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Seyama

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(54) **COMMUNICATION APPARATUS AND COMMUNICATION METHOD**

(75) Inventor: **Takashi Seyama**, Kawasaki (JP)

(73) Assignee: **Fujitsu Limited**, Kawasaki (JP)

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(51) **Int. Cl.**

H04B 7/02 (2006.01)

H04L 1/02 (2006.01)

(52) **U.S. Cl.** **375/267**; 375/260

(58) **Field of Classification Search** 375/267
See application file for complete search history.

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Primary Examiner — David C. Payne

Assistant Examiner — Erin File

(74) *Attorney, Agent, or Firm* — Katten Muchin Rosenman LLP

(57) **ABSTRACT**

A communication apparatus calculates a residual component by noting one of a given plurality of transmitted signals and by canceling a component corresponding to a candidate/candidates for the other/others of the plurality of transmitted signals from a signal corresponding to one of a plurality of received signals. The communication apparatus determines a candidate for the given transmitted signal by selecting a value closest to the residual component from among the values that the given transmitted signal can take, and obtains a plurality of candidate groups by changing that given transmitted signal, each candidate group being constructed as a collection of candidate sets each comprising a candidate for that given transmitted signal and a candidate/candidates for that other transmitted signal/signals. Then, the communication apparatus selects transmitted signal candidate sets that are common to the plurality of candidate groups and estimates the plurality of transmitted signals using the selected candidate sets.

