational complexity.

9. The filtering control method for improving image quality of the bi-linear interpolated image according to claim 7, wherein a two-dimensional gaussian filter is used as the two-dimensional high frequency filter C in order to determine the mitigation of the original image.

10. A filtering control method for improving the image quality of a bi-linear interpolated image when recovering a high resolution image from a low resolution image, *the method comprising performing operations using at least one processor the operations comprising:*

defining an added function M(f) for finding a PSF(H) from an equation $g=Bz=Hf+n$ (wherein B, H are bi-linear filters, n is a noise component generated by an assumed H when the H is a PSF (Point Spread Function), f is a requested high resolution image, z is a low resolution image, and g is a high resolution image gotten by the bi-linear interpolation method);

finding a PSF(P) of a $f=Pg$ function after finding the PSF (H) from the defined added function M(f); and

restoring the requested high resolution image f by finding an added filter coefficient Q of the PSF(P) and interpolation filter B from the equation $f=Pg=PBz=Qz$;

wherein the PSF(H) is found by an equation

$$H(k,l)=(G(k,l)/F(-k,l).$$

wherein G(k,l) is the component in the k,l frequency region of the bi-linear interpolated image, and F(k,l) is the component in the k,l frequency region of the high resolution image.

11. A filtering control method for improving the image quality of a bi-linear interpolated image when recovering a high resolution image from a low resolution image, *the method comprising performing operations using at least one processor, the operations comprising:*

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defining an added function M(f) for finding a PSF(H) from an equation $g=Bz=Hf+n$ (wherein B, H are bi-linear filters, n is a noise component generated by an assumed H when the H is a PSF (Point Spread Function), f is a requested high resolution image, z is a low resolution image, and g is a high resolution image gotten by the bi-linear interpolation method); finding a PSF(P) of a $f=Pg$ function after finding the PSF (H) from the defined added function M(f); and restoring the requested high resolution image f by finding an added filter coefficient Q of the PSF(P) and interpolation filter B from the equation $f=Pg=PBZ=Qz$; wherein the PSF(P) is found by using an IFT (Inverse Fourier Transform) by an equation

$$P(k, l) = \frac{H^*(k, l)}{H^*(k, l)H(k, l) + C^*(k, l)C(k, l)}$$

H(k,l) is a component in the k,l frequency region of the PSF(H), and C is a two-dimensional high frequency filter.

12. The filtering control method for improving the image quality of the bi-linear interpolated image according to claim 11, wherein the number of a [kernel] kernel of the PSF(P) is differently set in accordance with an up-sampling value of the image.

13. A method for generating an interpolated pixel data in a digital video system including a processor, the method comprising generating a set of [the] interpolated pixel data from a set of original pixel data from an original image using the processor, wherein interpolated pixel data for a particular pixel is generated by performing operations using [at least one] the processor, the operations comprising: selecting, with the processor, original pixel data [for] including more than three pixels of the original image; obtaining, with the processor, at least a first filter coefficient and a second filter coefficient, the first filter coefficient and the second filter coefficient being configured to interpolate the original pixel data; applying, with the processor, the first filter coefficient to the selected original pixel data to produce first inter-

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polated pixel data, the first filter coefficient including weighting factors having at least three different numerical values, wherein said applying the first filter coefficient to the selected original pixel data comprises: multiplying each of the weighting factors and the selected original pixel data to produce weighted pixel data, and summing the weighted pixel data to produce the first interpolated pixel data; multiplying, with the processor, the second filter coefficient and the first interpolated pixel data to produce second interpolated pixel data; and identifying, with the processor, the interpolated pixel data for the particular pixel as the second interpolated pixel data.

14. The method of claim 13, wherein the second filter coefficient is a matrix that includes one or more individual numeric values.

15. The method of claim 13, wherein the first filter coefficient and the second filter coefficient each comprise at least one integer value.

16. The method of claim 13, wherein a value of the first filter coefficient and a value of the second filter coefficient are one.

17. The method of claim 13, wherein a value of the second filter coefficient is one.

18. The method of claim 13, wherein the original image is obtained from a low-resolution imaging system.

19. The method of claim 13, wherein the second filter coefficient is a point spread function (P) and the first filter coefficient is a bi-linear interpolation filter (B).

20. The method of claim 13, wherein the operations used for generating the interpolated pixel data for the particular pixel are represented by the following equation:

$$f=PBz$$

where f represents the interpolated pixel data for the particular pixel, P represents the second filter coefficient, B represents the first filter coefficient, and z represents the original pixel data.

