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(54) JOINT ADAPTIVE OPTIMIZATION OF SOFT DECISION DEVICE AND FEEDBACK EQUALIZER

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- (63) Continuation-in-part of application No. 10/322,299, filed on Dec. 17, 2002, now abandoned.
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 H03H 7/30 (2006.01)

 H03H 7/40 (2006.01)

 H03K 5/159 (2006.01)

See application file for complete search history.

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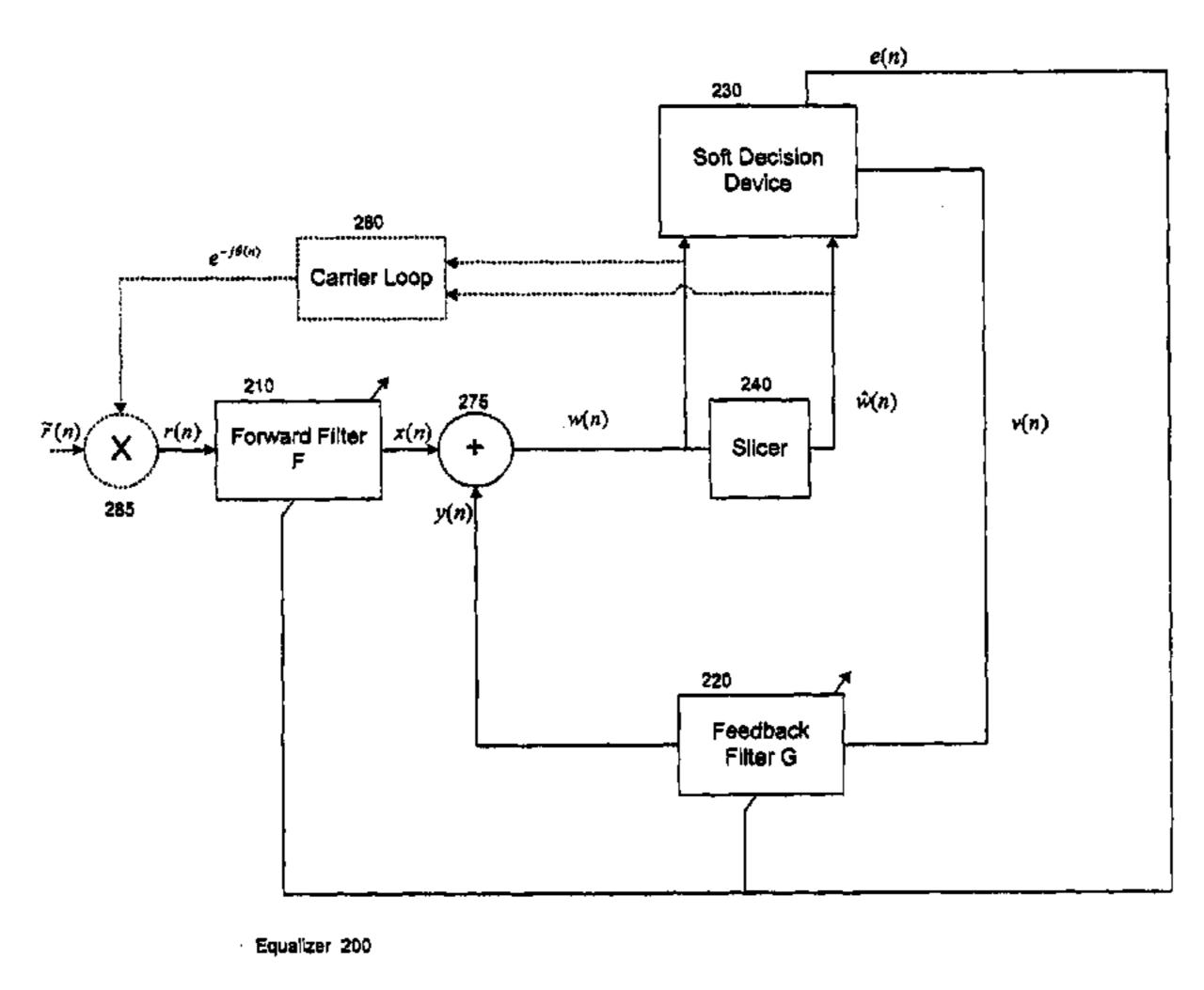
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(57) ABSTRACT

The present invention uses a novel adaptive soft decision device in order to jointly optimize decision device and DFE operation. The soft decision device receives the input and output samples of the slicer and generates a feedback sample by non-linearly combining them with respect to a single decision reference parameter. Moreover, the soft decision device provides novel error terms used to adapt equalizer coefficients in order to jointly optimize decision device and equalizer coefficients.