12 Claims, 20 Drawing Sheets

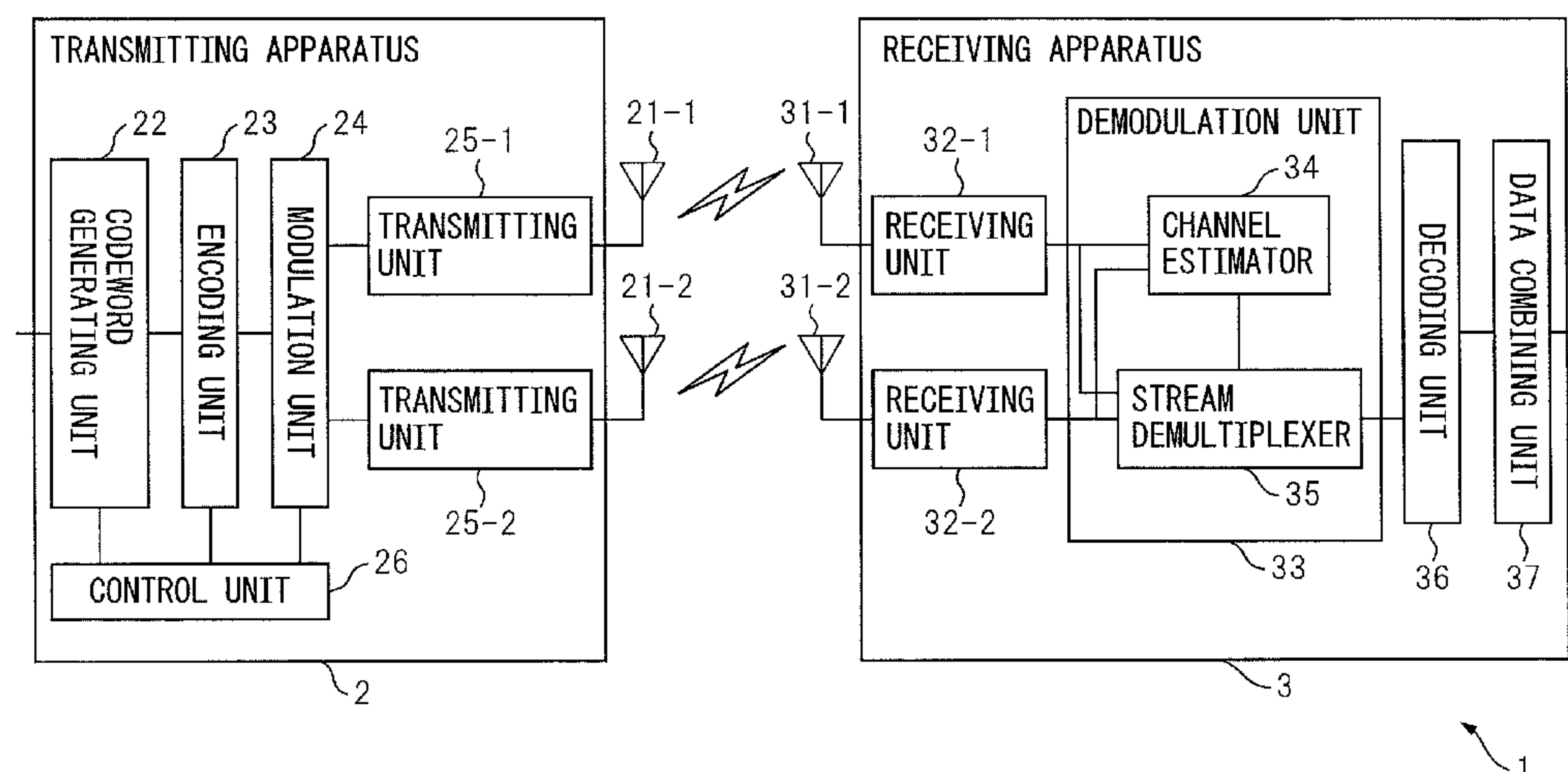


FIG. 1

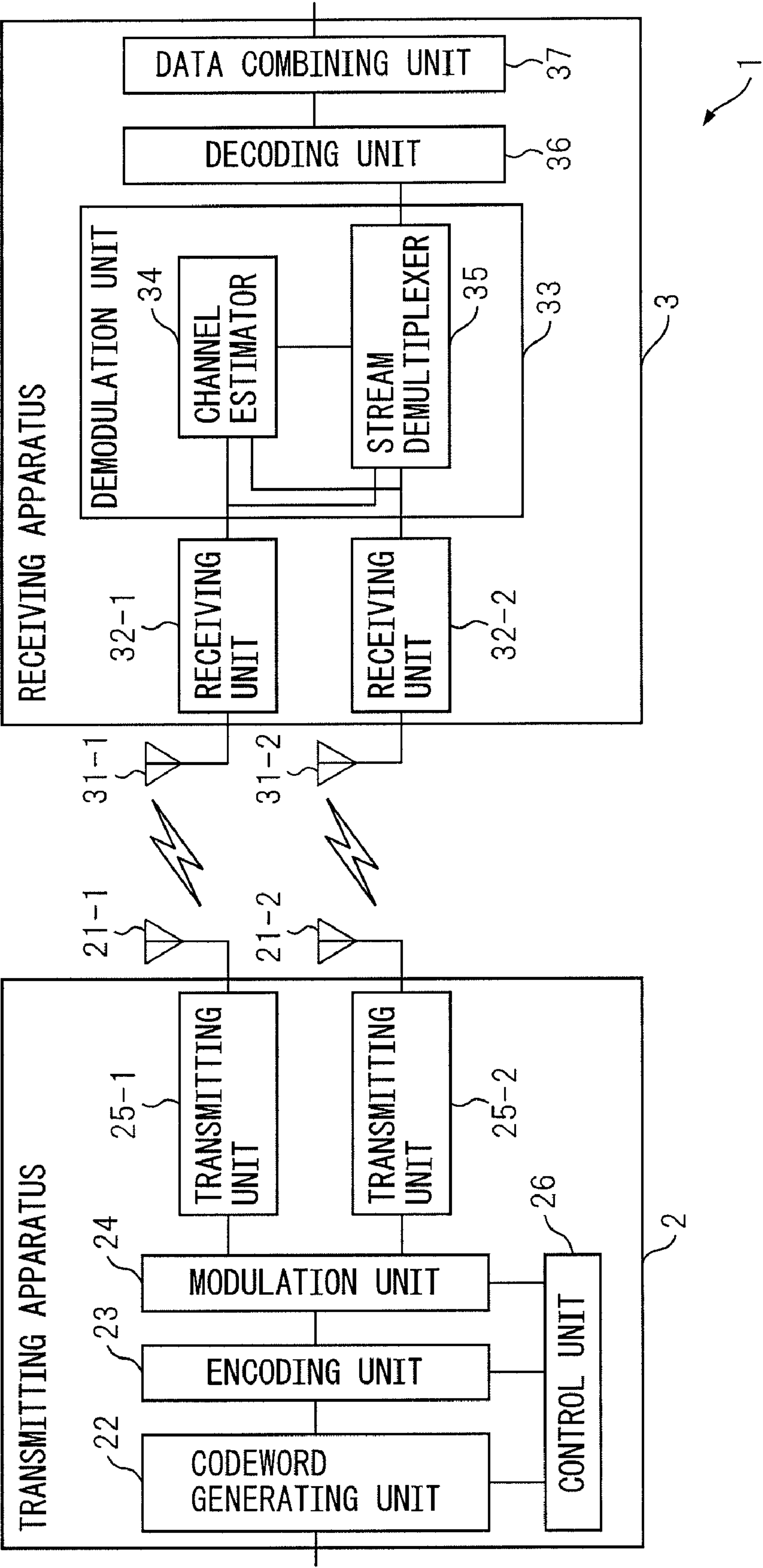


FIG. 2

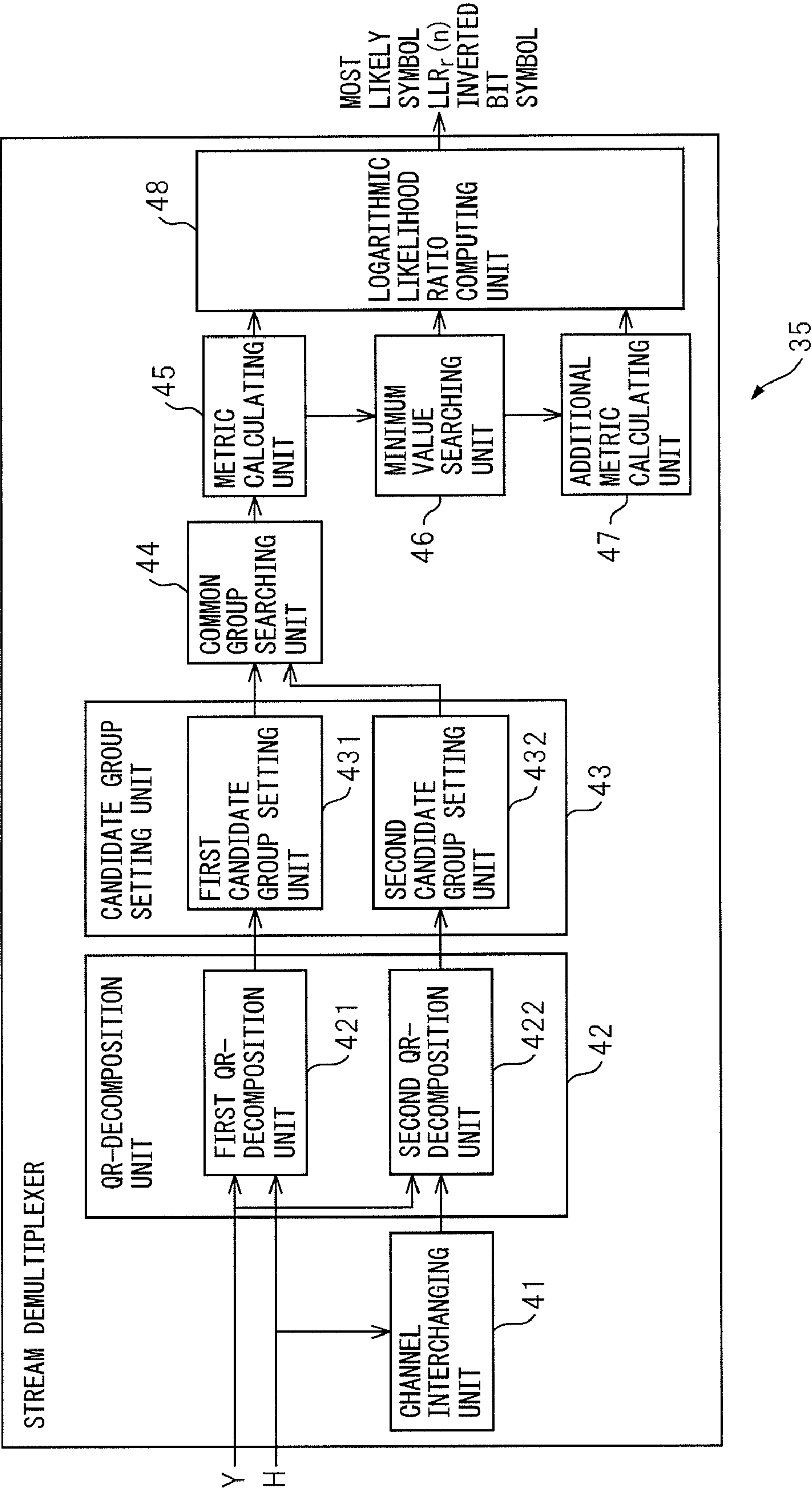


FIG. 3A

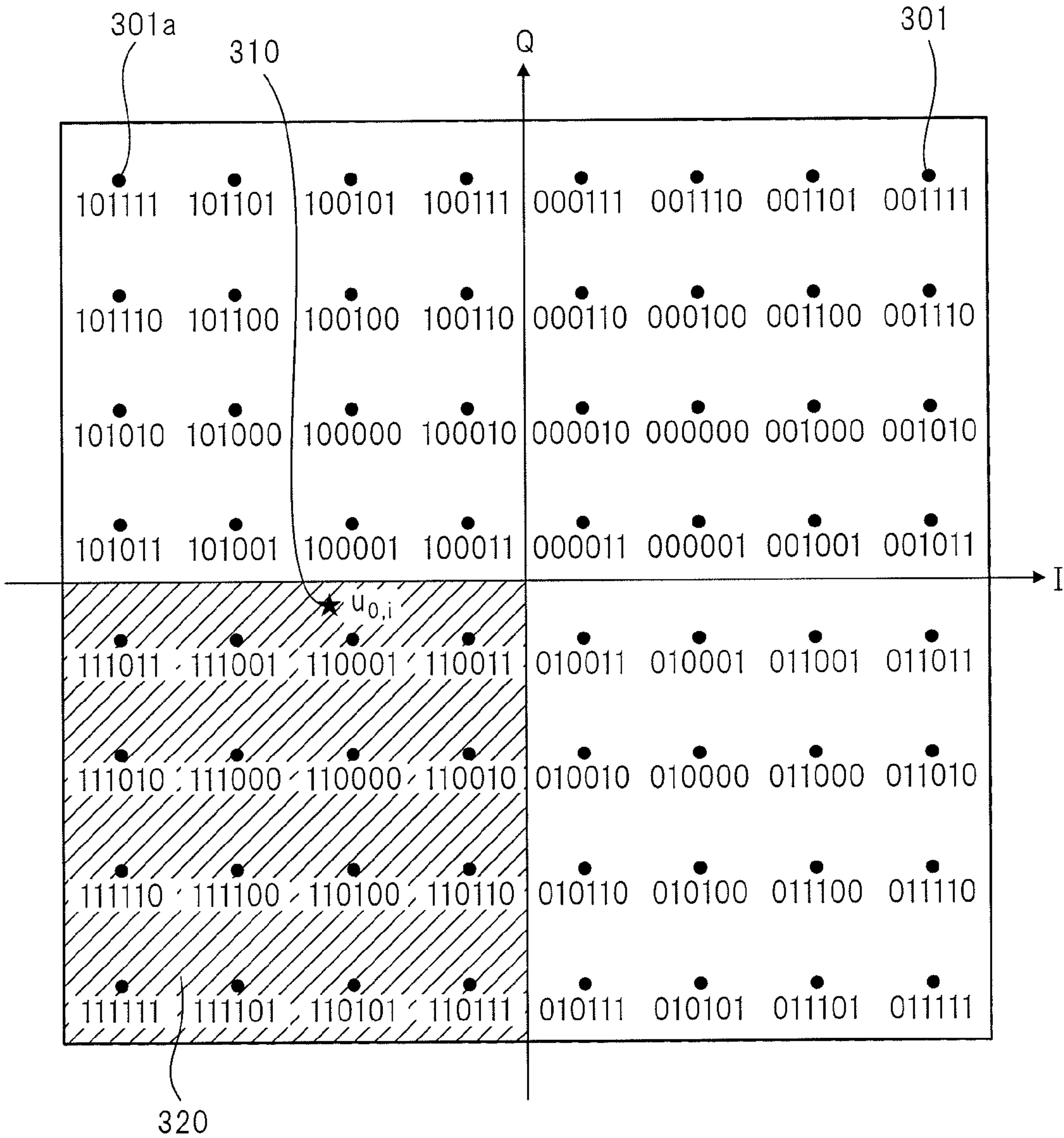


FIG. 3B