* * * * *

UNITED STATES PATENT AND TRADEMARK OFFICE
CERTIFICATE OF CORRECTION

PATENT NO. : RE45,859 E
APPLICATION NO. : 14/472205
DATED : January 19, 2016
INVENTOR(S) : Hong et al.

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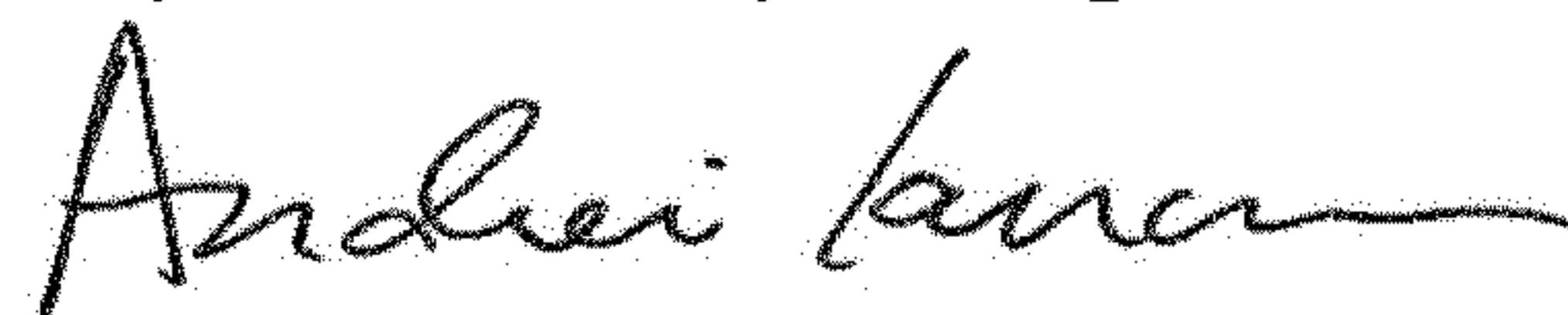
It is certified that error appears in the above-identified patent and that said Letters Patent is hereby corrected as shown below:

In the Specification

At Column 1, under the heading "CROSS-REFERENCE TO RELATED APPLICATIONS," replace Lines 20-29 (approx.), with the following:

--NOTICE: More than one reissue application has been filed for the reissue of U.S. Reissue Patent No. RE42,045 E. The reissue applications are U.S. Reissue Patent Application Nos. 14/963,818, 14/963,765, 14/962,608, 14/962,578, 14/961,345, 14/961,306, 14/961,275, 14/959,697, 14/959,662, and 14/472,205. The relationships of the reissue applications are U.S. Reissue Patent Application Serial Nos. 14/963,818 and 14/963,765, each filed on December 9, 2015, now U.S. Reissue Patent No. RE47,291 E, issued March 12, 2019, and now abandoned, respectively, together with U.S. Reissue Patent Application Serial Nos. 14/962,608 and 14/962,578, each filed on December 8, 2015, now U.S. Reissue Patent No. RE47,274 E, issued March 5, 2019, and now abandoned, respectively, U.S. Reissue Patent Application Serial Nos. 14/961,345, 14/961,306, and 14/961,275, each filed on December 7, 2015, now abandoned, now U.S. Reissue Patent No. RE47,238 E, issued February 12, 2019, and now U.S. Reissue Patent No. RE47,310 E, issued March 19, 2019, respectively, and U.S. Reissue Patent Application Serial Nos. 14/959,697 and 14/959,662, each filed on December 4, 2015, now U.S. Reissue Patent Nos. RE47,337 E and RE47,341 E, respectively, issued April 2, 2019 and April 9, 2019, respectively, each of which ('818, '765, '608, '578, '345, '306, '275, '697, and '662) is a continuation reissue application of U.S. Reissue Patent Application Serial No. 14/472,205 (the present application), filed on August 28, 2014, now U.S. Reissue Patent No. RE45,859 E, issued January 19, 2016, which is a reissue application of U.S. Reissue Patent Application Serial No. 11/546,484, filed on October 12, 2006, now U.S. Reissue Patent No. RE42,045 E, issued January 18, 2011,--

Signed and Sealed this
Twenty-second Day of September, 2020



Andrei Iancu
Director of the United States Patent and Trademark Office