9 Claims, 7 Drawing Sheets



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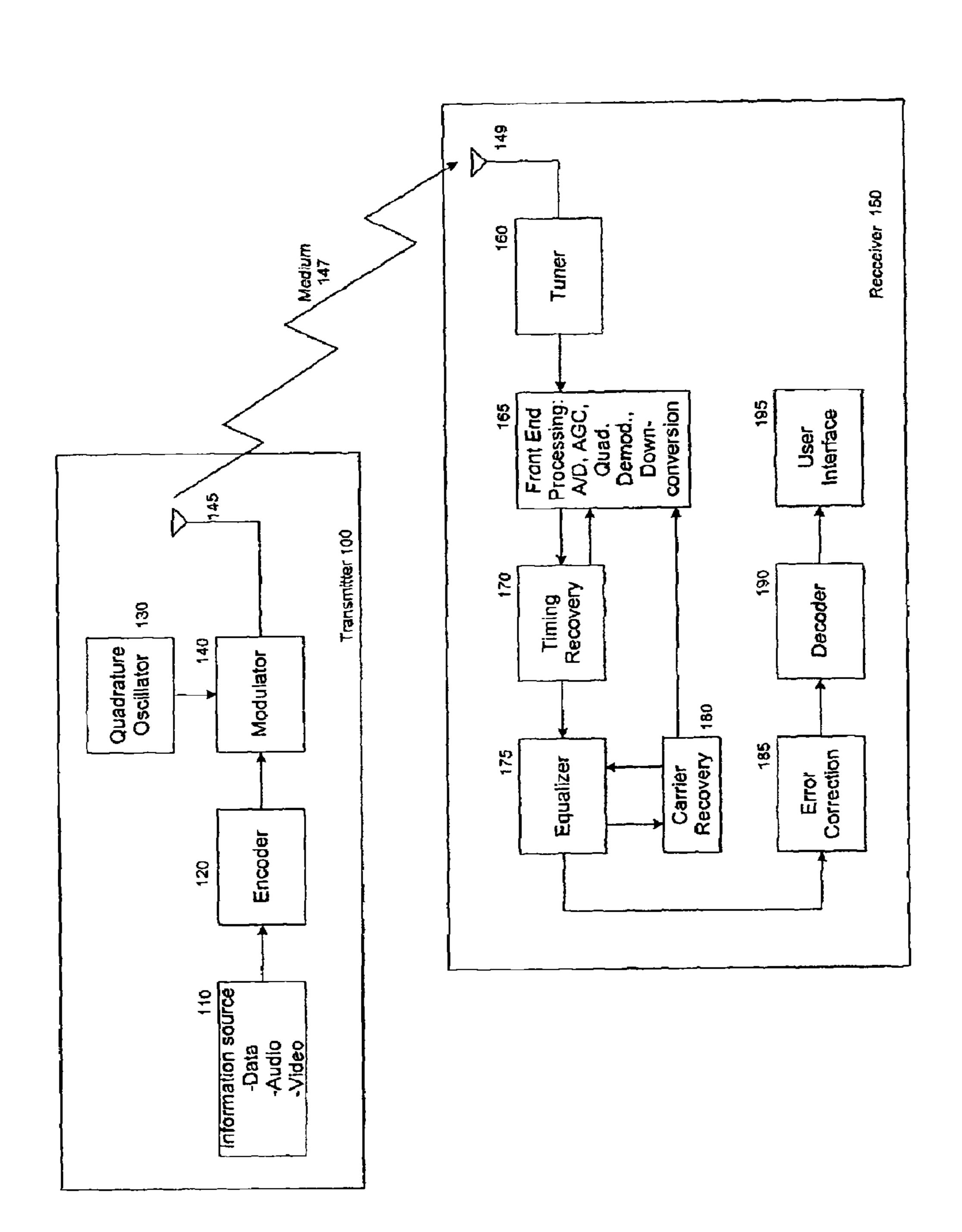
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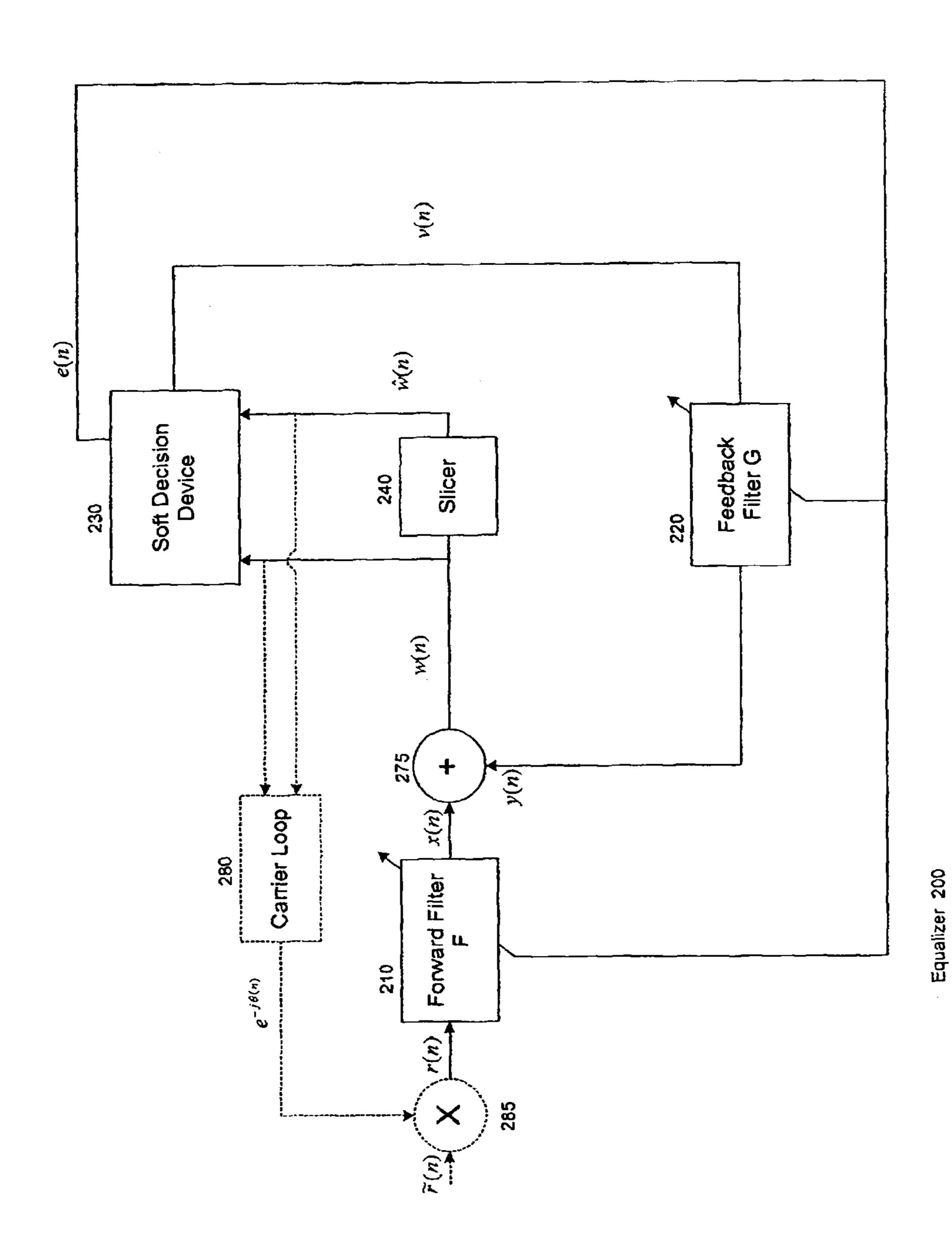
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self-initializing decision feedback equalizer