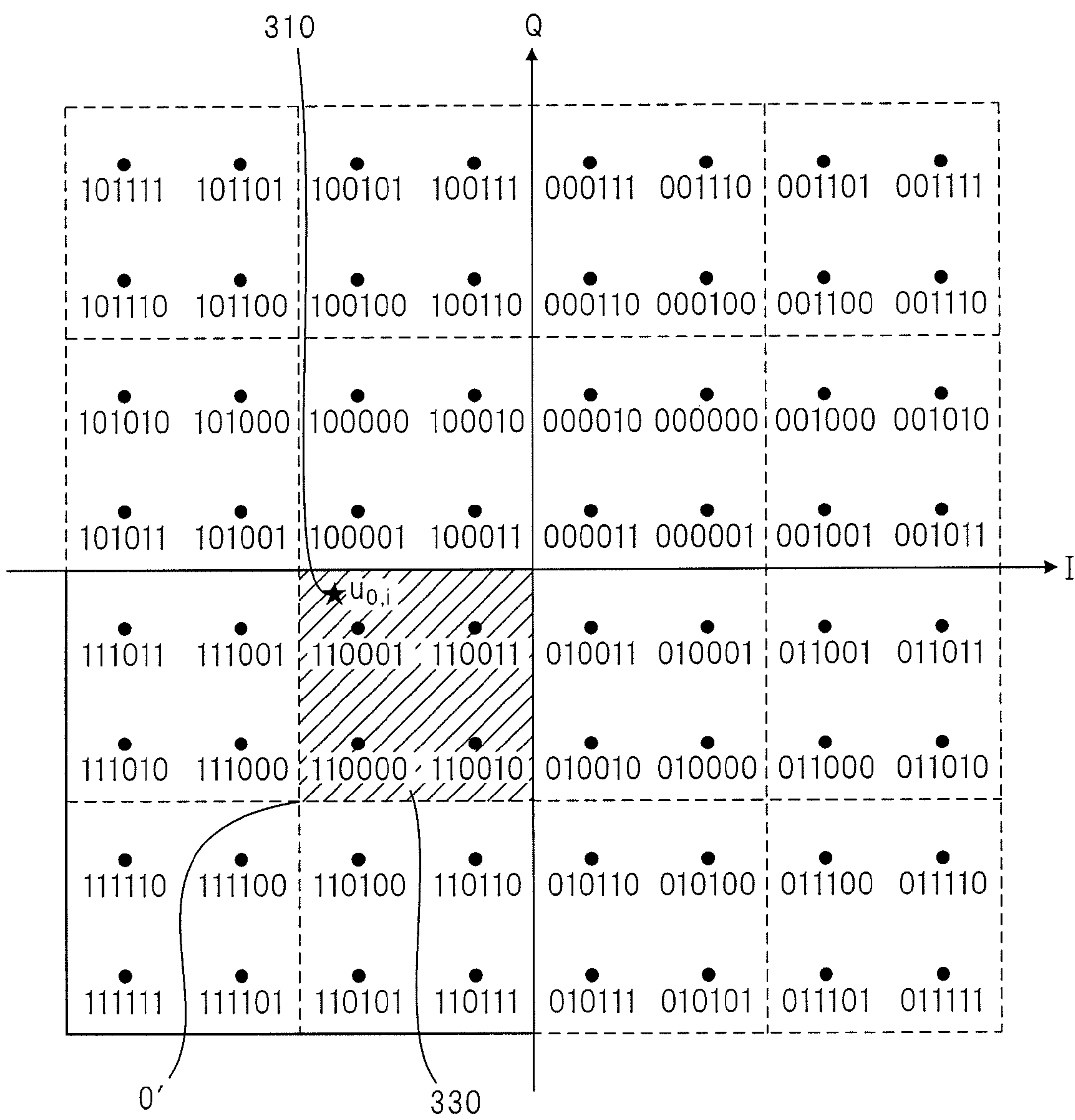


FIG. 3C

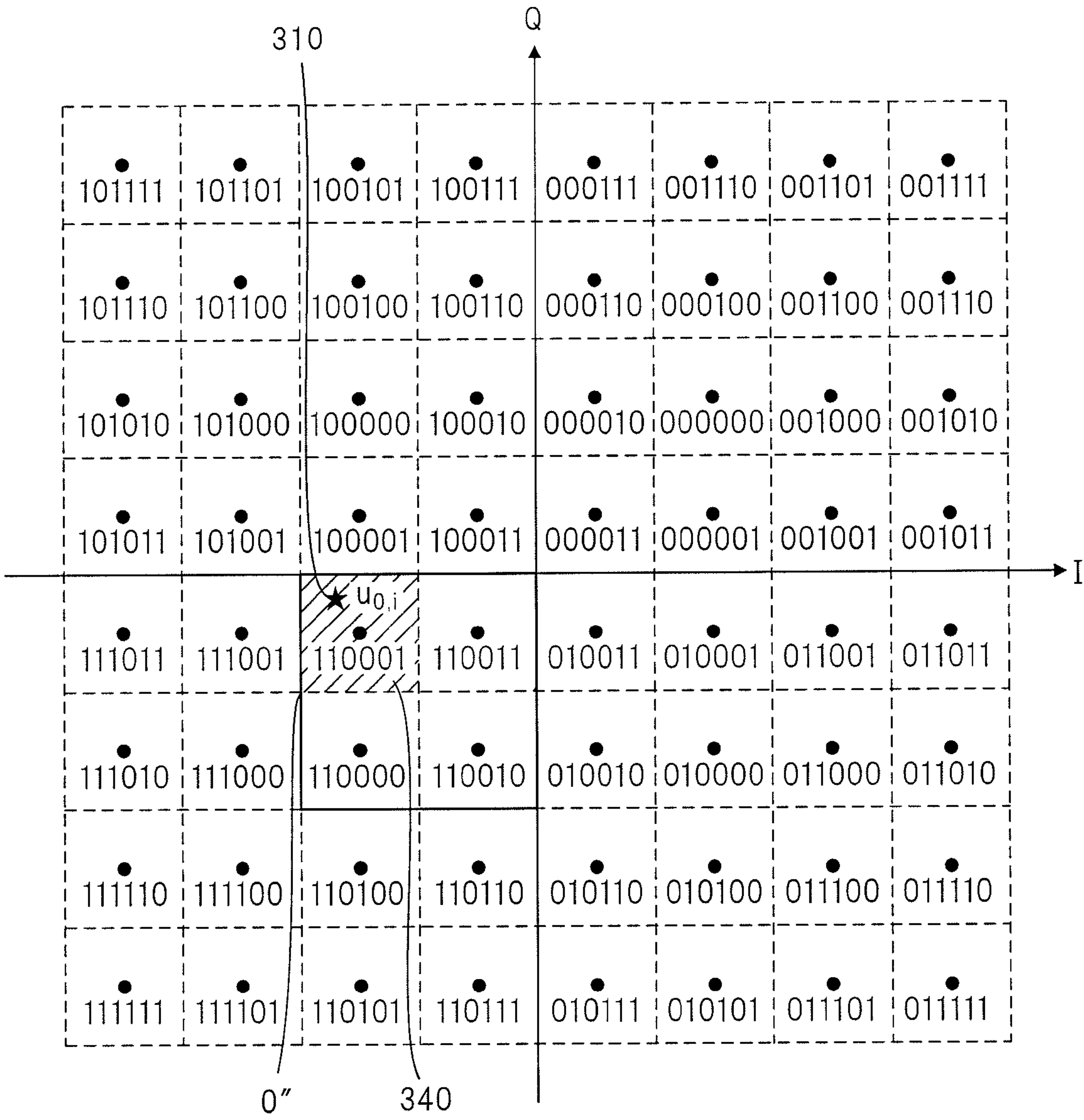


FIG. 4

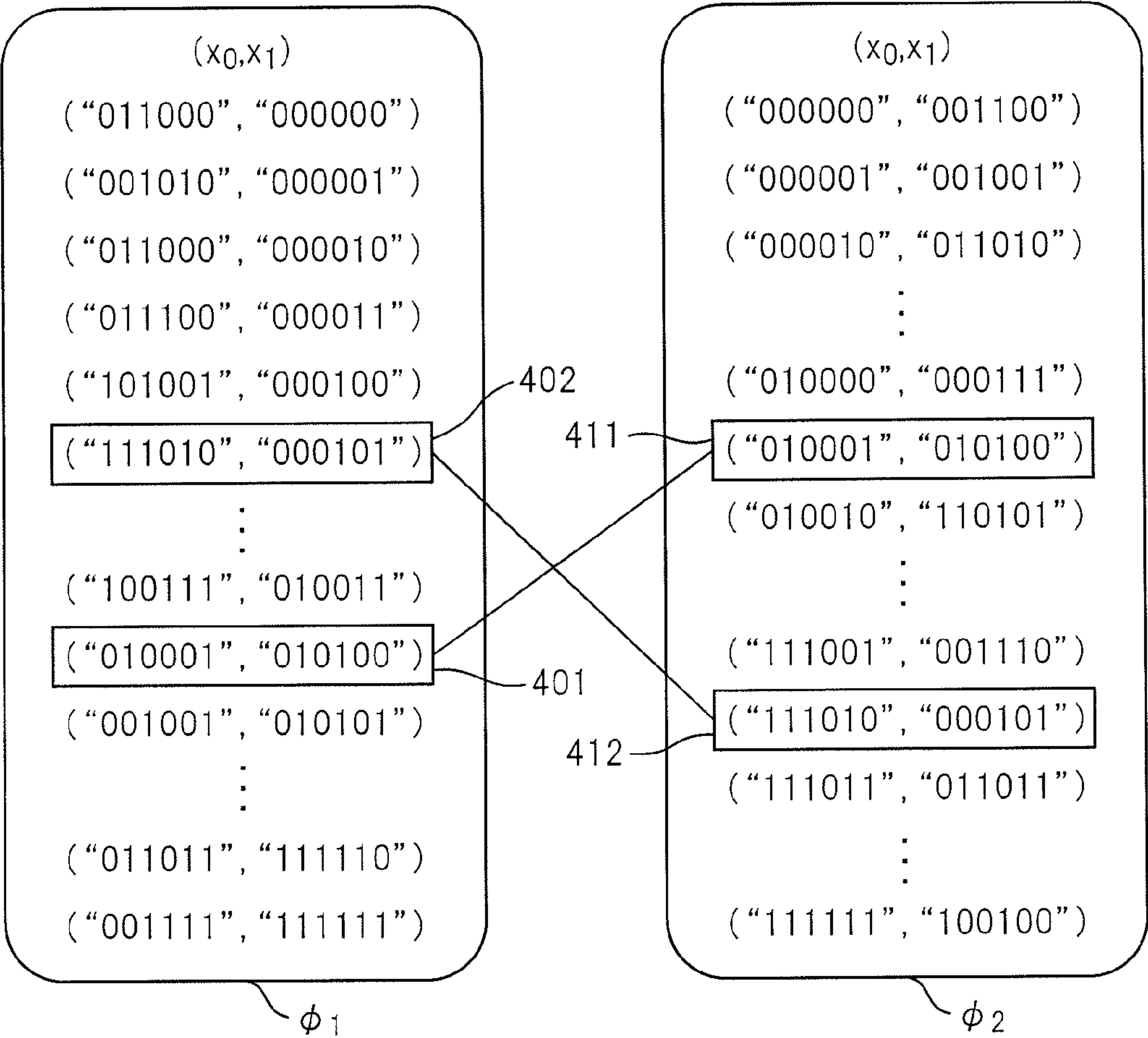


FIG. 5

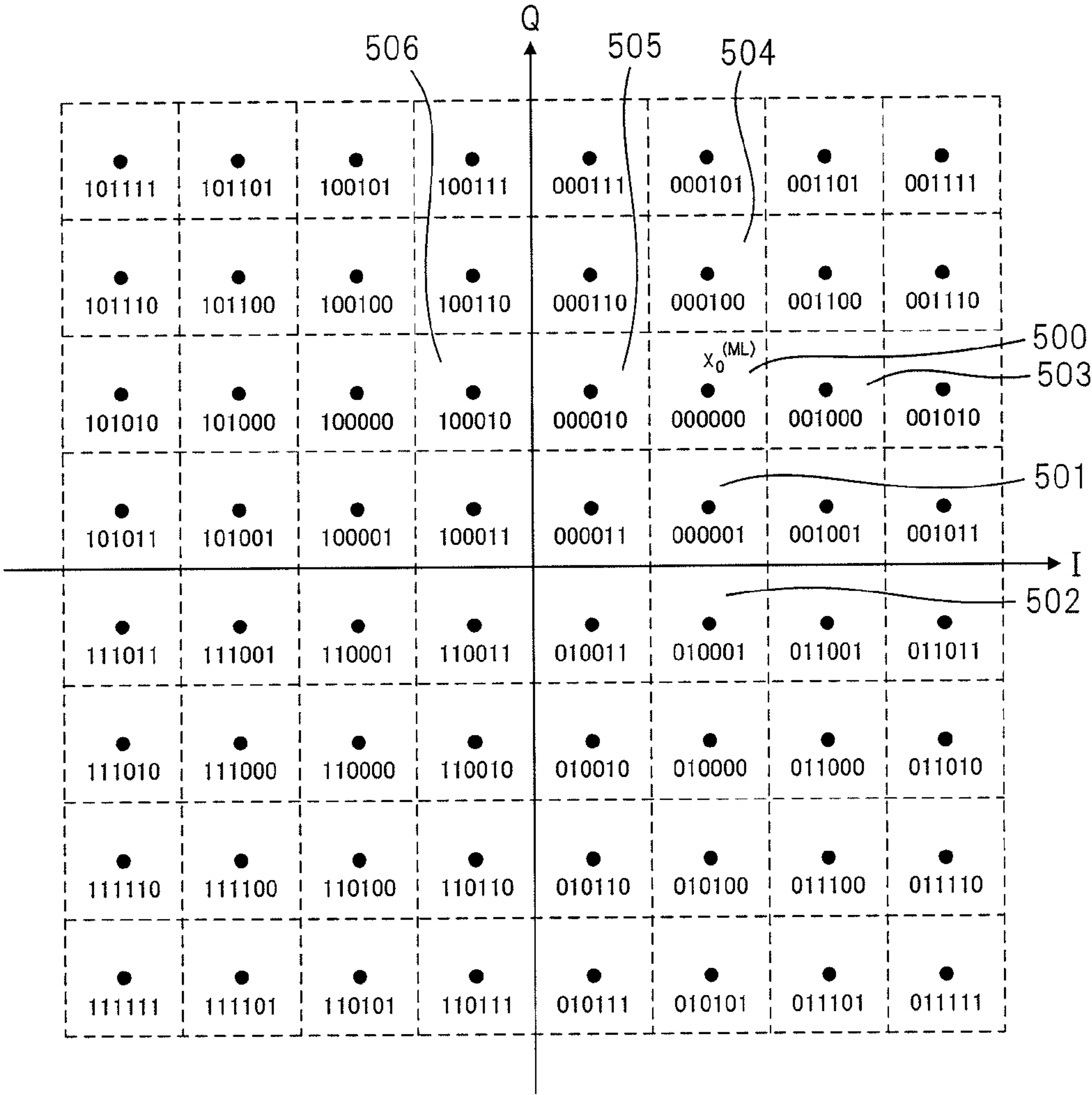


FIG. 6

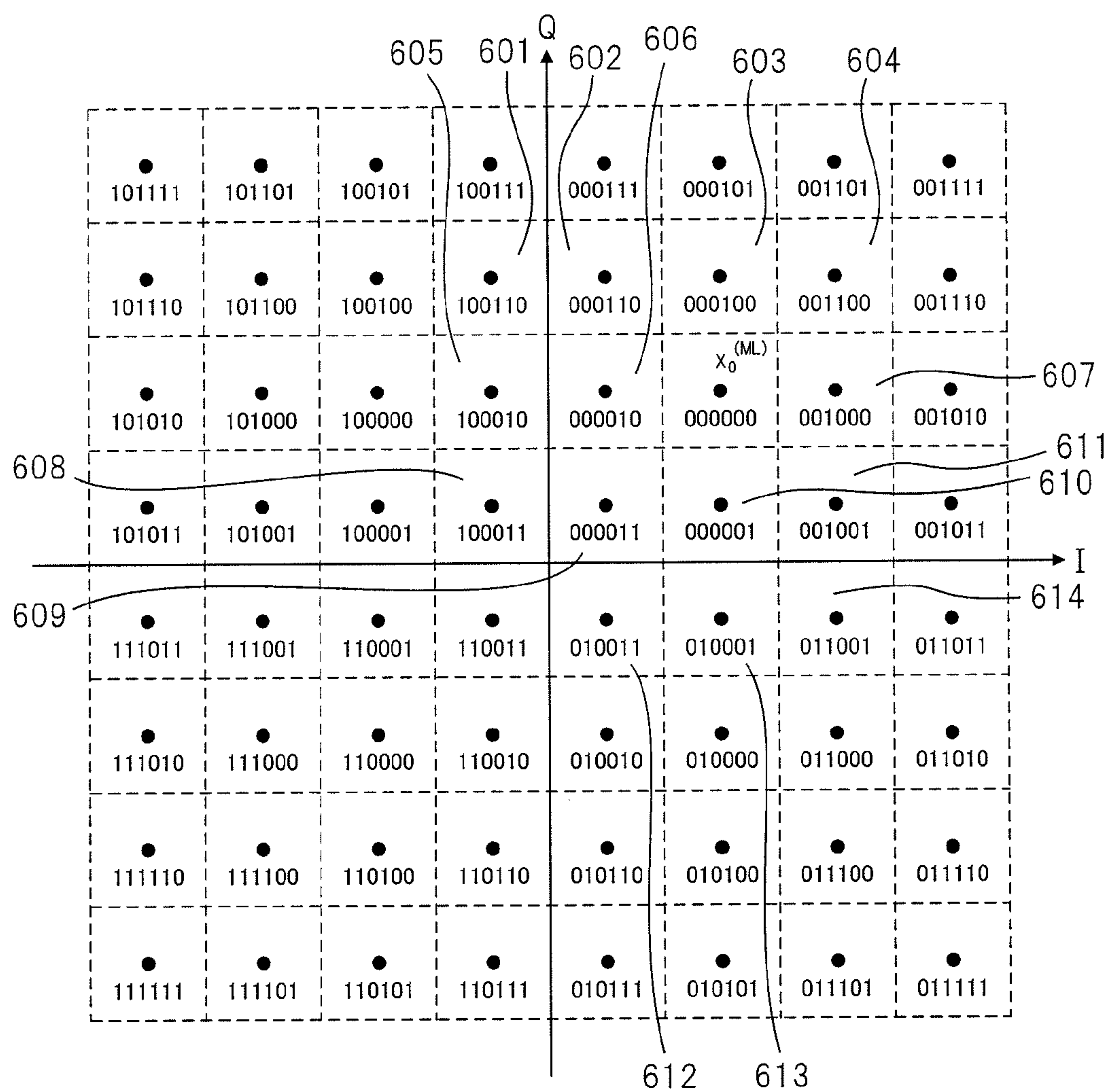


FIG. 7A

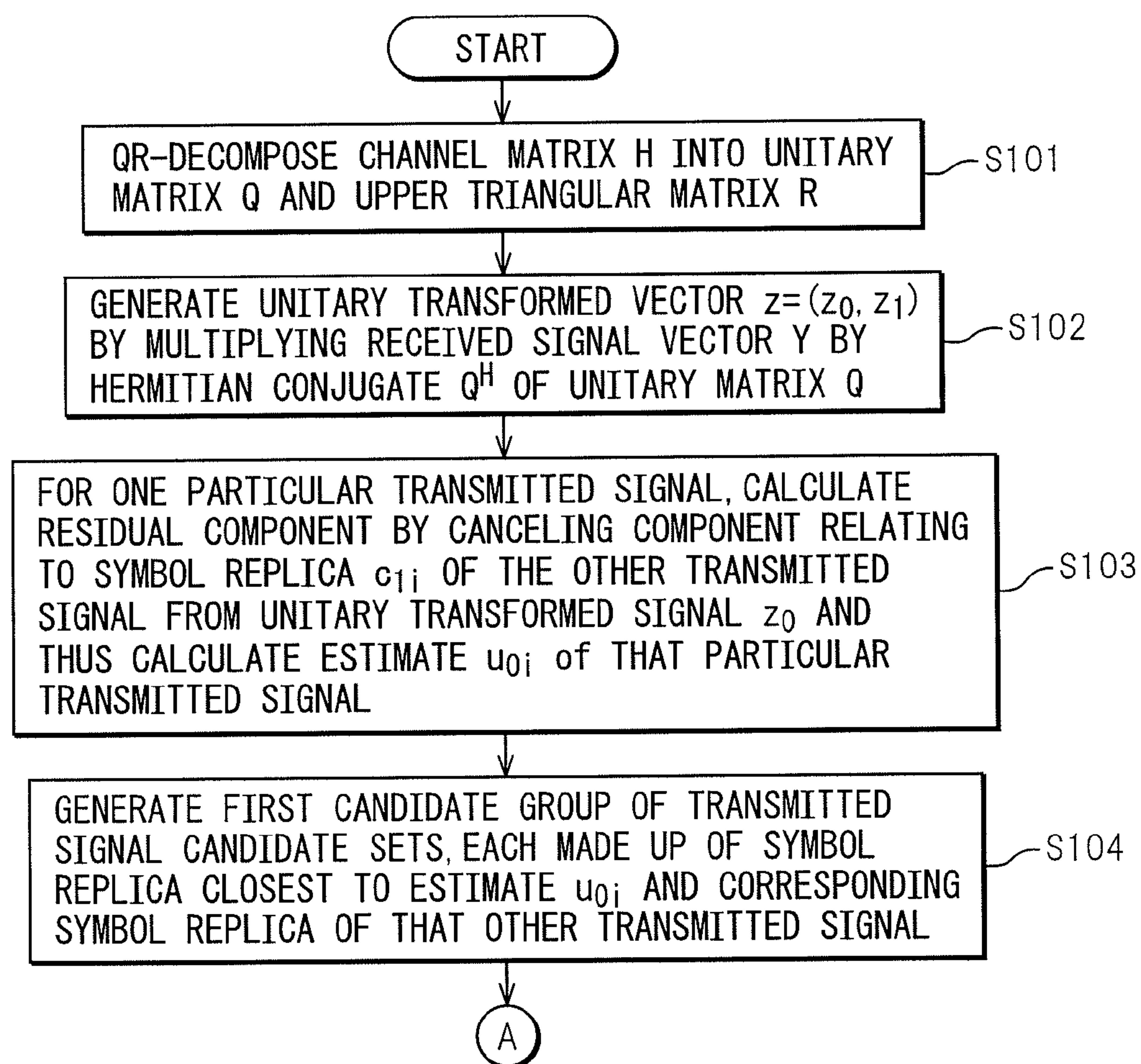


FIG. 7B

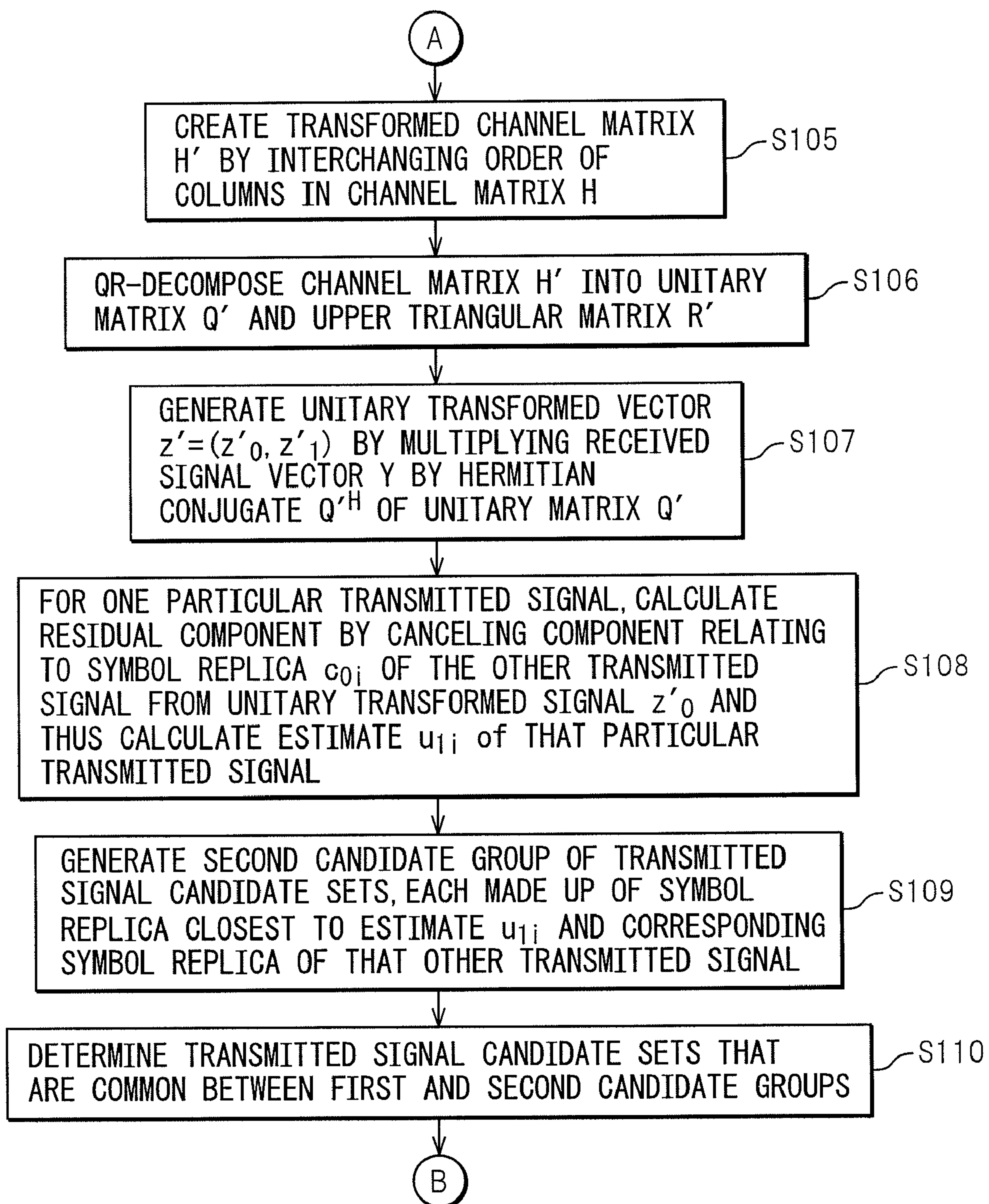


FIG. 8

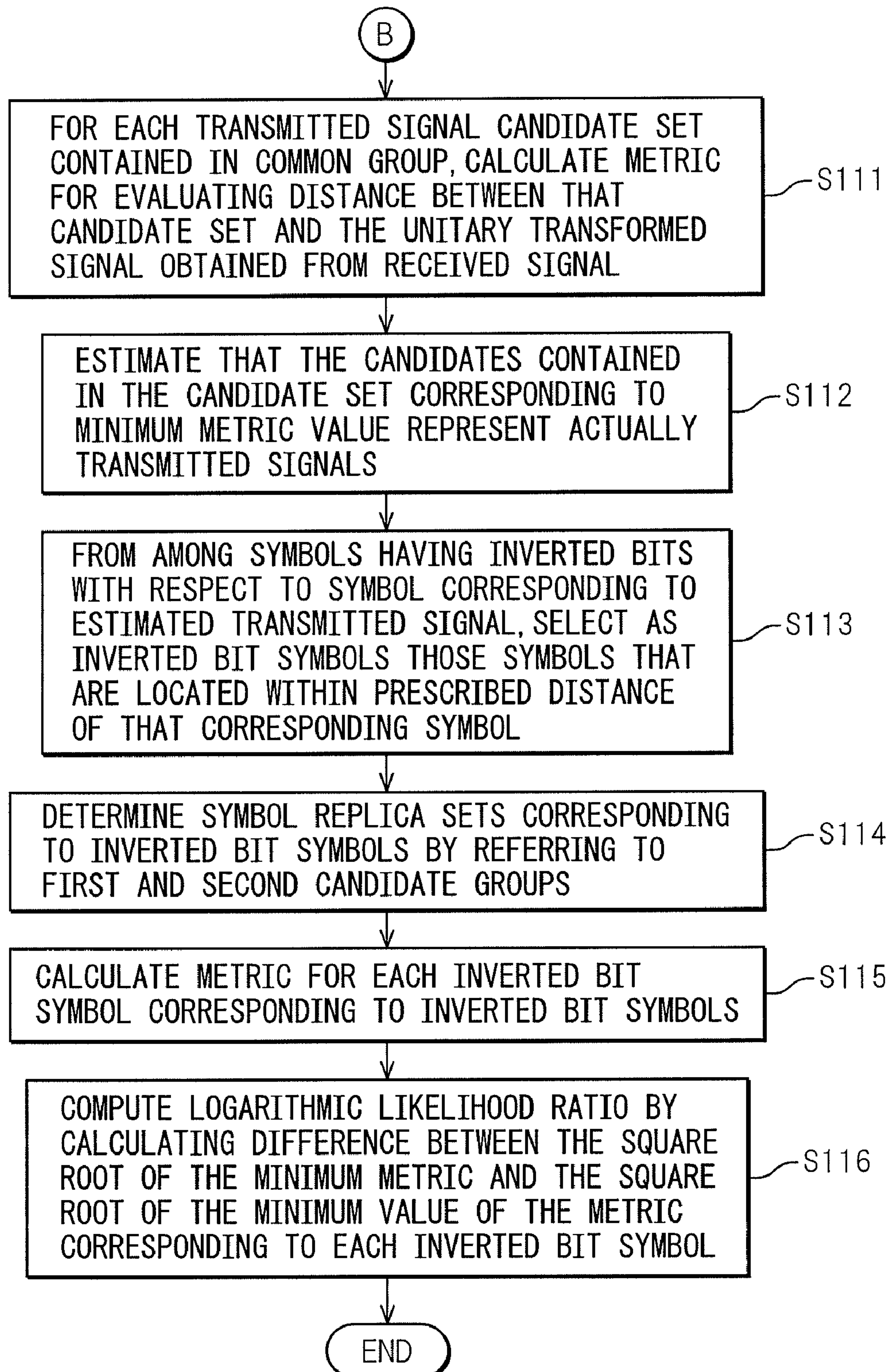


FIG. 9

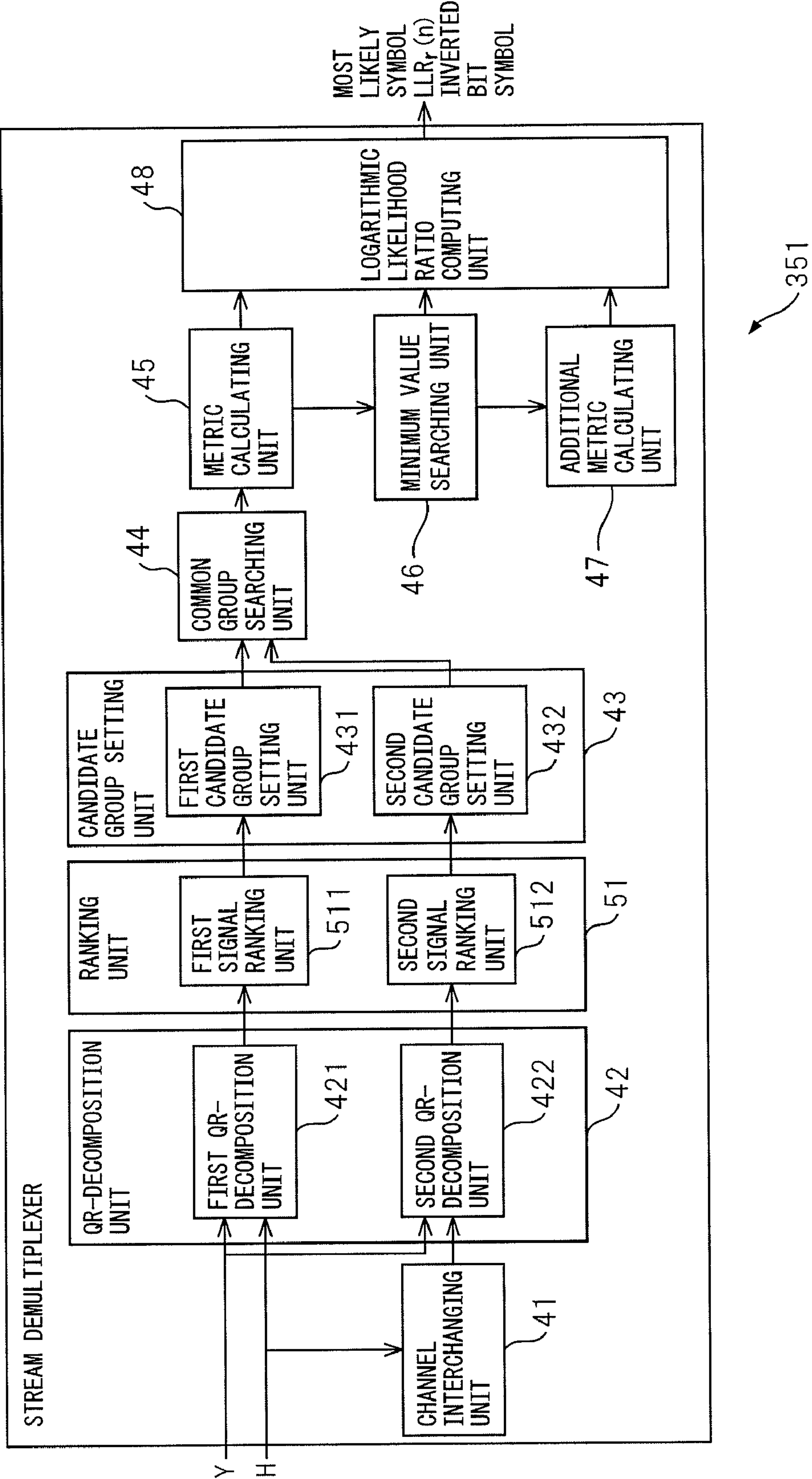


FIG.10A

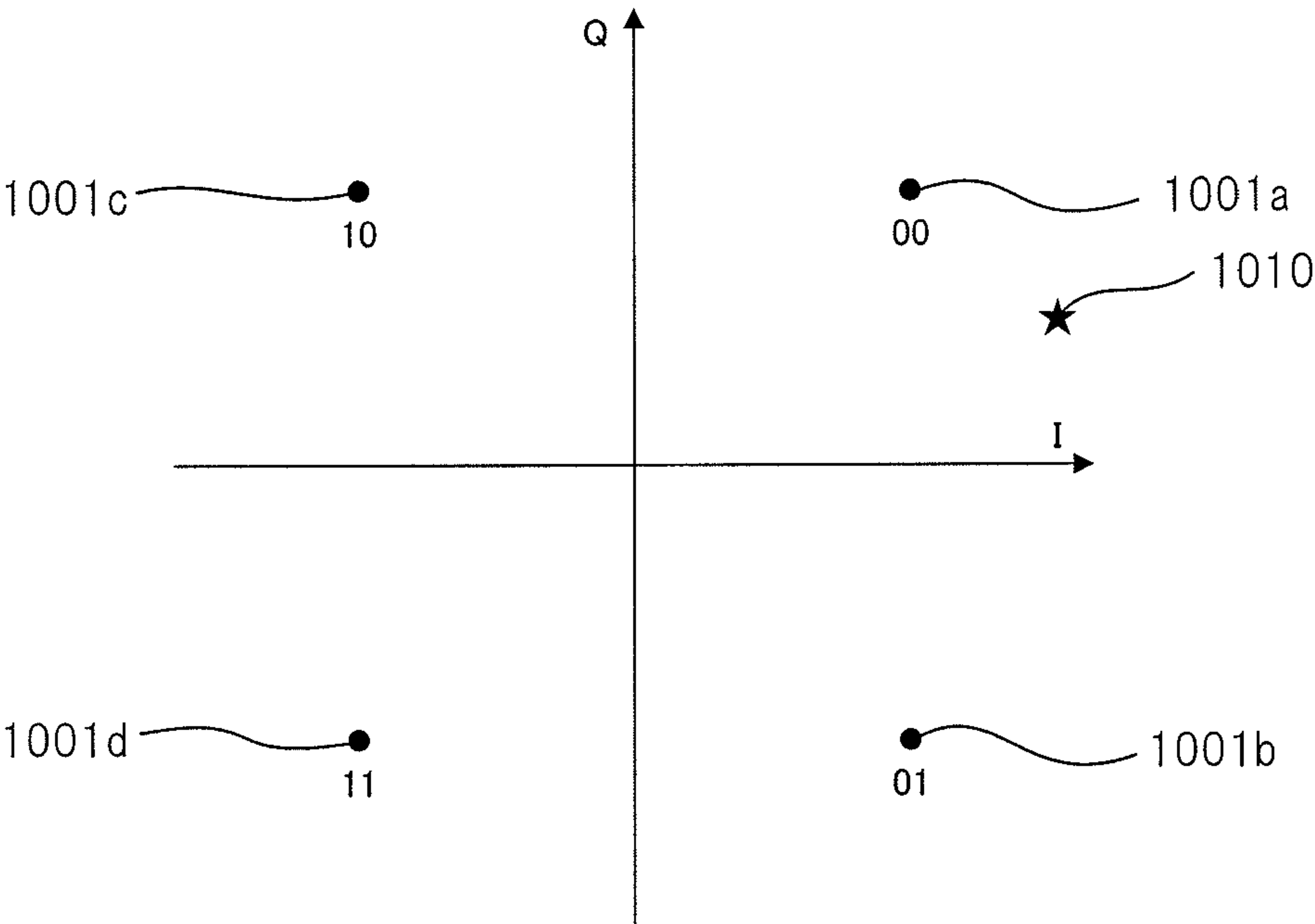