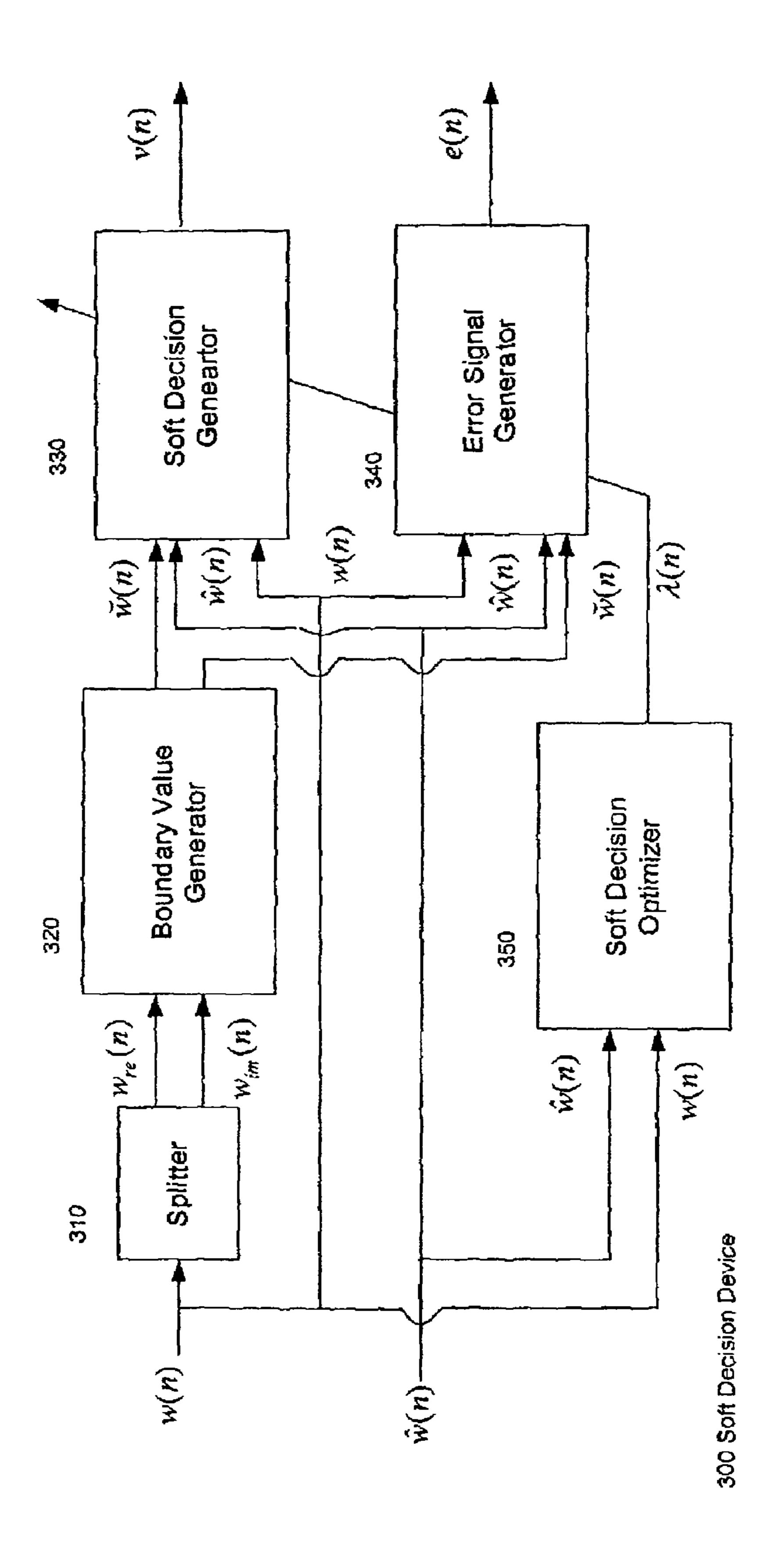
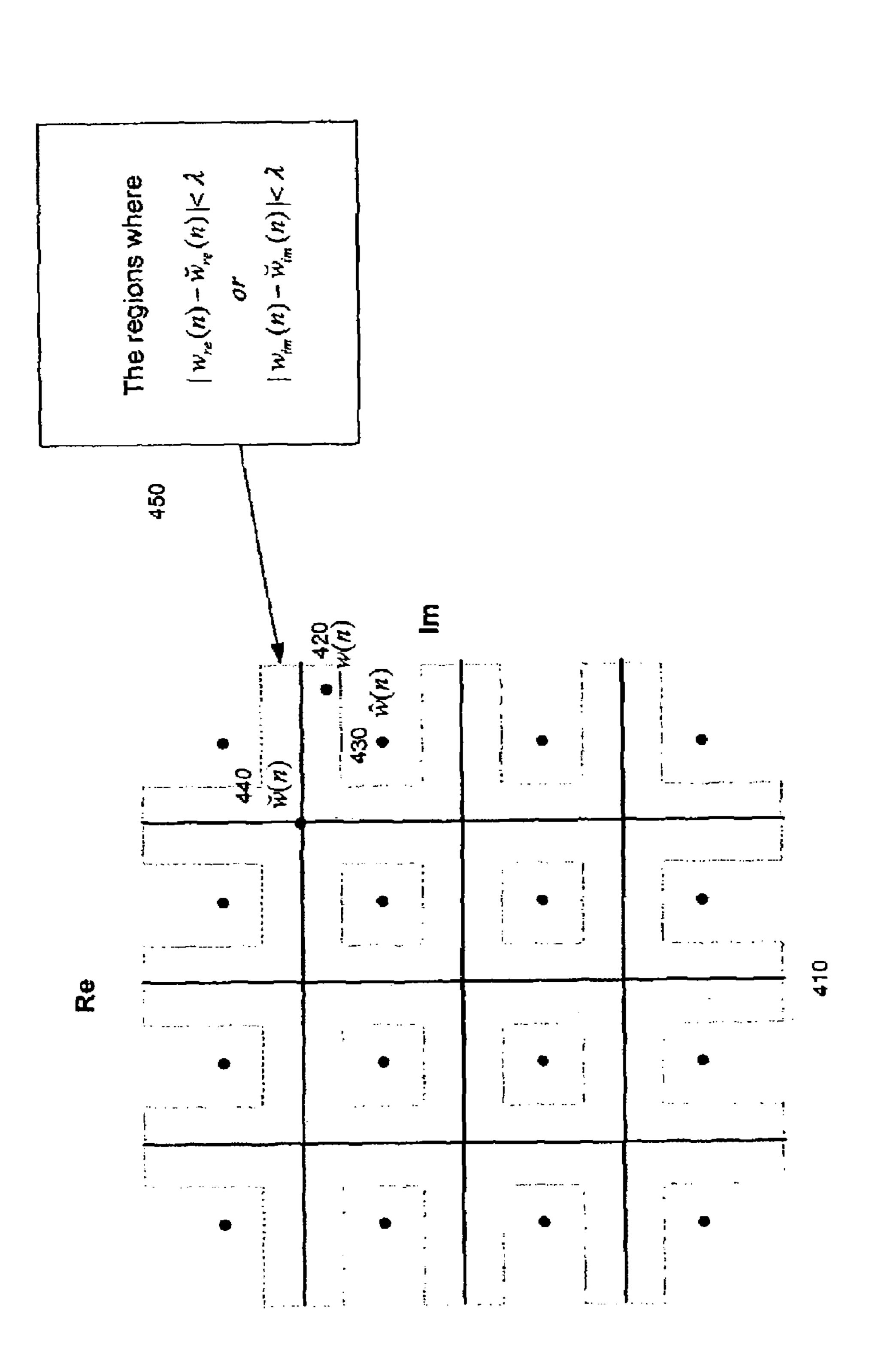
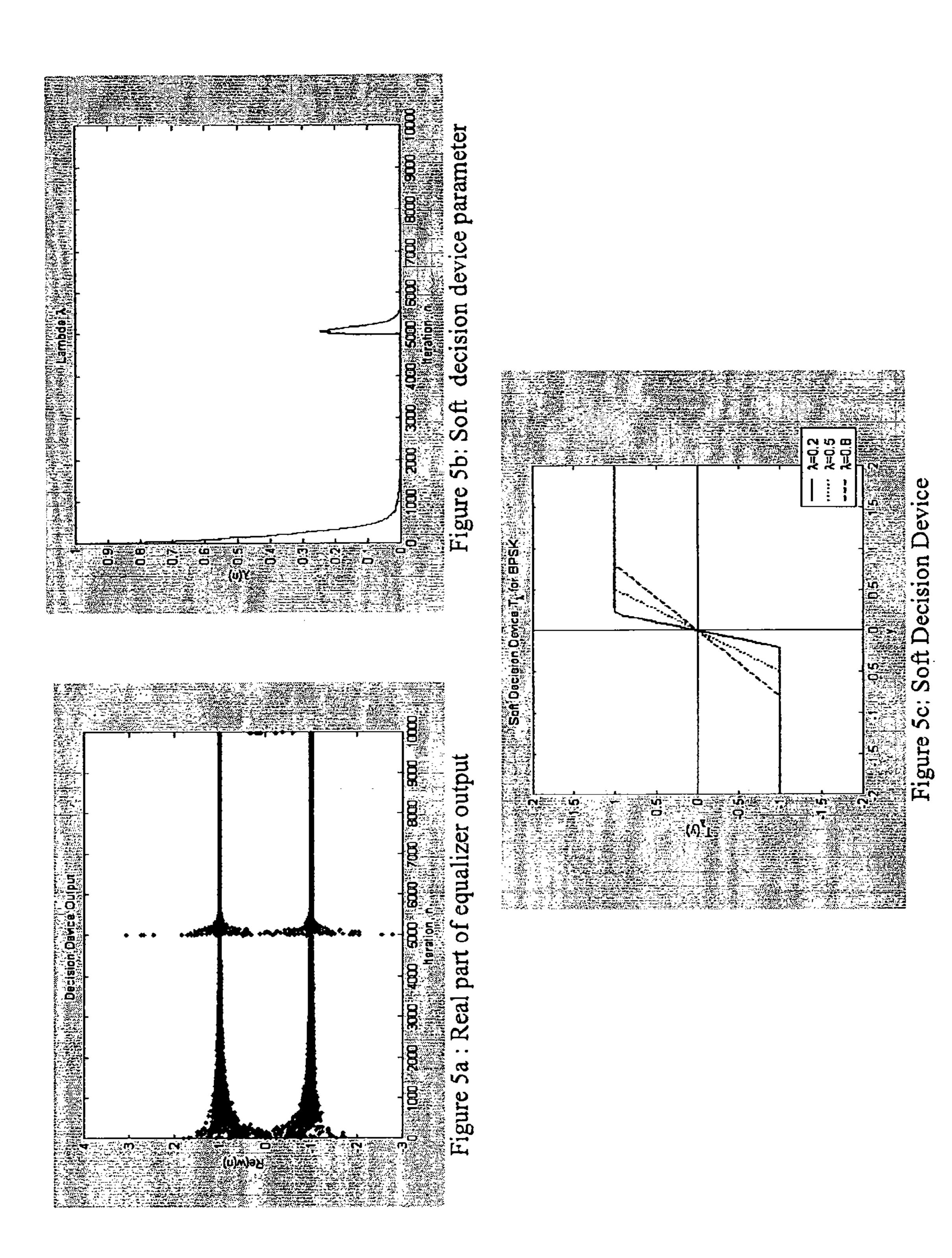