FIG.10B

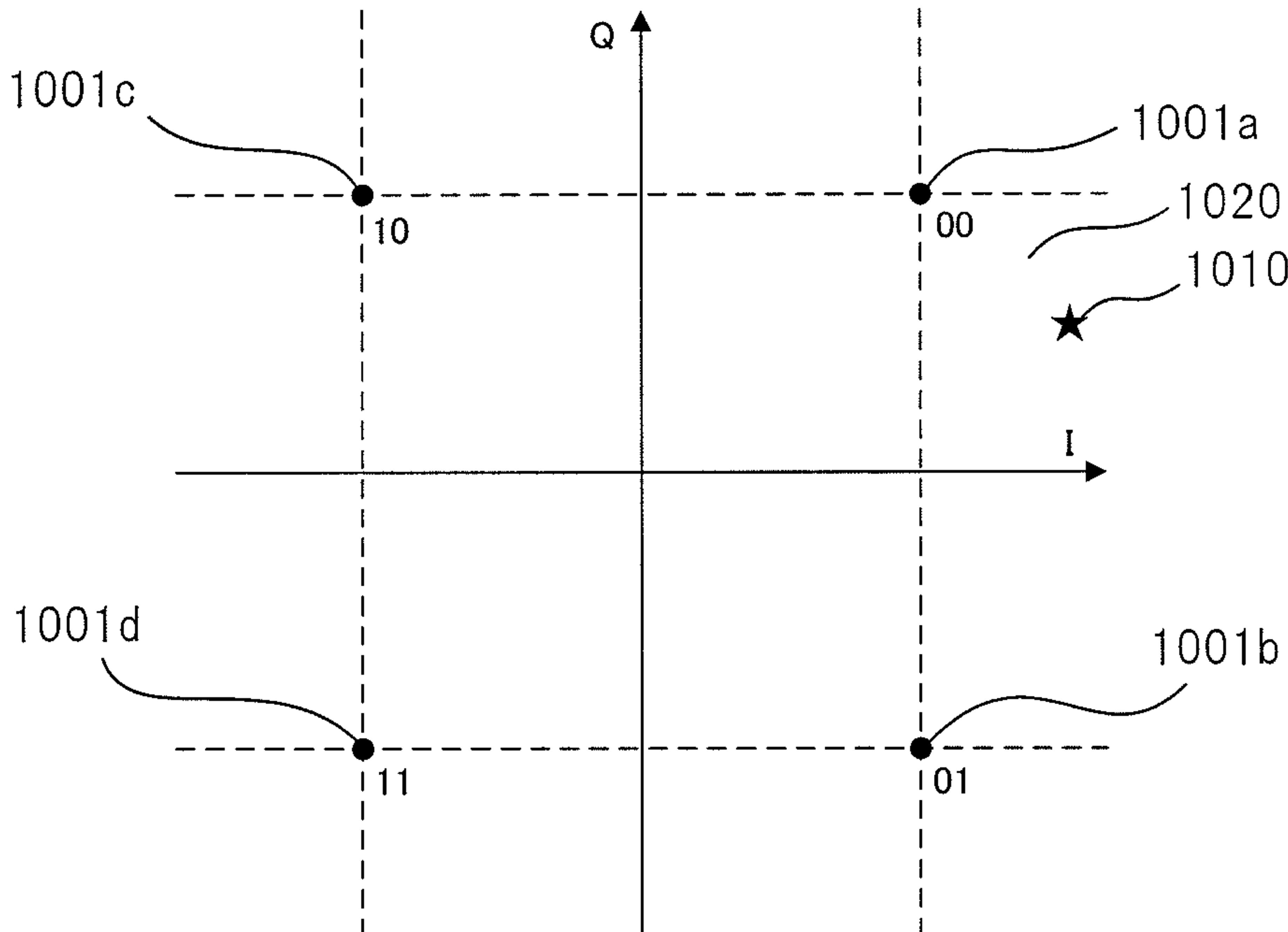


FIG. 11A

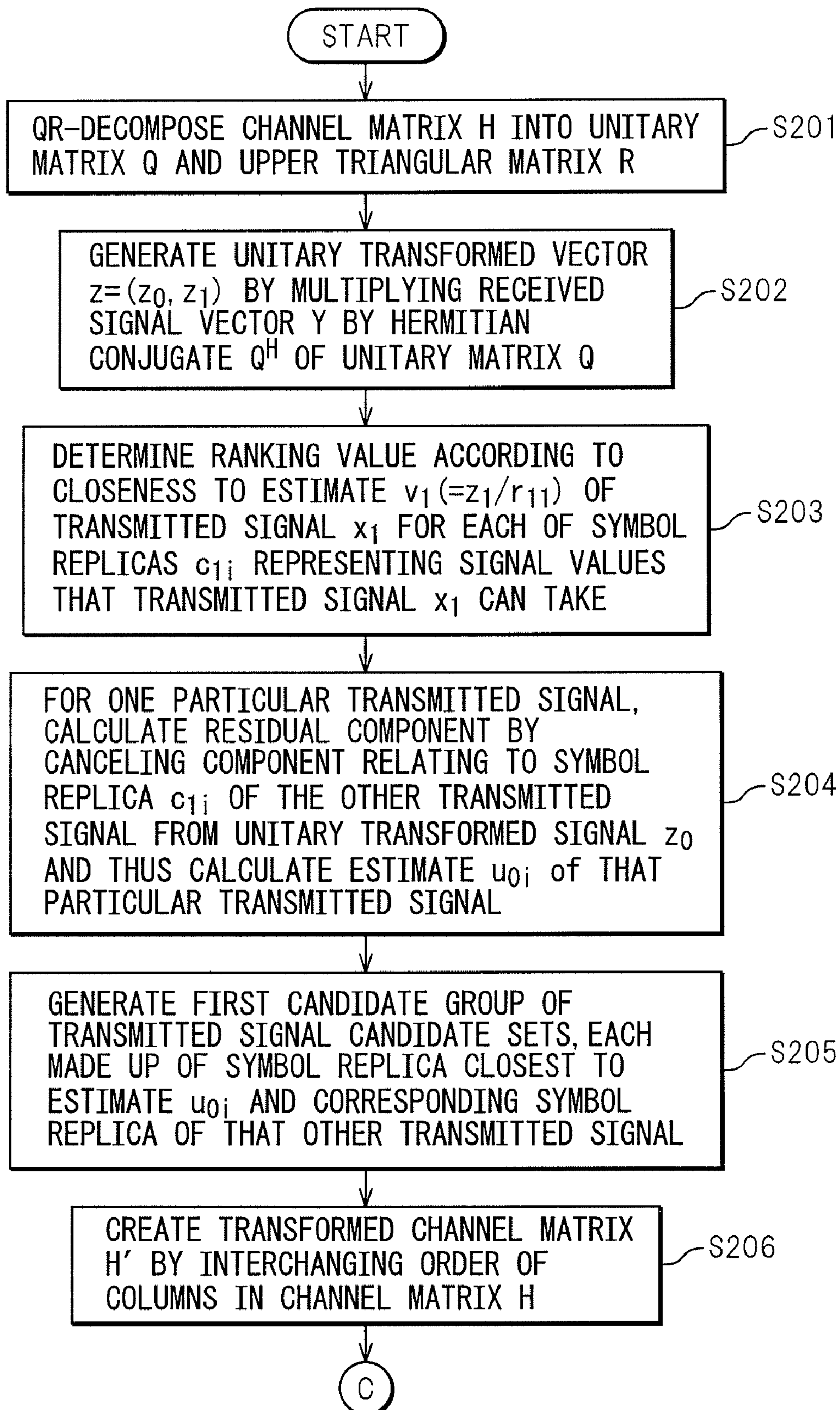


FIG. 11B

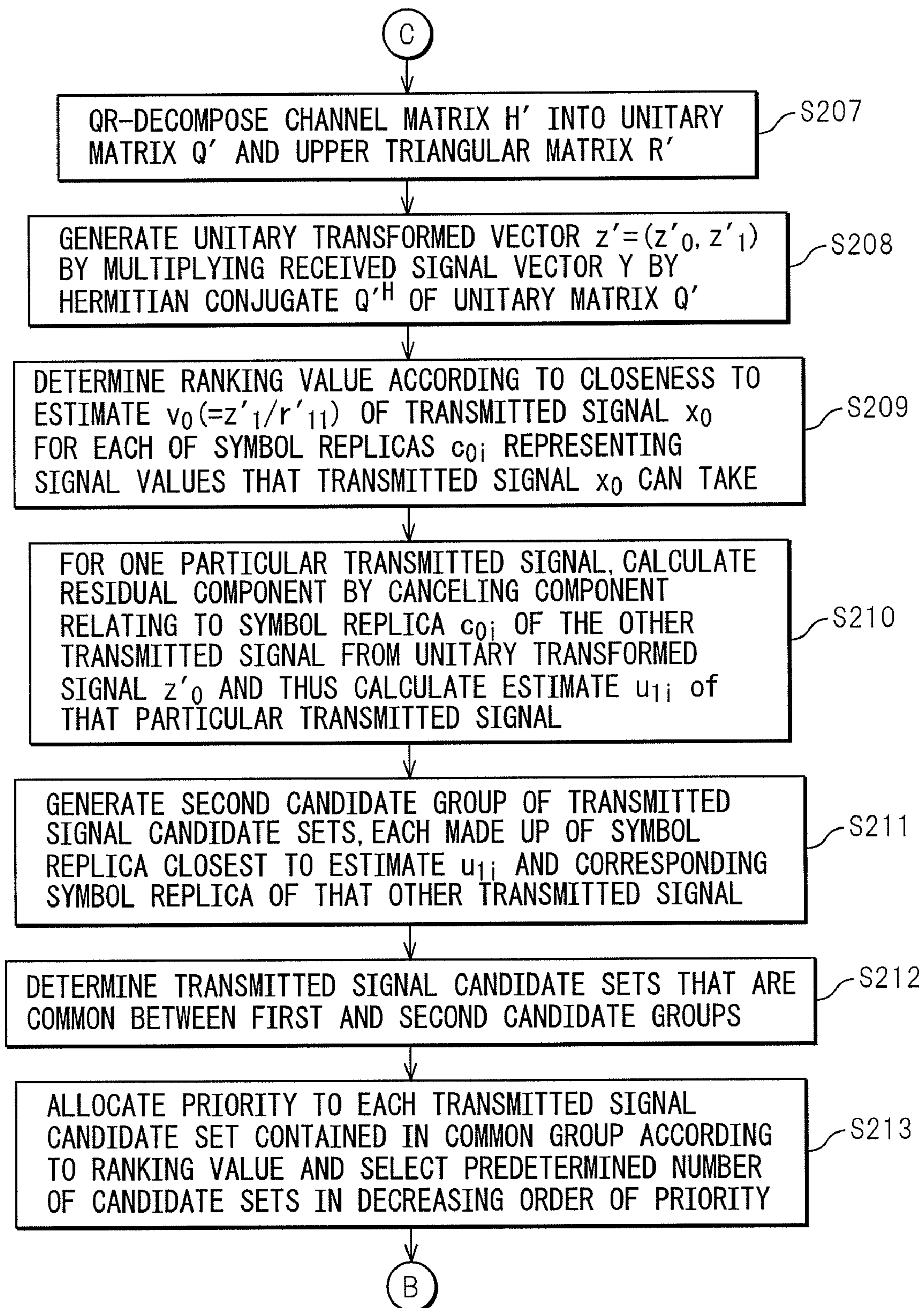


FIG. 12

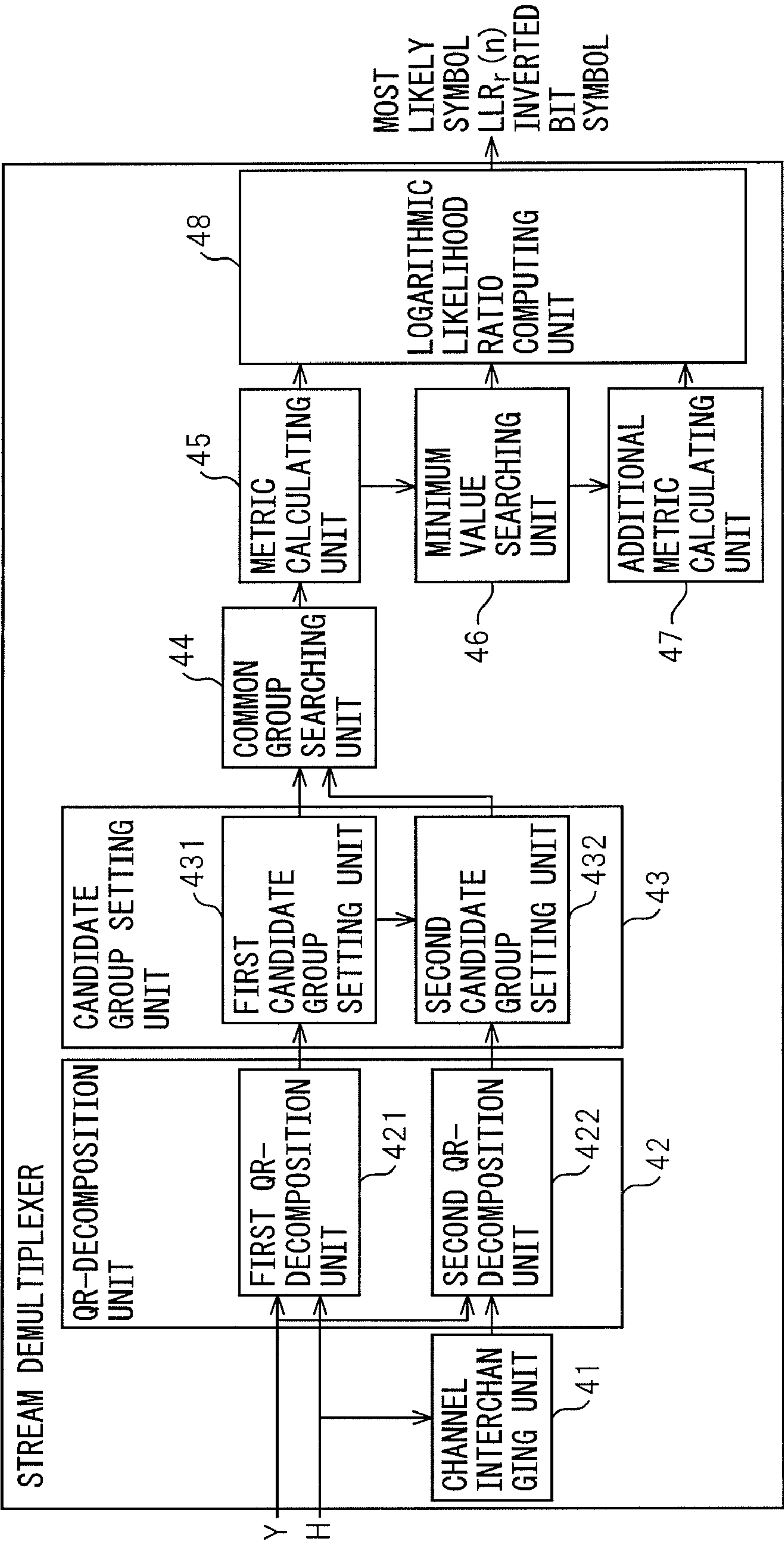
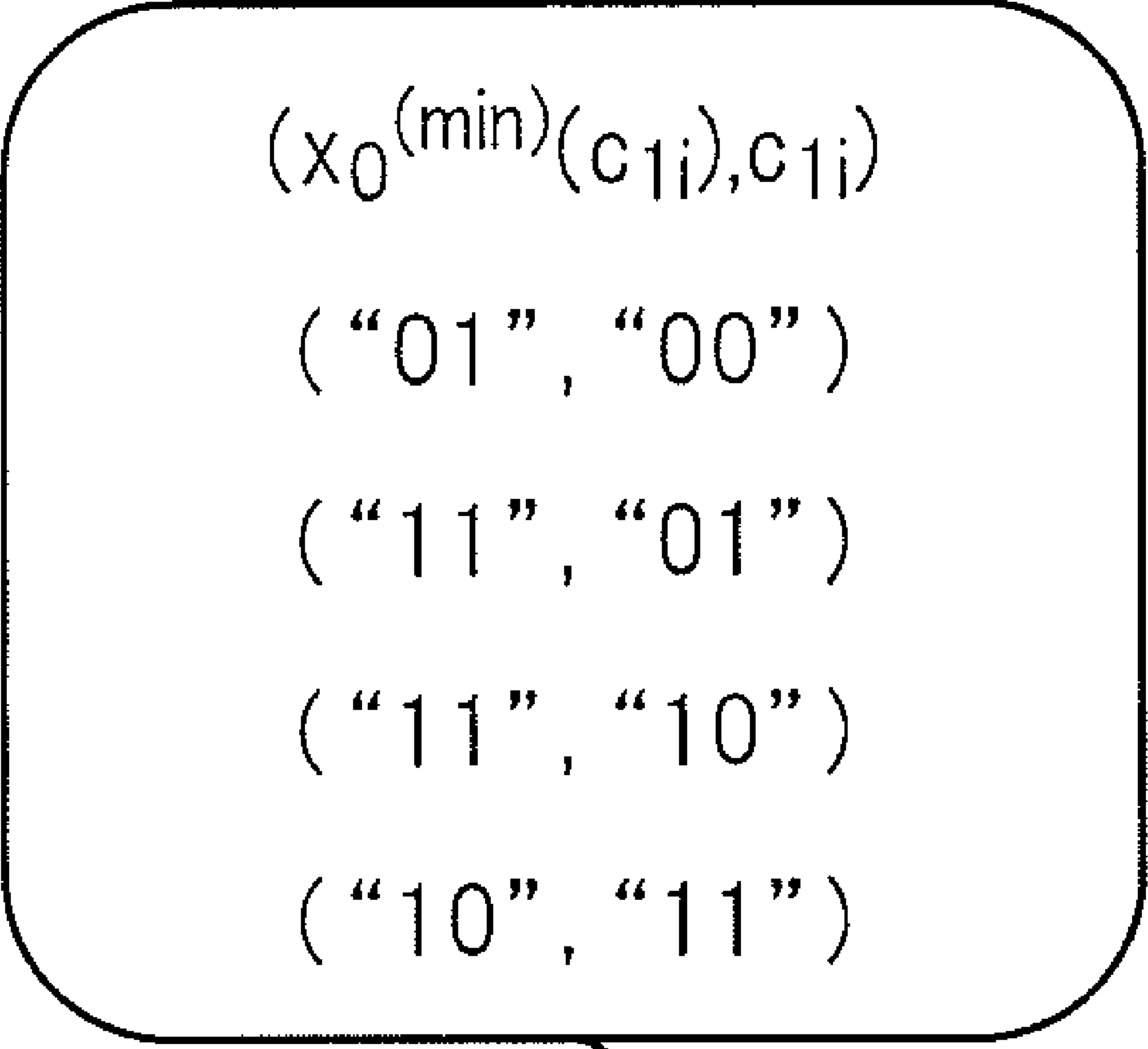