Figure 3: Block Diagram of Soft Decision Device





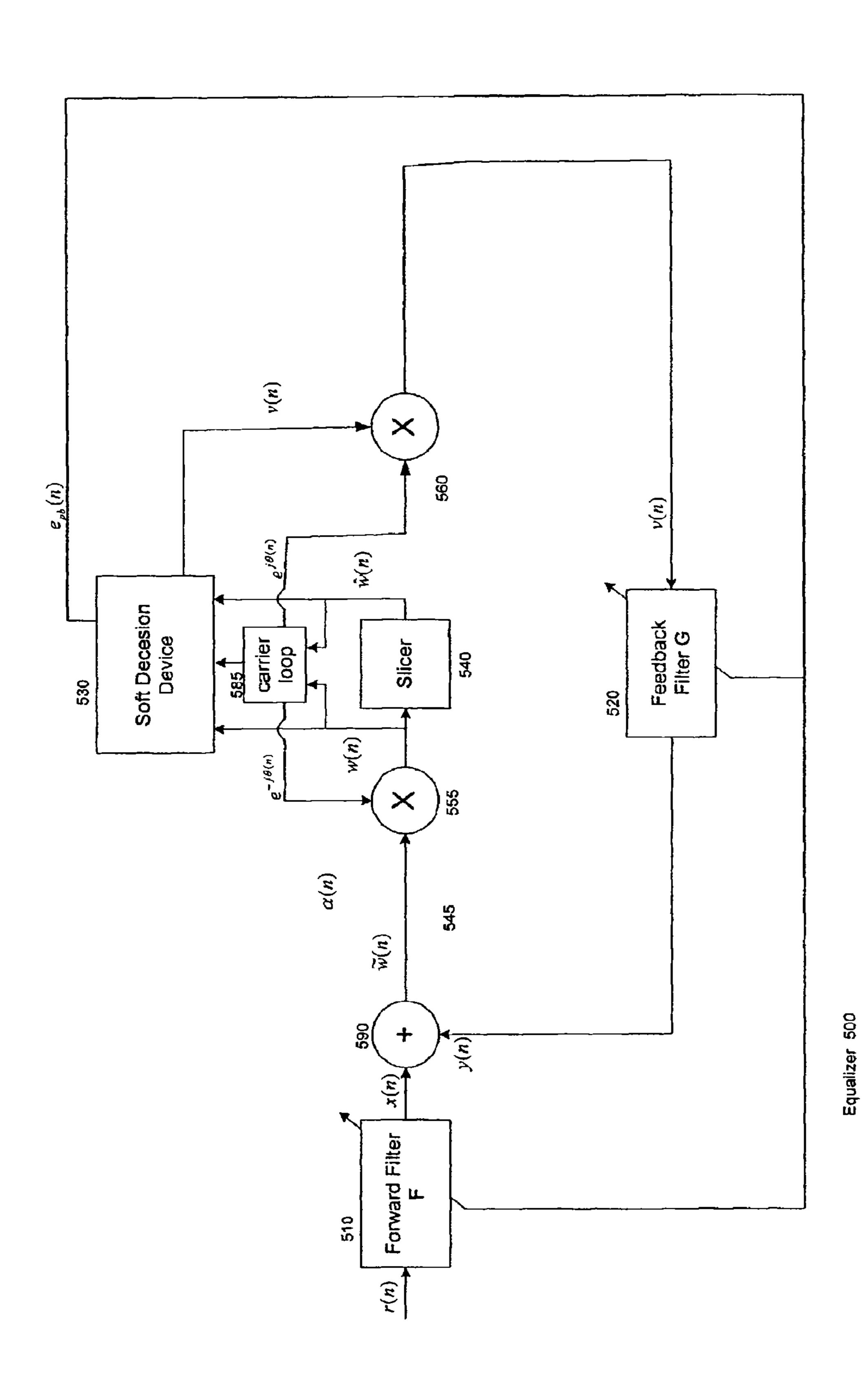
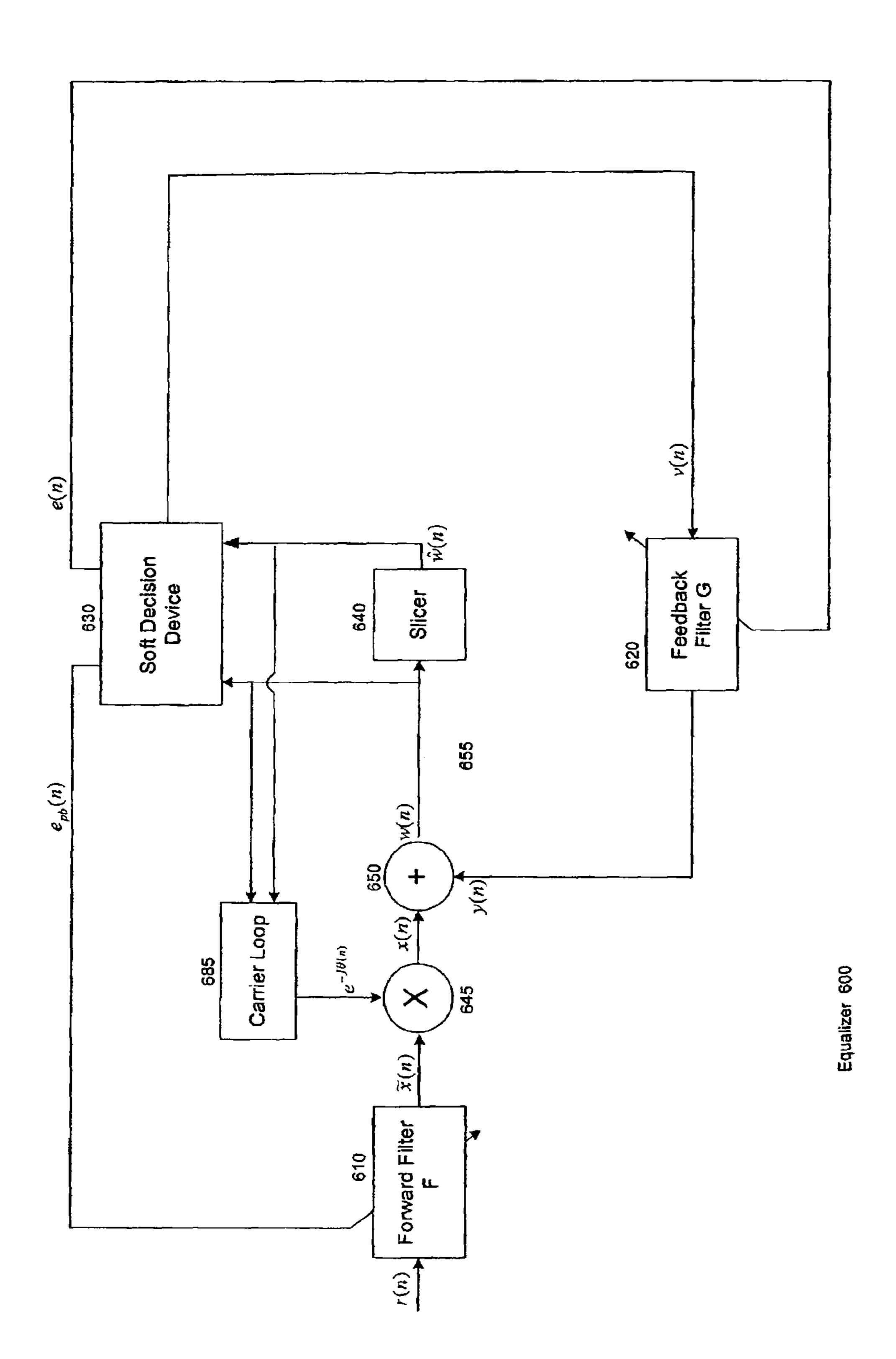


Figure 6: Alternative embodiment of invention showing equalizer forward and feedback filters operating



JOINT ADAPTIVE OPTIMIZATION OF SOFT DECISION DEVICE AND FEEDBACK EQUALIZER

Matter enclosed in heavy brackets [] appears in the original patent but forms no part of this reissue specification; matter printed in italics indicates the additions made by reissue.

[CONTINUATION IN PART] CROSS-REFERENCE TO RELATED APPLICATIONS

[This] This patent application is a reissue application for commonly assigned U.S. Pat. No. 7,180,942, issued on Feb. 15 20, 2007 from U.S. patent application Ser. No. 10/327,280, filed on Dec. 20, 2002, which is a continuation-in-part of that certain U.S. Ser. No. 10/322,299, filed Dec. 17, 2002 now abandoned, entitled "Self-Initializing Decision on Feedback Equalizer With Automatic Gain Control;" Endres, Long, 20 Cunningham and Ray, inventors, which relies on U.S. Ser. No. 60/341,931, filed Dec. 18, 2001 entitled "Self-Initializing Decision Feedback Equalizer With Automatic Gain Control." These documents are incorporated herein by this reference.

FIELD OF INVENTION

The present invention relates to adaptive optimization techniques for Decision Feedback Equalizers in order to compensate for distortions introduced in digital communications systems using modulation techniques such as Quadrature Amplitude Modulation (QAM) or Pulse Amplitude Modulation (PAM).

BACKGROUND

In digital communication systems, the digital information bits are mapped to symbols drawn from a finite set of discrete real or complex numbers. These symbols are used to modulate a radio frequency (RF) carrier's frequency, amplitude 40 and/or phase. For example, a quadrature oscillator can be used to modulate the complex symbols onto the amplitude and phase of the RF carrier, and the signaling is referred to as Quadrature Amplitude Modulation (QAM). The time interval between symbols is referred to as the symbol or baud interval, 45 and the inverse of this interval is referred to as the symbol or baud rate.

Most modem digital communication systems use a symbol rate that sends thousands or millions of symbols per second, over propagation media including satellite links through the 50 earth's atmosphere, terrestrial links from towers to fixed or mobile land-based receivers, or wired links using ancient twisted-pair copper connections or more sophisticated fiber optic connections. Such media are dispersive, causing fading and reflections that result in multiple path delays arriving at 55 the receiver. Such behavior is known as multipath, and causes symbols to smear across multiple symbol boundaries, which is referred to as inter-symbol interference (ISI). Moreover, mismatches in transmitter and receiver filtering induce ISI. Noise is added to the received signal from transmitter and 60 receiver component imperfections, and from sources through the propagation path. At the receiver, an equalizer is used to mitigate the effects of ISI and noise induced in the entire channel, including transmitter, propagation medium, and front-end receiver processing. Since the exact channel char- 65 acteristics are not known apriori at the receiver, the equalizer is usually implemented with adaptive methods.

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A common type of equalizer uses adaptive filters, and the adjustment of filter coefficients can be done in a variety of ways. Trained equalization methods rely on the embedding of a pre-determined sequence in the transmitted data, referred to as a training or reference sequence. The receiver stores or generates a replica of the training sequence, and to the extent that the received sequence differs from the training sequence, an error measure is derived to adjust equalizer coefficients. Usually, equalizer coefficient convergence relies on multiple transmissions of the training sequence, and the channel characteristics are also time varying. Hence, periodic re-training is necessary.

A common method of trained coefficient adaptation uses the Least Mean Squares (LMS) algorithm, which minimizes a Mean Squared Error (MSE) cost function with a stochastic gradient descent update rule as described in a paper entitled "The complex LMS algorithm," by Widrow, McCool, and Ball, in The Proceedings of the IEEE, vol. 63, no. 4, pp. to 719-720, April 1975.

Unfortunately, the training sequence needed for LMS takes up valuable bandwidth that could be used for data transmissions. Hence, methods that do not rely on a reference signal, or derive a reference signal from the data itself, are desirable. Such methods are referred to as blind equalization methods. A 25 common blind equalization method replaces the reference signal in the LMS algorithm with the receiver's best guess at the data, and is therefore referred to as Decision Directed LMS (DD-LMS), as proposed in a paper entitled "Techniques" for adaptive equalization of digital communication systems," by R. W. Lucky, in the Bell Systems Technical Journal, vol. 45, no. 2, pp. 255-286, February 1966. Unfortunately, DD-LMS needs a reasonably low percentage of incorrect decisions to prevent algorithm divergence, and is therefore impractical from a cold-start initialization. Other blind algo-35 rithms are usually used from a cold-start.

The Constant Modulus Algorithm (CMA), proposed independently by Godard and Treichler ("Self-recovering equalization and carrier tracking in two-dimensional data communication systems," by. D. N. Godard, in IEEE Transactions on Communications, vol. 28, no. 11, pp. 1867-1875, October 1980, and "A new approach to multipath correction of constant modulus signals," by J. R. Treichler, and B. G. Agee, in IEEE Transactions on Acoustics, Speech, and Signal Processing, vol. ASSP-31, no. 2, pp. 459-472, April 1983) has rapidly become the most popular blind equalization algorithm in practice, and is well-studied in the archival literature, due to its robustness to realistic signaling environments and LMSlike computational complexity and asymptotic performance. Instead of minimizing a MSE cost function, CMA minimizes a quartic Constant Modulus (CM) cost function that penalizes dispersion at the equalizer output.

Though both LMS and CMA were originally introduced using a linear transversal, or finite impulse response (FIR) equalizer structure, a Decision Feedback Equalizer (DFE) is generally believed to provide superior ISI cancellation with less noise gain than an FIR equalizer structure. A DFE acts to additively cancel ISI by subtracting filtered decisions (or best guesses, also known as hard decisions) from the sampled received signals. The feedback structure embeds a FIR filter in a feedback loop, fed by symbol estimates, and therefore has infinite impulse response (IIR). Like the DD-LMS algortihm, the DFE architecture requires a low percentage of incorrect decisions to prevent algorithm divergence and error propagation, a phenomenon whereby an incorrect decision causes more incorrect decisions due to the recursive structure of the DFE. Therefore, a DFE requires alternative adaptive strategies from a cold-start. Several techniques based on adaptive

IIR filtering have been proposed as summarized in a chapter entitled "Current approaches to blind decision feedback equalization," by R. A. Casas et al., in the textbook, "Signal processing advances in wireless and mobile communications: trends in channel estimation and equalization," edited by G. Giannakis, et al., Prentice Hall, Upper Saddle River, N.J., 2000.

Though adaptive IIR filtering approach for blind DFE initialization can achieve successful cold start up, its performance is significantly less optimal than DD-LMS/DFE and mechanical switch from IIR adaptation to DD-LMS adaptation usually exhibits performance degradation in transient period, and thus, in dealing with time varying channels. In order to achieve better transition between IIR adaptation and DD-LMS/DFE Endres et. al in Provisional Application No. 60,341,931, filed Dec. 17, 2001 entitled "Self-initializing decision feedback equalizer with automatic gain control" proposed linearly combining IIR adaptation and DD-LMS adaptation of the DFE coefficients.

On the other hand, it has been recognized that DFE is not robust under severe noise environment due to error propagation rooted in its recursive structure. Recent studies such as in "Joint Coding and Decision Feedback Equalization for Broadband Wireless Channels," by Ariyavisitakul et at in ²⁵ IEEE Journals on Selected Areas in Comm. Vol. 16, No. 9, December 1998 proposed a soft decision device approach to reduce MSE of DFE output by replacing the hard decisions with cleverly estimated soft decisions.

The present invention combines the soft decision device approach and the seamless transition between IIR adaptation and DD-LMS adaptation. Unlike the linear combination of IIR and DD-LMS adaptations, this present invention uses a family of non-linear soft decision devices approximating the optimal soft decision device studied in soft-decision DFE 35 literatures. According to the selection rule inferred from the non-linear soft decision device, DFE coefficients are updated by selected error signals between IIR adaptation and DD-LMS adaptation on a symbol-by-symbol basis, which jointly optimizes the soft decision device and DFE adaptation.

SUMMARY

In accordance with the present invention, a Decision Feedback Equalizer (DFE) uses input samples to the feedback 45 filter that are generated from a novel adaptive soft decision device. The soft decision device receives the input and output samples of the slicer and generates a feedback sample based on a novel non-linear decision rule. Moreover, the soft decision device provides novel error terms used to adapt equalizer 50 coefficients.

BRIEF DESCRIPTION OF DRAWINGS

Other aspects, features, and advantages of the present 55 invention will become more fully apparent from the following detailed description, the appended claims, and the accompanying drawings in which:

FIG. 1 shows a typical prior art communication system that may be employed for transmission of digital signals;

FIG. 2 shows an exemplary embodiment of the present invention, showing a self-initializing decision feedback equalizer operating at precise baseband;

FIG. 3 describes the Soft Decision Device in the present invention;

FIG. 4 shows a 16-QAM constellation selection regions for Soft Decision Device in the present invention;

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FIG. 5a shows the in-phase component of the equalizer output from a computer simulation of the preferred embodiment of the present invention;

FIG. 5b shows the soft decision parameter $\lambda(n)$ trajectory from a computer simulation of the preferred embodiment of the present invention;

FIG. 5c illustrates the input-output relation of the Soft Decision Device for a given $\lambda(n)$ and constellation;

FIG. **6** shows an alternative embodiment of the present invention, with equalizer forward and feedback filters operating on passband samples; and

FIG. 7 shows an alternative embodiment of the present invention, with equalizer forward filter operating on passband samples, and equalizer feedback filter operating on baseband samples.

DETAILED DESCRIPTION

FIG. 1 depicts a typical prior art digital communication 20 system. Transmitter station 100 is coupled to receiver 150 by propagation medium 147. The propagation medium could be a cable, telephone twisted-pair wire, satellite link, terrestrial link, or fiber optic connection, for example. Transmitter station 100 includes an information source 110, that contains the content such as data, audio, or video, which is to be communicated to the receiver 150. The information source 110 is coupled to encoder 120, which formats the information in a manner suitable for digital communication, typically in accordance with a given standard or protocol. The encoder 120 is coupled to modulator 140, which is also coupled to a quadrature oscillator 130. The modulator 140 uses the signal from the quadrature oscillator 130 to modulate the encoded information provided by encoder 120 onto a suitable Radio Frequency (RF) carrier frequency in amplitude and phase. The modulated signal from modulator 140 is coupled to transmit antenna 145 for transmission into propagation medium **147**.