FIG. 13



$(x_0^{(\min)}(c_{1i}), c_{1i})$

("01", "00")

("11", "01")

("11", "10")

("10", "11")

$\phi 1$

FIG.14

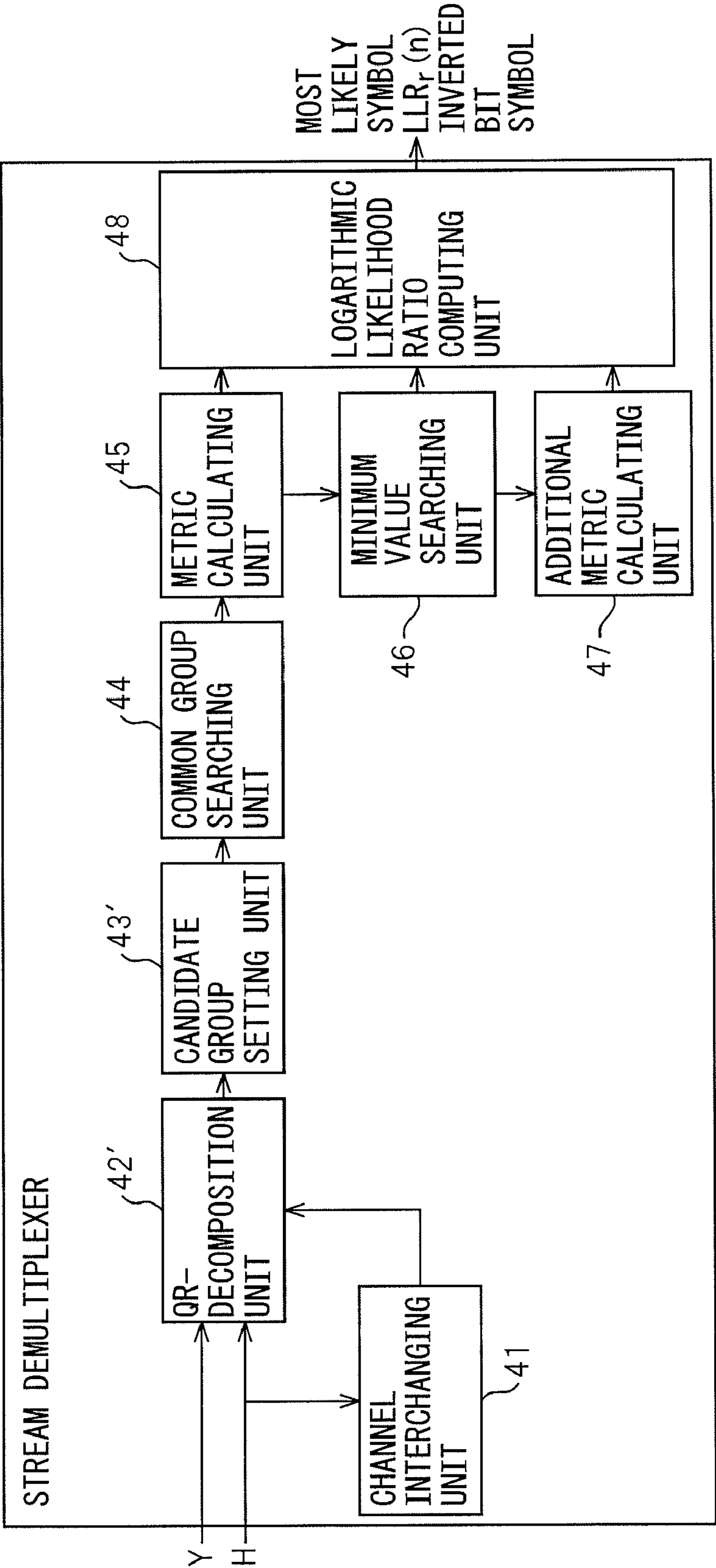


FIG. 15

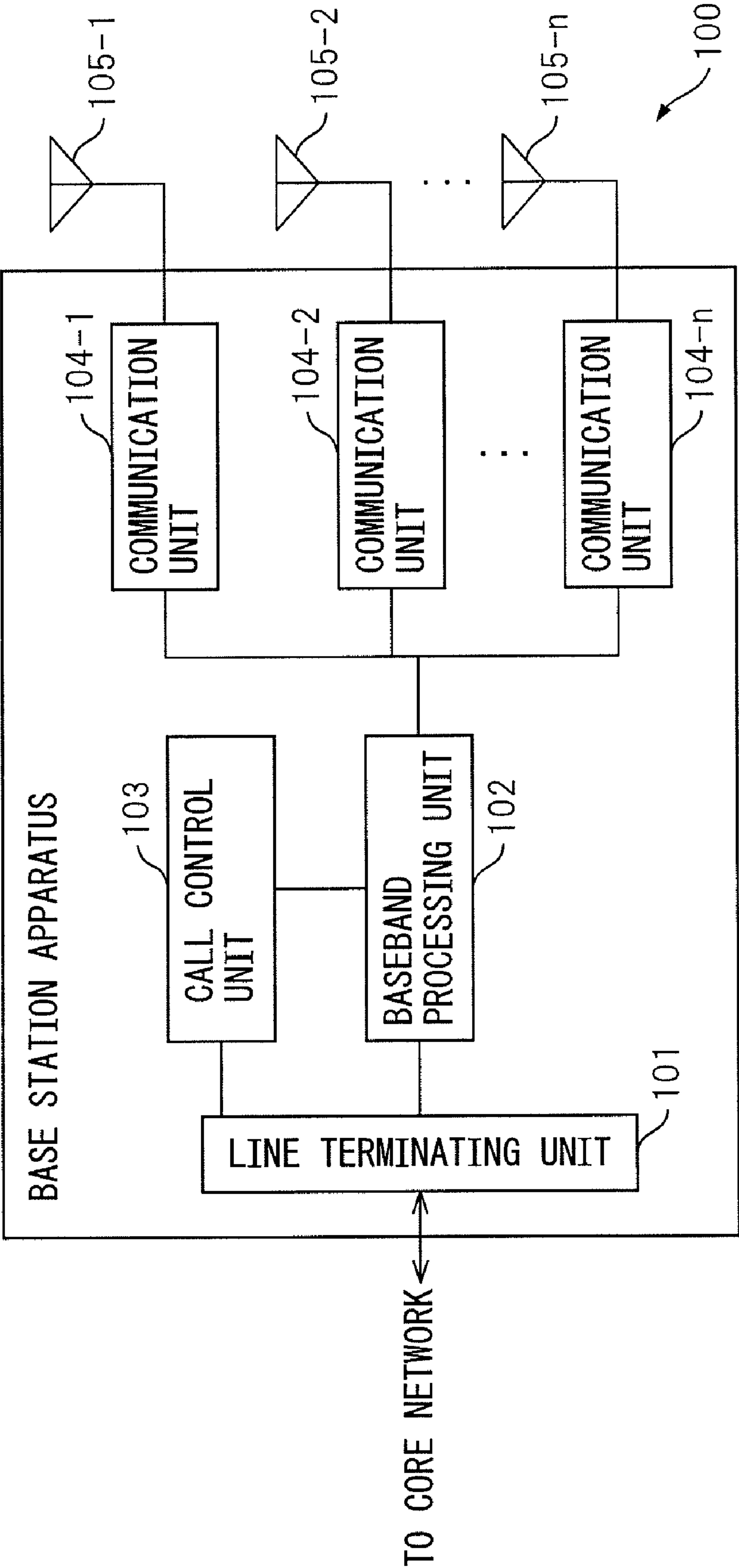
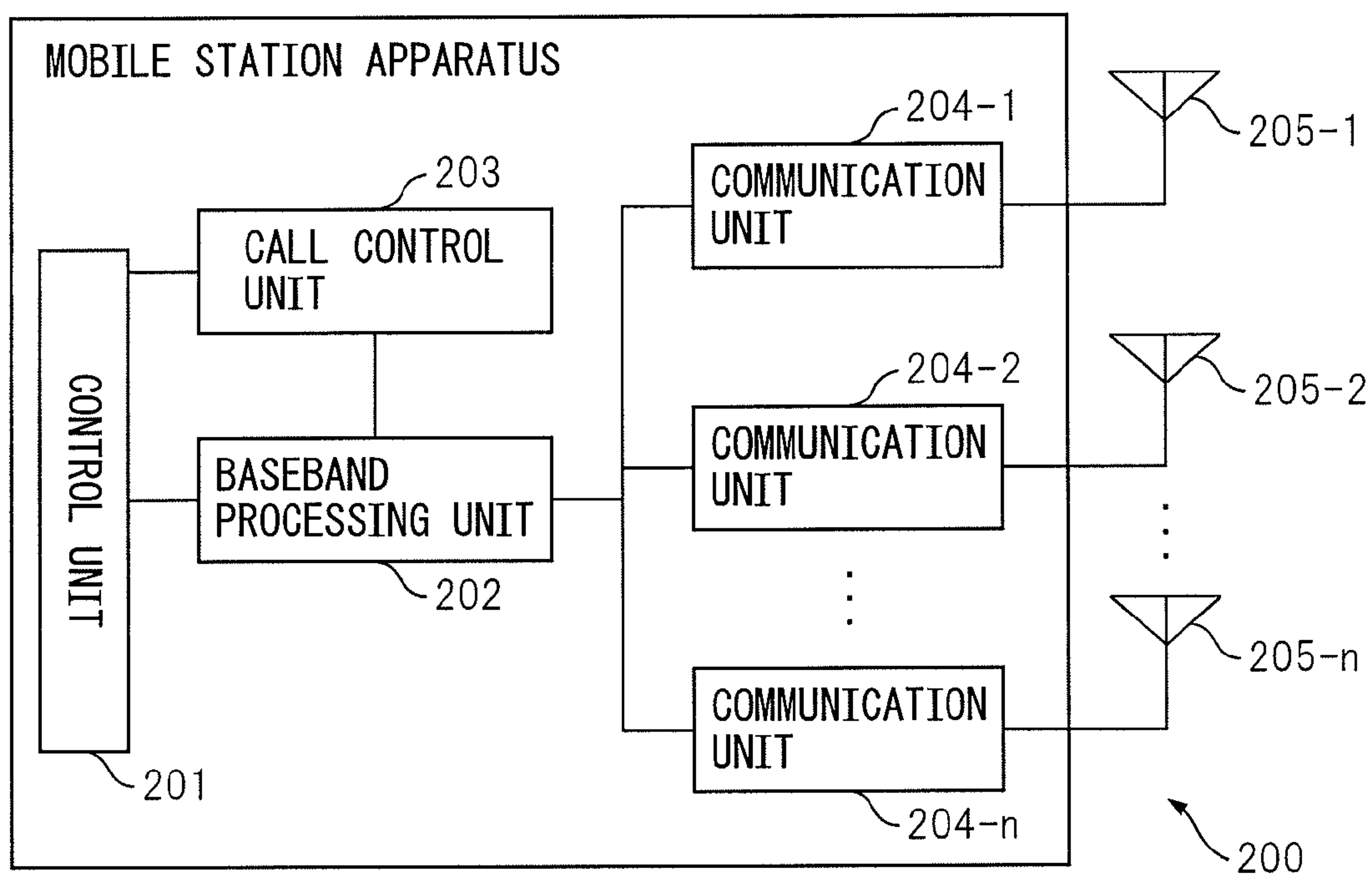


FIG. 16



1

COMMUNICATION APPARATUS AND
COMMUNICATION METHODCROSS-REFERENCE TO RELATED
APPLICATION

This application is based upon and claims the benefit of priority of the prior Japanese Patent Application No. 2010-106243, filed on May 6, 2010, the entire contents of which are incorporated herein by reference.

FIELD

The embodiments discussed herein are related to a communication apparatus and communication method wherein signals transmitted from a plurality of different antennas are received using a plurality of antennas.

BACKGROUND

There has long been a need to enhance data transmission speed in wireless communications. To address this, work on next-generation data communication standards, such as Long Term Evolution (LTE) has been proceeding. In high-speed data communication standards such as LTE, Multiple Input Multiple Output (MIMO) technology has been attracting attention, since it can apparently increase the bandwidth by transmitting and receiving signals in parallel using multiple antennas at both the transmitting and receiving ends.

In a communication system using MIMO technology, a transmitting apparatus equipped with a plurality of antennas splits one or more data streams into a plurality of signals for transmission. The transmitting apparatus transmits each signal via one of the antennas. On the other hand, a receiving apparatus, which is also equipped with a plurality of antennas, receives the transmitted signals from the transmitting apparatus by the respective antennas. The receiving apparatus then demultiplexes the simultaneously transmitted signals from the signals received by the respective antennas. To demultiplex the transmitted signals, a known method such as Minimum Mean Square Error (MMSE) or Maximum Likelihood Detection (MLD) is used. A receiving apparatus using MLD compares the actually received set of signals with each of the sets of received signals estimated from the sets of candidates for the likely transmitted signals, selects the transmitted signal candidates corresponding to the mostly likely set among the estimated sets, and takes the thus selected signal candidates as the actually transmitted signals. To compare the actually received set of signals with each of the sets of received signals estimated from the sets of transmitted signal candidate, the receiving apparatus using MLD calculates a metric such as the squared Euclidian distance between the two received signal sets.

Compared with a linear demultiplexing method such as MMSE, MLD can achieve excellent reception characteristics. However, the amount of computation that MLD performs in order to demultiplex the transmitted signals from the received signals is larger than the amount of computation that a linear demultiplexing method such as MMSE performs in order to demultiplex the transmitted signals. In particular, in the case of MLD, the number of metric calculations increases exponentially as the number of simultaneously transmitted signals and the number of values that the modulation scheme used for transmission can take increase.

In view of the above, MLD techniques that can reduce the amount of computation have been proposed (for example, refer to: Japanese Laid-Open Patent Publication Nos. 2006-

2

121348 and 2009-33636; K. J. Kim and J. Yue, "Joint channel estimation and data detection algorithms for MIMO-OFDM systems," in Proc. Thirty-Sixth Asilomar Conference on Signals, Systems and Computers, Nov. 2002, pp. 1857-1861; K. Higuchi, H. Kawai, N. Maeda, and M. Sawahashi, "Adaptive Selection of Surviving Symbol Replica Candidates Based on Maximum Reliability in QRM-MLD for OFCDM MIMO Multiplexing," Proc. of IEEE Globecom 2004, November 2004, pp. 2480-2486; and M. Siti and M. P. Fitz, "Layered Orthogonal Lattice Detector for Two Transmit Antenna Communications," in Proc. Allerton Conference on Communication Control and Computing, September 2005).

For example, K. J. Kim and J. Yue describe using QRM-MLD which reduces the number of metric calculations by combining QR decomposition with M algorithm. Suppose that the relationship between N transmitted signals (x_0, x_1, \dots, x_{N-1}) simultaneously transmitted from a transmitting apparatus and N received signals (y_0, y_1, \dots, y_{N-1}) received by a receiving apparatus is expressed by the following equation. Here, N is an integer not smaller than 2. Further, the number of transmitted signals need not be the same as the number of received signals, i.e., the number of antennas of the receiving apparatus. As long as the number of antennas of the receiving apparatus is greater than the number of simultaneously transmitted signals, the signals can be transmitted and received using MIMO technology.

$$Y = HX \quad (1)$$

$$\begin{pmatrix} y_0 \\ y_1 \\ \vdots \\ y_{N-1} \end{pmatrix} = \begin{pmatrix} h_{0,0} & h_{0,1} & \dots & h_{0,N-1} \\ h_{1,0} & h_{1,1} & \dots & h_{1,N-1} \\ \vdots & \vdots & \ddots & \vdots \\ h_{N-1,0} & h_{N-1,1} & \dots & h_{N-1,N-1} \end{pmatrix} \begin{pmatrix} x_0 \\ x_1 \\ \vdots \\ x_{N-1} \end{pmatrix}$$

where the matrix H represents the effective channel matrix describing the correspondence between the transmitted signals and the received signals. In equation (1), noise added to the transmitted signals is omitted for simplicity. In QRM-MLD, the effective channel matrix H is decomposed into a unitary matrix Q and a triangular matrix R, and expressed as shown in the following equation.

$$H = QR \quad (2)$$

$$\begin{pmatrix} h_{0,0} & h_{0,1} & \dots & h_{0,N-1} \\ h_{1,0} & h_{1,1} & \dots & h_{1,N-1} \\ \vdots & \vdots & \ddots & \vdots \\ h_{N-1,0} & h_{N-1,1} & \dots & h_{N-1,N-1} \end{pmatrix} = \begin{pmatrix} q_{0,0} & q_{0,1} & \dots & q_{0,N-1} \\ q_{1,0} & q_{1,1} & \dots & q_{1,N-1} \\ \vdots & \vdots & \ddots & \vdots \\ q_{N-1,0} & q_{N-1,1} & \dots & q_{N-1,N-1} \end{pmatrix} \begin{pmatrix} r_{0,0} & r_{0,1} & \dots & r_{0,N-1} \\ 0 & r_{1,1} & \dots & r_{1,N-1} \\ \vdots & \ddots & \ddots & \vdots \\ 0 & \dots & 0 & r_{N-1,N-1} \end{pmatrix}$$

By multiplying both sides of equation (1) from the left by the Hermitian conjugate Q^H of the unitary matrix Q, the following equation is obtained.

$$Z = Q^H Y = Q^H Q R X = R X \quad (3)$$

-continued

$$\begin{pmatrix} z_0 \\ z_1 \\ \vdots \\ z_{N-1} \end{pmatrix} = \begin{pmatrix} r_{0,0} & r_{0,1} & \dots & r_{0,N-1} \\ 0 & r_{1,1} & \dots & r_{1,N-1} \\ \vdots & \ddots & \ddots & \vdots \\ 0 & \dots & 0 & r_{N-1,N-1} \end{pmatrix} \begin{pmatrix} x_0 \\ x_1 \\ \vdots \\ x_{N-1} \end{pmatrix}$$

where the vector $z=(z_0, z_1, \dots, z_{N-1})$ is the unitary transformed vector of the received signal vector which is obtained by the product of the received signal vector Y and the matrix Q^H . As shown in equation (3), the number of transmitted signals associated with each element of the unitary transformed vector z differs from one element to another. For example, only the transmitted signal x_{N-1} is associated with the signal z_{N-1} . On the other hand, N transmitted signals x_0 to x_{N-1} are associated with the signal z_0 .

The receiving apparatus calculates as the metric the squared Euclidian distance between each of the values of z_0 to z_{N-1} obtained from the actually received signals and each of the values of z_0 to obtained by substituting the set of symbol replicas corresponding to the likely transmitted signals into the vector X in equation (3). The symbol replicas are signals tentatively set by the receiving apparatus. In MLD, the receiving apparatus estimates that the set of symbol replicas that minimizes the sum of the metrics obtained for all of z_0 to z_{N-1} represents the actually transmitted signals.

The receiving apparatus using QRM-MLD calculates the metrics for the signals z_0 to z_{N-1} in order of increasing number of transmitted signals associated therewith. For example, in equation (3), the number of transmitted signals associated with the signal z_{N-1} is the smallest. Accordingly, the receiving apparatus calculates in the first stage the metrics for the signal z_{N-1} , and then calculates in the second stage the metrics for the signal z_{N-2} which is the second smallest in terms of the number of transmitted signals associated therewith. In the m -th stage, the receiving apparatus calculates the metrics only for M symbol replicas selected in increasing order of the metrics calculated for the signal z_{m-1} in the immediately preceding stage. For example, suppose that $M=3$ and that the transmitted signals x_0 to x_{N-1} are modulated by 64-QAM. In this case, there are 64 symbol replicas for each transmitted signal. Then, since only the transmitted signal x_{N-1} is associated with the signal z_{N-1} , the receiving apparatus first calculates the metrics for the 64 symbol replicas $c_{N-1,0}$ to $c_{N-1,63}$ corresponding to the transmitted signal x_{N-1} . Suppose that the symbol replicas corresponding to the three metrics selected in increasing order of the metrics are $C_{N-1,a}$, $C_{N-1,b}$, and $C_{N-1,c}$ (where $0 \leq a, b, c \leq 63$ and $a \neq b \neq c$). In this case, the receiving apparatus selects only the three symbol replicas $C_{N-1,a}$, $C_{N-1,b}$, and $C_{N-1,c}$ for the transmitted signal x_{N-1} when calculating the metrics for the signal z_{N-2} . Then, the receiving apparatus calculates the metric for each symbol replica set made up of one of the three symbol replicas $C_{N-1,a}$, $C_{N-1,b}$, and $C_{N-1,c}$ and one of the 64 symbol replicas $c_{N-2,0}$ to $c_{N-2,63}$ that the transmitted signal x_{N-2} can take. Since there is no need to calculate the metrics for all the symbol replica sets, the receiving apparatus using QRM-MLD can reduce the amount of computation.

Japanese Laid-Open Patent Publication No. 2006-121348 discloses a technique in which a decision on symbol candidates for a plurality of transmitted signals is made by separately applying the QRM-MLD method to received signals arranged in two different orders and, based on the result of the decision, outputs a plurality of symbol candidates and their likelihood.

K. Higuchi, H. Kawai, N. Maeda, and M. Sawahashi teach an Adaptive Selection of Surviving Symbol replica candidates based on maximum reliability (ASESS) method that can further reduce the number of metric calculations compared with QRM-MLD. In the ASESS method, the receiving apparatus obtains residual received signals at each metric calculation stage by subtracting the signal components of the surviving symbol replica candidates from the received signals obtained by QR-decomposing the channel matrix and thus orthogonalizing the transmitted signals. Then, based on the residual received signals, the symbol replica candidates for which the branch metrics are to be calculated are ranked by the receiving apparatus in increasing order of the expected branch metrics. The receiving apparatus then calculates the branch metrics in sequence starting from the highest ranking symbol replica candidate, and allows only the symbol replica candidates whose branch metrics are smaller than a predetermined threshold value to survive. The ranking of the symbol replica candidates is determined by detecting the quadrant to which the residual received signals belong.

On the other hand, in the Layered Orthogonal Lattice Detector (LORD) method proposed by M. Siti and M. P. Fitz and in the method disclosed in Japanese Laid-Open Patent Publication No. 2009-33636, the receiving apparatus applies QR decomposition to a first channel matrix. Then, based on the upper triangular matrix and unitary matrix obtained by the QR decomposition, the receiving apparatus calculates the metric when some of the plurality of transmitted signals are of a prescribed value. Further, the receiving apparatus generates a second channel matrix by interchanging the order of the channels in the first channel matrix. Then, based on the upper triangular matrix and signal vector Z' obtained by the QR decomposition of the second channel matrix, the receiving apparatus calculates the metric when some other ones of the plurality of transmitted signals are of a prescribed value. The receiving apparatus then estimates the transmitted signals by determining a set of symbol replicas based on the metric obtained for the first channel matrix and the metric obtained for the second channel matrix.

SUMMARY

However, in any of the above prior art methods, a large amount of computation has to be performed to estimate the transmitted signals, because each method involves gradually reducing the number of transmitted signal candidate sets while calculating the metrics for a plurality of transmitted signal candidate sets. As a result, if these computations are to be performed without reducing the communication speed, the amount of computing circuitry has to be increased. If the amount of computing circuitry increases, it becomes difficult to reduce the size of mobile apparatus such as a mobile phone if the MIMO technology is to be applied to such mobile apparatus. Furthermore, since the power consumed by the computing circuitry increases with increasing amount of computation, it is preferable to reduce the amount of computation for battery-driven receiving apparatus such as mobile terminals.

According to one embodiment, there is provided a communication apparatus. The communication apparatus includes: a plurality of antennas; a plurality of receiving units which are each coupled to one of the plurality of antennas, and which respectively acquire received signals by receiving, via the coupled antennas, a plurality of signals transmitted from a transmitting apparatus having a plurality of antennas; a candidate group setting unit which, based on a first channel matrix describing a communication channel between the plu-

5

ality of transmitted signals and the plurality of received signals, calculates a first residual component by canceling a component corresponding to a candidate or candidates for a first other transmitted signal or signals other than a first transmitted signal among the plurality of transmitted signals from a first signal corresponding to at least one of the plurality of received signals and having components corresponding to all of the plurality of transmitted signals, determines a candidate for the first transmitted signal by selecting a value closest to the first residual component from among values that the first transmitted signal can take, and constructs a first candidate group as a collection of candidate sets each comprising a candidate for the first transmitted signal and a candidate or candidates for the first other transmitted signal or signals, and which, based on a second channel matrix describing a communication channel between the plurality of transmitted signals and the plurality of received signals, calculates a second residual component by canceling a component corresponding to a candidate or candidates for a second other transmitted signal or signals other than a second transmitted signal among the plurality of transmitted signals from a second signal corresponding to at least one of the plurality of received signals and having components corresponding to all of the plurality of transmitted signals, determines a candidate for the second transmitted signal by selecting a value closest to the second residual component from among values that the second transmitted signal can take, and constructs a second candidate group as a collection of candidate sets each comprising a candidate for the second transmitted signal and a candidate or candidates for the second other transmitted signal or signals; a common group searching unit which constructs a common group by selecting any transmitted signal candidate set that is common between the first candidate group and the second candidate group; a metric calculating unit which, for each transmitted signal candidate set contained in the common group, computes an estimated received signal set corresponding to the transmitted signal candidate set, and calculates a distance between the estimated received signal set and the plurality of received signals; and a signal estimating unit which estimates that the transmitted signal candidate set that minimizes the distance represents the set of the plurality of transmitted signals.

The object and advantages of the invention will be realized and attained by means of the elements and combinations particularly pointed out in the claims.

It is to be understood that both the foregoing general description and the following detailed description are exemplary and explanatory and are not restrictive of the invention, as claimed.

BRIEF DESCRIPTION OF DRAWINGS

FIG. 1 is a diagram schematically illustrating the configuration of a communication system which includes a receiving apparatus according to a first embodiment.

FIG. 2 is a diagram schematically illustrating the configuration of a stream demultiplexer incorporated in the receiving apparatus according to the first embodiment.

FIGS. 3A to 3C are diagrams each depicting the relationship between an estimate of a transmitted signal x_0 and the quadrant to which the estimate belongs.

FIG. 4 is a conceptual diagram illustrating two candidate groups and the transmitted signal candidate sets common to the two groups.

FIG. 5 is a diagram depicting inverted bit symbols when, for each inverted bit, a symbol that is closest to the most likely bit is selected as the inverted bit symbol.

6

FIG. 6 is a diagram depicting inverted bit symbols when, for each inverted bit, symbols that are closest and second closest to the most likely bit are selected as the inverted bit symbols.

FIGS. 7A and 7B are an operation flowchart illustrating a transmitted signal demultiplexing process.

FIG. 8 is an operation flowchart illustrating the transmitted signal demultiplexing process.

FIG. 9 is a diagram schematically illustrating the configuration of a stream demultiplexer in a receiving apparatus according to a second embodiment.

FIGS. 10A and 10B are diagrams depicting an example of the positional relationship between an estimate v_1 of a transmitted signal x_1 and symbol replicas.

FIGS. 11A and 11B are an operation flowchart illustrating a transmitted signal demultiplexing process according to the second embodiment, which is performed instead of the transmitted signal demultiplexing process of steps S101 to S110 illustrated in FIGS. 7A and 7B.

FIG. 12 is a diagram schematically illustrating the configuration of a stream demultiplexer in a receiving apparatus according to a third embodiment.

FIG. 13 is a diagram depicting one example of a candidate group.

FIG. 14 is a diagram schematically illustrating the configuration of a stream demultiplexer in a receiving apparatus according to a fourth embodiment.

FIG. 15 is a diagram schematically illustrating the configuration of a base station apparatus in which the receiving apparatus according to any one of the embodiments is incorporated.

FIG. 16 is a diagram schematically illustrating the configuration of a mobile station apparatus in which the receiving apparatus according to any one of the embodiments is incorporated.

DESCRIPTION OF THE EMBODIMENTS

A receiving apparatus according to one embodiment will be described below with reference to the drawings. Using MIMO technology, the receiving apparatus receives, via a plurality of antennas, a plurality of signals transmitted from a transmitting apparatus having a plurality of antennas. The receiving apparatus then demultiplexes the transmitted signals from the signals received by the respective antennas. To demultiplex the transmitted signals, the receiving apparatus obtains two channel matrices by interchanging the order of the channels between them. Then, the receiving apparatus obtains sets of transmitted signal candidates for each channel matrix. The receiving apparatus determines one of the plurality of transmitted signal candidates as being a symbol replica closest to the residual component calculated by canceling the component corresponding to the other transmitted signal candidate from the unitary transformed signal of the received signal having components relating to all of the transmitted signals. The receiving apparatus calculates the metrics only for the candidate sets common to the two groups of transmitted signal candidate sets obtained for the two channel matrices, thus reducing the number of metric calculations each of which involves a large amount of computation.

FIG. 1 is a diagram schematically illustrating the configuration of a communication system 1 which includes a receiving apparatus 3 according to a first embodiment. The communication system 1 includes a transmitting apparatus 2 equipped with two antennas 21-1 and 21-2, as well as the receiving apparatus 3 which is also equipped with two antennas 31-1 and 31-2. The transmitting apparatus 2 radiates

transmitted signals as radio signals simultaneously from the respective antennas **21-1** and **21-2**. On the other hand, the receiving apparatus **3** receives the transmitted signals from the transmitting apparatus **2** by the respective antennas **31-1** and **31-2**. The signals received by the respective antennas **31-1** and **31-2** will hereinafter be referred to as the received signals. The receiving apparatus **3** recovers the transmitted signals based on each received signal.