The receiver 150 receives the RF signal from propagation medium 147 via receiver antenna 149. Receiver antenna 149 40 is coupled to tuner **160**. Tuner **160** is set to receive the RF signal in the desired frequency range, while rejecting signals in nearby or adjacent frequency ranges. Tuner 160 may provide automatic gain control at the RF frequency and also downconvert the received signal to an intermediate frequency (IF) before passing the signal to the Front End Processing block 165. Front End Processing block 165 samples the signal with an analog-to-digital converter and contains an automatic gain control circuit that scales the signal to the proper dynamic range in accordance with the analog-to-digital converter. Front End Processing block 165 may further include a digital downconversion in frequency, and performs a quadrature demodulation to split the signal into in-phase (I) and quadrature-phase (Q) samples. Front End Processing block 165 is coupled to Timing Recovery module 170 that determines a correct sampling phase. Timing Recovery module 170 may adjust the sampling phase by interpolating the data samples, or adjusting the phase and sampling frequency of the analog-to-digital converter in Front End Processing block 165. Timing Recovery module 170 is coupled to Equalizer 175, which is used to mitigate the distortions, such as intersymbol interference and noise, that are introduced by the propagation medium 147, transmitter 100, receiver Tuner 160, receiver Front End Processing block 165, and receiver Timing Recovery module 170. Equalizer 175 is coupled to 65 Carrier Recovery module 180, which detects residual offset in frequency and phase. The detected carrier offset in Carrier Recovery module may be supplied back to the Equalizer 175

for translation of equalized samples to precise baseband, or used to adjust the downconversion process in Front End Processing block **165**, or both. The output of Equalizer **175** is coupled to Error Correction module **185**, which detects and corrects bit errors in the recovered bit stream. The Error Correction module **185** is coupled to Decoder **190**, which decodes the bit stream in accordance with the standard or protocol used in the Encoder **120** of Transmitter **100**. The decoded bits from Decoder **190** represent the recovered information source, consisting of data, audio, or video, and are supplied to a user interface **195**. The present invention is embodied in the Equalizer **175** portion of the communication system.

Baseband/Baseband Equalization

FIG. 2 shows an exemplary embodiment of the present invention. An Equalizer 200 receives complex data $\tilde{r}(n)$ that is input to mixer 285. The mixer 285 also receives a signal from carrier recovery loop **280**, $e^{-j\Theta(n)}$, that is an estimate of the ²⁰ conjugate of the carrier offset. Methods of carrier recovery are well known to one skilled in the art, and may be found, for example, in chapter 16 of the text "Digital Communication" by E. A. Lee and D. G. Messerschmitt, Kluwer Academic Publishers, 1994, which is incorporated herein by reference. ²⁵ The carrier recovery loop 280 and mixer 285 are shown as dashed lines, to represent that translation to precise baseband is done prior to equalization, and may be done anywhere prior to equalization in the signal processing chain. For example, some systems embed pilot tones or pulses to aid synchroni- ³⁰ zation, allowing translation to precise baseband in the receiver front end, prior to equalization. In this exemplary embodiment of the invention, the equalizer 200 operates on samples that have been translated to precise baseband.

The output of mixer **285** is a received signal, r(n), that is at precise baseband, and is input to forward filter **210**. Forward filter **210** may operate at the baud rate or faster, in which case the equalizer is said to be fractionally-spaced, and exploits temporal diversity. Also, the forward filter **210** may receive multiple inputs, as from multiple antennae, to exploit spatial diversity. Temporal or spatial diversity uses a multi-channel forward filter. For simplicity, however, a single forward filter **210** is shown, and extension to a multi-channel model is understood by one skilled in the art.

Filtering

Forward filter **210** is a finite impulse response (FIR) filter, computing its output according to the convolution sum

$$\mathbf{x}(\mathbf{n}) \!\!=\!\! \mathbf{f}_0(\mathbf{n}) \mathbf{r}(\mathbf{n}) \!\!+\!\! \mathbf{f}_1(\mathbf{n}) \mathbf{r}(\mathbf{n} \!\!-\!\! 1) \!\!+\!\! \mathbf{f}_2(\mathbf{n}) \mathbf{r}(\mathbf{n} \!\!-\!\! 2) \!\!+\!\! \ldots +\!\! \mathbf{f}_{L_f \!\!-\!\! I}\!(\mathbf{n}) \mathbf{r}$$

where r(n) is the sample sequence input to forward filter 210, x(n) is the output sample sequence of forward filter 210, f_i are the forward filter coefficients (or parameters,) and L_f is the number of forward filter coefficients. Note that the forward filter coefficients are also shown with time index n to indicate that the forward filter 210 is adaptive.

The feedback filter 220 is not multi-channel, and is a FIR filter that calculates its output according to the convolution sum

$$y(n)=g_0(n)v(n)+g_1(n)v(n-1)+g_2(n)v(n-2)+...+g_{L_{\sigma}}^{-I}$$

where v(n) is the sample sequence input to feedback filter 220, y(n) is the output sample sequence of feedback filter 220, g_i are the feedback filter coefficients (or parameters,) and L_g is the number of feedback filter coefficients. Note that the 65 feedback filter coefficients are also shown with time index n to indicate that the feedback filter 220 is adaptive. Though the

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feedback filter **220** is a FIR filter, it is embedded in a feedback loop, so that the equalizer has an overall impulse response that is infinite.

Adder 275 combines the outputs of forward filter 210 and feedback filter 220, x(n) and y(n), respectively, to form sample sequence w(n). Sample sequence w(n) is referred to as slicer inputs. The slicer inputs, w(n), are input to slicer 240. Slicer 240 is a nearest-element decision device that outputs a hard decision, $\hat{w}(n)$, corresponding to the source alphabet member with closest Euclidean distance to its input sample. The slicer input w(n) and the hard decisions, $\hat{w}(n)$, from slicer 240 are input to the Soft Decision Device 230.

Soft Decision Device

FIG. 3 describes the Soft Decision Device in accordance with the present invention. The slicer input w(n) is splitted into real and imaginary components. For the real and imaginary parts of w(n), $w_{re}(n)$ and $w_{im}(n)$ respectively, the Boundary Value Generator 320 produces the nearest decision boundary values $\check{w}_{re}(n)$ and $\check{w}_{im}(n)$ by treating $w_{re}(n)$ and $w_{im}(n)$ as a Pulse Amplitude Modulated (PAM) signals, which belong to a alphabet set

$$\{-(2M-1)\Gamma, \ldots, -3\Gamma, -\Gamma, 3\Gamma, \ldots (2M-1)\Gamma\}$$

where the constellation unit Γ and PAM level M are determined from the QAM level.

$$\widetilde{\mathbf{w}} = \underset{2k\Gamma}{\operatorname{argmin}} |\mathbf{w} - 2k\Gamma|,$$

for
$$k=-M+1, ..., M-1$$
.

with |·| denoting absolute value, or magnitude. Remind that the hard decision of a PAM signal is defined by

$$\hat{\mathbf{w}} = \underset{(2k-1)\Gamma}{\operatorname{argmin}} |\mathbf{w} - (2k-1)\Gamma|,$$

for k=-M+1, ..., M-1.

FIG. 4 illustrates the relation among w(n) (420), $\hat{\mathbf{w}}$ (n) (430), $\hat{\mathbf{w}}_{re}$ (n) (440), and $\hat{\mathbf{w}}_{im}$ (n) (440) for a 16-QAM constellation.

In FIG. 3 the Soft Decision Generator 330 generates the soft decision based on the comparison between the distance between the nearest boundary values from the slicer input, $|\mathbf{w}_{re}(\mathbf{n}) - \check{\mathbf{w}}_{re}(\mathbf{n})|$ and $|\mathbf{w}_{im}(\mathbf{n}) - \check{\mathbf{w}}_{im}(\mathbf{n})|$, and a decision reference parameter $\lambda(\mathbf{n})$, according to

$$\begin{cases}
\frac{\mathbf{w}(\mathbf{n}) - \mathbf{w}(\mathbf{n})}{\lambda(\mathbf{n})} & \text{if } \left| \mathbf{w}_{re}(\mathbf{n}) - \mathbf{w}_{re}(\mathbf{n}) \right| < \lambda(\mathbf{n}) \text{ or } \left| \mathbf{w}_{im}(\mathbf{n}) - \mathbf{w}_{im}(\mathbf{n}) \right| < \lambda(\mathbf{n})
\end{cases}$$

60 where $\check{\mathbf{w}}(\mathbf{n}) = \check{\mathbf{w}}_{re} + \mathbf{j} \check{\mathbf{w}}_{im}$.

v(n) =

The soft decision device is made adaptive by adaptation of the decision reference parameter $\lambda(n)$. The decision reference parameter $\lambda(n)$ is initialized by $\lambda(0)=1$ and adjusted from 0 to 1 depending on the signal quality. The Soft Decision Optimizer **350** optimizes the decision reference parameter $\lambda(n)$. The decision reference parameter $\lambda(n)$ can be approximately optimized by setting $\lambda(n)=E|w(n)-\hat{w}(n)|^2/E|w(n)|^2$ with $E\{\cdot\}$

$$\lambda(n) = (1 - \rho_{\lambda}) \cdot \lambda(n-1) + \rho_{\lambda} \cdot |w(n) - \hat{w}|^2 / \Delta$$

where Δ is chosen to normalize $|w(n)-\hat{w}|^2$ (for example average signal power, $\Delta = E|w(n)|^2$) and ρ_{λ} is the leakage term and is chosen less than or equal to one and greater than or equal to zero.

Alternatively, $\lambda(n)$ can be updated on a block by block base based on the block estimation of $E|w(n)-\hat{w}(n)|^2/E|w(n)|^2$, or 10 using training signals instead of $\hat{w}(n)$ for the training periods. Furthermore, the combining weight $\lambda(n)$ may be compared to two thresholds, T_U and T_L . If $\lambda(n) > T_U$, then $\lambda(n)$ is set to one; if $\lambda(n) < T_L$, then $\lambda(n)$ is set to zero

Error Signal Generation and Coefficient Adaptation

Adaptation of the forward filter **210** coefficients and feedback filter **220** coefficients uses a stochastic gradient descent update rule:

$$f_i(n+1)=f_i(n)-\mu_f\Phi^*(n)e(n)$$

$$g_i(n+1)=g_i(n)-\mu_g \phi^*(n)e(n)$$

where $(\cdot)^*$ represents complex conjugation, and μ_f and μ_g are small, positive stepsizes governing algorithm convergence rate, tracking capabilities and stochastic jitter. Using simplified updates, the data used in the adaptation equations are set to $\Phi(n)$ =r(n) and $\phi(n)$ =v(n). The baseband error term e(n) that updates the forward filter 210 and feedback filter 220 at each 30 baud instance is selected by Error Signal Generator 340 in Soft Decision Device 300 and is calculated according to

$$e(n) = \begin{cases} e_1(n) & \text{if } \left| \mathbf{w}_{re}(n) - \widetilde{\mathbf{w}}_{re}(n) \right| < \lambda(n) \text{ or } \left| \mathbf{w}_{im}(n) - \widetilde{\mathbf{w}}_{im}(n) \right| < \lambda(n) \\ e_2(n) & \text{else} \end{cases}$$

The preferred embodiment of the present invention uses a Constant Modulus Algorithm (CMA) error term of order p=2 40 (as described by Godard in "Self recovering equalization and carrier tracking in two-dimensional data communication systems") for $e_1(n)$ and a Decision-Directed LMS (DD-LMS) error term for $e_2(n)$. For example, CMA ad DD-LMS error terms may be calculated according to

$$e_{cma} = \left(\frac{\mathbf{w}(\mathbf{n}) - \mathbf{\tilde{w}}(\mathbf{n})}{\lambda(\mathbf{n})} + \mathbf{\tilde{w}}(\mathbf{n})\right) \cdot \left(\left|\frac{\mathbf{w}(\mathbf{n}) - \mathbf{\tilde{w}}(\mathbf{n})}{\lambda(\mathbf{n})} + \mathbf{\tilde{w}}(\mathbf{n})\right|^2 - \gamma\right)$$

$$\mathbf{e}_{\textit{did-lms}} \!\!=\!\! \mathbf{w}(\mathbf{n}) \!\!-\! \hat{\mathbf{w}}(\mathbf{n})$$

where γ is a real scalar referred to as the CM dispersion constant or Godard radius, and is usually calculated as $\gamma = E\{|s| 55|(n)|^4\}/E\{|s(n)|^2\}$ for source sequence s(n), (These error terms are said to be baseband, since they are derived from samples at precise baseband.)

The intuition behind this error term generation is that the slicer inputs near hard decision boundaries are treated less 60 reliable signals than the slicer inputs near hard decision samples. The Error Signal Generator **340** separates the unreliable signals and reliable signals, and apply IIR adaptation for the unreliable signals after proper resealing. For the reliable signals the conventional DD-LMS is applied.

Other choices of error terms may include CMA error terms of order other than p=2; those derived from the Bussgang

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class of cost functions, as described in chapter 2 of "Blind Deconvolution," Prentice Hall, written by S. Bellini, edited by S. Haykin, 1994; single-axis error terms which use real-part extraction, as described in a paper by A. Shah et al, entitled "Global convergence of a single-axis constant modulus algorithm," Proceedings of the IEEE statistical signal and array processing workshop, Pocono Manor, Pa., August, 2000; or error terms derived from other blind or non-blind criteria.

Setting Φ(n)=r(n) and φ(n)=v(n) in the above equations used to adapt forward filter **210** and feedback filter **220** coefficients is referred to as "simplified updates," since the step known as regressor filtering is omitted. True cost function minimization requires an extra stage of filtering for the regressor data of the forward filter **210** and the feedback filter **220** in the adaptation process, using the current equalizer coefficients. Such regressor filtering is typically omitted in practice due to implementation burden. Regressor filtering is described in Chapter 5 of "Theory and design of adaptive filters" by J. R. Treichler, C. R. Johnson, Jr., and M. G. Larimore, Prentice Hall, 2001. One skilled in the art would recognize how to modify the regressor data used in the adaptation equations above to incorporate the extra stage of regressor filtering.

FIGS. 5a and 5b illustrate the equalizer output and soft decision reference parameter $\lambda(n)$ in operation from a computer simulation of the preferred embodiment of the present invention. The source signal is 4-QAM (QPSK) data passed through a closed-eye channel that has rapid time variation at the 5,000th baud sample. There are 10,000 baud samples, with adaptation of equalizer coefficients and decision reference parameter at the start of the simulation. The leakage value for Soft Decision Device optimization is ρ_{λ} =0.01. Thresholds for the combining weight are set to T_{L} =1 and T_{L} =0.

FIG. 5a shows the real part of slicer inputs converging to correct decisions as adaptation is processed. Sudden dispersion at the 5,000th baud sample is due to sudden change of the multipath channel.

FIG. 5b shows the trajectory of decision reference parameter $\lambda(n)$, initialized to unity, and converging towards zero when channel is static, and optimizing the adaptation and soft decision device when channel is varying.

FIG. 5c draws the soft decision device as a function of slicer input for various choice of decision reference parameter $\lambda(n)$ in this simulation. For $\lambda(n)=0$ the soft decision device agrees with hard limiter and DFE is operating with DD-LMS algorithm. As $\lambda(n)$ increases the region of unreliable signals are increased too and DFE is operating with the conventional CMA in that region.

Passband/Passband Equalization

An alternative embodiment of the present invention is shown in FIG. 5, in which the equalizer 500 operates in the passband; that is, not at precise baseband. Equalizer 500 is similar to equalizer 200 in FIG. 2, so only the differences in equalizer 500 of FIG. 5 are described.

Forward filter **510** and feedback filter **520** produce data by convolution sums in an analogous manner to that described for the exemplary embodiment in FIG. **2**, yielding passband signals x(n) and y(n), respectively. The outputs of forward filter **510** and feedback filter **520** are combined in adder **590**, yielding the passband sample $\tilde{w}(n)$. This sample is translated to precise baseband (or de-rotated) slicer input w(n) in multiplier **555** by multiplication with the conjugate of the carrier offset, $e^{-j\Theta(n)}$, provided by carrier recovery loop **585**. The slicer **540** is a nearest-element decision device that outputs a

hard decision, $\hat{\mathbf{w}}(\mathbf{n})$, corresponding to the source alphabet member with closest Euclidean distance to its input sample. The slicer input and hard decision samples are input to the Soft Decision Device and the soft decision $\mathbf{v}(\mathbf{n})$ is translated back to the passband in multiplier **560** by multiplication with the carrier offset $e^{i\theta(n)}$, provided by the carrier recovery loop **585**.

Though soft decision is made actually in baseband, equalizer adaptation must use an error term that is in the passband. The translation rules between passband and baseband error terms are given by:

$$\mathbf{e}_{dd-lms}^{passband} = \mathbf{e}_{dd-lms} \cdot e^{\mathbf{j}\theta(n)}$$

 $\mathbf{e}_{CMA}^{passband} = \mathbf{e}_{CMA} \cdot e^{\mathbf{j}\theta(n)}$

Since both forward filter **510** and feedback filter **520** operate in the passband, they are updated with passband error 20 terms.

Passband/Baseband Equalization

FIG. 6 shows equalizer 600, an alternative embodiment of 25 the present invention, in which the forward filter 610 operates on passband data, while the feedback filter 650, and all processing after multiplier 645, operate at precise baseband. Forward filter 610 operates on received passband data r(n) and calculates output $x_{pb}(n)$ via the convolution sum discussed for the filtering process of equalizer 200 in FIG. 2.

Multiplier **645** translates the output of forward filter **610** to precise baseband by multiplication with the conjugate of the carrier offset estimate, $e^{-j\Theta(n)}$, provided by carrier recovery loop **685**. The remainder of the equalizer **600** operates analogously to the equalizer **200** in FIG. **2**, except that the equalizer control module **630** receives also the carrier offset estimate from carrier recovery loop **685** to produce a passband error term, $e_{pb}(n)$, as well as a baseband error term, e(n). Feedback filter **620** operates on baseband data, and thus is adapted with the baseband error terms described for operation of equalizer **200** in FIG. **2**. However, since forward filter **610** in FIG. **6** processes passband data, it is adapted by passband error terms that are generated by rotating the baseband error term with the 45 current offset of the carrier recovery estimate, $e^{j\Theta(n)}$.

One skilled in the art would understand that the equations described herein may include scaling, change of sign, or similar constant modifications that are not shown for simplicity. One skilled in the art would realize that such modifications can be readily determined or derived for the particular implementation. Thus, the described equations may be subject to such modifications, and are not limited to the exact forms presented herein.

The present invention has been described using Quadrature 55 Amplitude Modulation (QAM) signals with complex signal processing, unless specifically noted. However, one skilled in the art would realize that the techniques described herein may be applied to a receiver processing Phase-Shift Keyed (PSK), Pulse Amplitude Modulation (PAM), or other signals.

As would be apparent to one skilled in the art, the various functions of equalization, signal combining, and automatic gain control may be implemented with circuit elements or may also be implemented in the digital domain as processing steps in a software program. Such software may be employed 65 in, for example, a digital signal processor, microcontroller, or general-purpose computer.

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The present invention can be embodied in the form of methods and apparatuses for practicing those methods. The present invention can also be embodied in the form of program code embodied in tangible media, such as floppy diskettes, CD-ROMs, hard drives, or any other machine-readable storage medium, wherein, when the program code is loaded into and executed by a machine, such as a computer, the machine becomes an apparatus for practicing the invention. The present invention can also be embodied in the form of program code, for example, whether stored in a storage medium, loaded into and/or executed by a machine, or transmitted over some transmission medium, such as over electrical wiring or cabling, through fiber optics, or via electromagnetic radiation, wherein, when the program code is loaded into and executed by a machine, such as a computer, the machine becomes an apparatus for practicing the invention. When implemented on a general-purpose processor, the program code segments combine with the processor to provide a unique device that operates analogously to specific logic circuits.

It will be further understood that various changes in the details, materials, and arrangements of the parts which have been described and illustrated in order to explain the nature of this invention may be made by those skilled in the art without departing from the principle and scope of the invention as expressed in the following claims.

What is claimed is:

- 1. A method for operating forward and feedback filters in a communications receiver having a decision feedback equalizer, said communications receiver having a decision feedback equalizer, said communications receiver responsive to a received signal to form slicer input samples and hard decision samples corresponding to said slicer output samples, said method comprising:
 - non-linearly combining said slicer input samples and said hard decision samples to form a soft decision samples in a soft decision device; and
 - the said soft decision device being adaptively adjusted to control contributions of said slicer input samples and said hard decision samples to form said soft decision samples; and
 - said soft decision device generating error signals to adjust said forward and feedback filters; and
 - operating said forward and feedback filters by coupling a composite decision samples to said feedback filter and by adapting said forward and feedback filters with said error signals.
- 2. The method of claim 1, wherein said decision feedback equalizer operates in passband.
- 3. The method of claim 1, wherein said feedback filter operates in baseband.
- 4. A receiver having a decision feedback equalizer, said receiver responsive to a received signal to form slicer input samples and hard decision samples corresponding to said slicer output samples, said receiver comprising:
 - a forward filter;
 - a feedback filter;
 - a slicer that is capable of generating the slicer output samples; and
 - a soft decision device that is capable of non-linearly combining said slicer input samples and said hard decision samples to form soft decision samples, said soft decision device further being adaptively adjusted to control contributions of said slicer input samples and said hard decision samples to form said soft decision samples,

further wherein said soft decision device is capable of generating error signals to adjust said forward and feedback filters;

wherein said forward and feedback filters are capable of coupling a composite decision samples to said feedback 5 filter and by adapting said forward and feedback filters with said error signals.

- 5. The receiver of claim 4, wherein said decision feedback equalizer operates in passband.
- 6. The receiver of claim 4, wherein said feedback filter 10 operates in baseband.

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- 7. The receiver of claim 5, wherein said forward filter and said feedback filter operate in the passband.
- 8. The receiver of claim 6, wherein said forward filter operates in passband.
- 9. The receiver of claim 4 wherein said forward filter has a plurality of coefficients that are updated using a stochastic gradient descent rule.

* * * *

UNITED STATES PATENT AND TRADEMARK OFFICE

CERTIFICATE OF CORRECTION

PATENT NO. : RE42,558 E Page 1 of 2

APPLICATION NO. : 12/390368

DATED : July 19, 2011

INVENTOR(S) : Chung et al.

It is certified that error appears in the above-identified patent and that said Letters Patent is hereby corrected as shown below:

Title Page 3, item (56), under "Other Publications", in Column 1, Line 43, delete "pages" and insert -- pages, --.

Title Page 3, item (56), under "Other Publications", in Column 2, Line 3, delete "Vestigal" and insert -- Vestigial --.

Title Page 3, item (56), under "Other Publications", in Column 2, Line 5, delete "Vestigal" and insert -- Vestigial --.

Title Page 3, item (56), under "Other Publications", in Column 2, Line 17, delete "McGaw-Hill." and insert -- McGraw-Hill. --.

Title Page 3, item (56), under "Other Publications", in Column 2, Line 32, delete "Transactins" and insert -- Transactions --.

Title Page 3, item (56), under "Other Publications", in Column 2, Line 43, delete "Embeddings" and insert -- Embedding --.

Title Page 3, item (56), under "Other Publications", in Column 2, Line 45, delete "television" and insert -- Television ---.

Title Page 3, item (56), under "Other Publications", in Column 2, Line 59, delete "Adverstisement" and insert -- Advertisement --.

Title Page 3, item (56), under "Other Publications", in Column 2, Line 61, delete "Adverstisement" and insert -- Advertisement --.

Title Page 3, item (56), under "Other Publications", in Column 2, Line 68, delete "entitle" and insert -- entitled --.

Signed and Sealed this Tenth Day of January, 2012

David J. Kappos

Director of the United States Patent and Trademark Office

CERTIFICATE OF CORRECTION (continued)

U.S. Pat. No. RE42,558 E

Title Page 4, item (56), under "Other Publications", in Column 1, Line 14, delete "Vestigal" and insert -- Vestigial --.

Title Page 4, item (56), under "Other Publications", in Column 1, Line 16, delete "Vestigal Sidebank" and insert -- Vestigial Sideband ---.

Title Page 4, item (56), under "Other Publications", in Column 2, Line 6, delete "Rhyme," and insert -- Rhyne, --.

Title Page 4, item (56), under "Other Publications", in Column 2, Line 15, delete "Printice" and insert -- Prentice --.