In the present embodiment, the number of antennas mounted on the transmitting apparatus **2** is only illustrative, and may be set to any number not smaller than 2 but not larger than the number that can be physically mounted on the transmitting apparatus **2**. Similarly, the number of antennas mounted on the receiving apparatus **3** is only illustrative, and may be set to any number not smaller than 2 but not larger than the number that can be physically mounted on the receiving apparatus **3**. Further, the number of antennas mounted on the transmitting apparatus **2** may be made different from the number of antennas mounted on the receiving apparatus **3**.

The transmitting apparatus **2** includes, in addition to the two antennas **21-1** and **21-2**, a codeword generating unit **22**, an encoding unit **23**, a modulation unit **24**, two transmitting units **25-1** and **25-2**, and a control unit **26**. The codeword generating unit **22**, the encoding unit **23**, the modulation unit **24**, the transmitting units **25-1** and **25-2**, and the control unit **26** may be provided as separate circuits or may be implemented together on a single integrated circuit for mounting in the transmitting apparatus **2**.

The codeword generating unit **22** splits transmit data into codewords each having a length defined by the transport block size (TBS) determined by the control unit **26**. The codeword is, for example, MAC-PDU data that conforms to the media access control (MAC) layer and the protocol data unit (PDU) layer. The codeword generating unit **22** assigns the generated codewords to the encoding unit **23** by referring to the number of streams determined by the control unit **26** for each of the codewords to be encoded by the encoding unit **23**. The number of streams represents the number of data to be transmitted simultaneously for one codeword. The codeword generating unit **22** passes the generated codewords to the encoding unit **23**.

The encoding unit **23** applies error correction coding, such as convolutional coding or Turbo coding, to the codewords received from the codeword generating unit **22**. Further, the encoding unit **23** generates data streams by splitting each encoded codeword in accordance with the number of streams determined by the control unit **26**. Then, the encoding unit **23** supplies the encoded codewords on a stream-by-stream basis to the modulation unit **24**.

The modulation unit **24** quadrature-modulates the data streams received from the encoding unit **23** in accordance with the modulation mode MOD determined by the control unit **26**. The modulation unit **24** supplies each data stream to one of the transmitting units **25-1** and **25-2** in accordance with the precoding matrix determined by the control unit **26**.

The transmitting units **25-1** and **25-2** each generate a transmit signal by superimposing the data stream supplied from the modulation unit **24** onto a carrier wave having a radio frequency. Each of the transmitting units **25-1** and **25-2** has a high-power amplifier. Each of the transmitting units **25-1** and **25-2** thus amplifies the strength of the transmit signal to a desired level. The transmitting units **25-1** and **25-2** are coupled to the antennas **21-1** and **21-2**, respectively, and transmit out the signals via the respective antennas.

The control unit **26** controls the entire operation of the transmitting apparatus **2**. The control unit **26** determines the codeword length, the modulation mode, the number of

streams for each codeword, and the precoding matrix, for example, by referring to the feedback information received from the receiving apparatus **3**. Then, the control unit **26** sends information such as the codeword length, the modulation mode, etc. to the corresponding units in the transmitting apparatus **2**. The feedback information includes, for example, a CQI value which indicates the quality of the signal received by the receiving apparatus **3**. The control unit **26** here can demodulate and decode the signal received from the receiving apparatus **3** via a receiving unit (not shown) coupled to one of the antennas and can extract the feedback information from the decoded signal.

Next, the receiving apparatus **3** according to the first embodiment will be described. The receiving apparatus **3** includes, in addition to the two antennas **31-1** and **31-2**, two receiving units **32-1** and **32-2**, a demodulation unit **33**, a decoding unit **36**, and a data combining unit **37**. The receiving units **32-1** and **32-2**, the demodulation unit **33**, the decoding unit **36**, and the data combining unit **37** may be provided as separate circuits or may be implemented together on a single integrated circuit for mounting in the receiving apparatus **3**.

The receiving units **32-1** and **32-2** are coupled to the antennas **31-1** and **31-2**, respectively. The receiving units **32-1** and **32-2** receive via the respective antennas **31-1** and **31-2** the transmit signals transmitted from the antennas **21-1** and **21-2** of the transmitting apparatus **2**. Each of the receiving units **32-1** and **32-2** has a low-noise amplifier which amplifies the received signal. Each of the receiving units **32-1** and **32-2** converts the frequency of the received signal into the base-band frequency by superimposing a signal having an intermediate frequency on the amplified received signal, and supplies the thus converted received signal to the demodulation unit **33**.

From the signals received from the receiving units **32-1** and **32-2**, the demodulation unit **33** demultiplexes the signals transmitted out from the respective antennas of the transmitting apparatus **2**. For this purpose, the demodulation unit **33** includes a channel estimator **34** and a stream demultiplexer **35**.

The channel estimator **34** obtains a channel matrix defining the relationship between the transmitted signals and the received signals. For example, the channel estimator **34** obtains the channel impulse response value of a signal known to the transmitting apparatus **2** and the receiving apparatus **3**, such as a pilot signal contained in the signal transmitted out from each antenna of the transmitting apparatus **2**. Then, the channel estimator **34** sets the channel impulse response value as an element in the channel matrix. In this case, the relationship between the transmitted signals and the received signals is expressed by the following equation using the channel matrix.

$$Y = HX + n \quad (4)$$

$$\begin{pmatrix} y_0 \\ y_1 \end{pmatrix} = \begin{pmatrix} h_{00} & h_{01} \\ h_{10} & h_{11} \end{pmatrix} \begin{pmatrix} x_0 \\ x_1 \end{pmatrix} + \begin{pmatrix} n_0 \\ n_1 \end{pmatrix}$$

where x_0 and x_1 represent the signals transmitted out from the respective antennas **21-1** and **21-2**. The transmitted signal vector X is a vector whose elements are the transmitted signals x_0 and x_1 . On the other hand, y_0 and y_1 represent the signals received via the respective antennas **31-1** and **31-2**. The received signal vector Y is a vector whose elements are the received signals y_0 and y_1 . The matrix H indicates the channel matrix whose elements h_{ij} are each obtained, for

example, as a channel impulse response to a pilot signal, as described above. The vector n indicates the noise vector whose elements n_0 and n_1 represent the noise components contained in the signals received by the respective antennas **31-1** and **31-2**. The ordering of the channels is not limited to the above example. For example, the transmitted signals x_0 and x_1 may be the signals transmitted out from the antennas **21-2** and **21-1**, respectively, and y_0 and y_1 may be the signals received via the antennas **31-2** and **31-1**, respectively. The channel estimator **34** passes the channel matrix to the stream demultiplexer **35**.

Based on the channel matrix, the stream demultiplexer **35** demultiplexes the transmitted signals from the received signals. The details of the stream demultiplexer **35** will be described later.

The demodulation unit **33** demodulates the demultiplexed transmitted signals in accordance with the modulation scheme applied to the transmitted signals, and passes the demodulated signals to the decoding unit **36**. Further, the demodulation unit **33** computes the feedback information such as CQI value, etc., to be fed back to the transmitting apparatus **2**, and passes the feedback information to a transmitting unit not shown. The transmitting unit generates a radio signal by quadrature-modulating the feedback-information carrying signal and superimposing it onto a carrier wave having a radio frequency. The transmitting unit radiates the feedback-information carrying radio signal from one of the antennas.

The decoding unit **36** reconstructs each encoded codeword by combining the data streams received from the demodulation unit **33**. Then, the decoding unit **36** applies error correction decoding to each encoded codeword. The decoding unit **36** supplies the thus decoded codewords to the data combining unit **37**.

The data combining unit **37** recovers the original data by combining the codewords received from the decoding unit **36**. The data combining unit **37** supplies the thus recovered original data to other component elements of the receiving apparatus **3**.

The details of the stream demultiplexer **35** will be described below. FIG. 2 is a diagram schematically illustrating the configuration of the stream demultiplexer **35**. The stream demultiplexer **35** includes a channel interchanging unit **41**, a QR-decomposition unit **42**, a candidate group setting unit **43**, a common group searching unit **44**, a metric calculating unit **45**, a minimum value searching unit **46**, an additional metric calculating unit **47**, and a logarithmic likelihood ratio computing unit **48**. These units constituting the stream demultiplexer **35** may be implemented as separate computing circuits. Alternatively, these units constituting the stream demultiplexer **35** may be integrated into a single computing circuit implementing the functions of the respective units.

The channel interchanging unit **41** creates a transformed channel matrix H' by interchanging the order of the columns in the channel matrix H . The relationship between the transmitted signals and the received signals, using the transformed channel matrix H' , is expressed by the following equation.

$$Y = H'X' + n \quad (5)$$

$$\begin{pmatrix} y_0 \\ y_1 \end{pmatrix} = \begin{pmatrix} h_{01} & h_{00} \\ h_{11} & h_{10} \end{pmatrix} \begin{pmatrix} x_1 \\ x_0 \end{pmatrix} + \begin{pmatrix} n_0 \\ n_1 \end{pmatrix}$$

The channel interchanging unit **41** passes the transformed channel matrix H' to the QR-decomposition unit **42**.

The QR-decomposition unit **42** includes a first QR-decomposition unit **421** and a second QR-decomposition unit **422**. The first QR-decomposition unit **421** QR-decomposes the channel matrix H received from the channel estimator **35** into a unitary matrix Q and an upper triangular matrix R . The channel matrix H is expressed as shown in the following equation by using the unitary matrix Q and the upper triangular matrix R .

$$H = QR \quad (6)$$

$$\begin{pmatrix} h_{00} & h_{01} \\ h_{10} & h_{11} \end{pmatrix} = \begin{pmatrix} q_{00} & q_{01} \\ q_{10} & q_{11} \end{pmatrix} \begin{pmatrix} r_{00} & r_{01} \\ 0 & r_{11} \end{pmatrix}$$

Then, the first QR-decomposition unit **421** multiplies both sides of equation (4) from the left by the Hermitian conjugate Q^H of the unitary matrix. In this way, the first QR-decomposition unit **421** obtains the unitary transformed vector z by unitary-transforming the received signal vector Y . The relationship between the unitary transformed vector z , the upper triangular matrix R , and the transmitted signal vector X is expressed by the following equation.

$$z = Q^H Y = Q^H Q R X + Q^H n = R X + Q^H n \quad (7)$$

$$\begin{pmatrix} z_0 \\ z_1 \end{pmatrix} = \begin{pmatrix} r_{00} & r_{01} \\ 0 & r_{11} \end{pmatrix} \begin{pmatrix} x_0 \\ x_1 \end{pmatrix} + \begin{pmatrix} q_{00}^* & q_{10}^* \\ q_{01}^* & q_{11}^* \end{pmatrix} \begin{pmatrix} n_0 \\ n_1 \end{pmatrix}$$

where unitary transformed signals z_0 and z_1 are the elements of the unitary transformed vector z and each have components relating to the received signals y_0 and y_1 .

The second QR-decomposition unit **422** QR-decomposes the transformed channel matrix H' received from the channel interchanging unit **41** into a unitary matrix Q' and an upper triangular matrix R' . The channel matrix H' is expressed as shown in the following equation by using the unitary matrix Q' and the upper triangular matrix R' .

$$H' = Q' R' \quad (8)$$

$$\begin{pmatrix} h_{01} & h_{00} \\ h_{11} & h_{10} \end{pmatrix} = \begin{pmatrix} q'_{00} & q'_{01} \\ q'_{10} & q'_{11} \end{pmatrix} \begin{pmatrix} r'_{00} & r'_{01} \\ 0 & r'_{11} \end{pmatrix}$$

Then, as in the first QR-decomposition unit **421**, the second QR-decomposition unit **422** multiplies both sides of equation (5) from the left by the Hermitian conjugate Q'^H of the unitary matrix. In this way, the second QR-decomposition unit **422** obtains the unitary transformed vector z' by unitary-transforming the received signal vector Y . The relationship between the unitary transformed vector z' , the upper triangular matrix R' , and the transmitted signal vector X' is expressed by the following equation.

$$z' = Q'^H Y = Q'^H Q' R' X + Q'^H n = R' X + Q'^H n \quad (9)$$

$$\begin{pmatrix} z'_0 \\ z'_1 \end{pmatrix} = \begin{pmatrix} r'_{00} & r'_{01} \\ 0 & r'_{11} \end{pmatrix} \begin{pmatrix} x_1 \\ x_0 \end{pmatrix} + \begin{pmatrix} q'_{00}^* & q'_{10}^* \\ q'_{01}^* & q'_{11}^* \end{pmatrix} \begin{pmatrix} n_0 \\ n_1 \end{pmatrix}$$

11

where unitary transformed signals z'_0 and z'_1 are the elements of the unitary transformed vector z' and each have components relating to the received signals y_0 and y_1 .

The first and second QR-decomposition units **421** and **422** can perform the QR decomposition by using such techniques as a Givens rotation, a Householder transformation, or a Gram-Schmidt decomposition. The QR-decomposition unit **42** passes the unitary transformed vectors z and z' and the upper triangular matrices R and R' to the candidate group setting unit **43**.

The candidate group setting unit **43** includes a first candidate group setting unit **431** and a second candidate group setting unit **432**.

The first candidate group setting unit **431** obtains a candidate set for transmitted signals by using the unitary transformed vector z and upper triangular matrix R calculated based on the channel matrix H . Referring to equation (7), it is seen that the unitary transformed signal z_0 contains the components of both transmitted signals x_0 and x_1 . Therefore, based on the expression relating to the unitary transformed signal z_0 in equation (7), the first candidate group setting unit **431** obtains as an estimate of the transmitted signal x_0 the residual component calculated by canceling the component relating to the candidate for the transmitted signal x_1 from the unitary transformed signal z_0 . Then, the first candidate group setting unit **431** obtains a pair made up of a given candidate c_{1i} for the transmitted signal x_1 and the value that is closest, among the values that the transmitted signal x_0 can take, to the estimate of the transmitted signal x_0 when the transmitted signal x_1 is represented by that given candidate, and sets this pair as the transmitted signal candidate set.

When the transmitted signal x_1 is c_{1i} ($i=0, 1, \dots, m_1=1$), the estimate u_{0i} of the transmitted signal x_0 is expressed by the following equation. Here, c_{1i} is a symbol replica which is generated by the receiving apparatus **3** as one of the possible signal values that the transmitted signal x_1 can take in the modulation scheme applied to the transmitted signal x_1 . Here, c_{1i} is expressed by a combination of a real (I) signal and an imaginary (Q) signal. On the other hand, m_1 represents the number of values that can be taken in the modulation scheme applied to the transmitted signal x_1 . For example, if the modulation scheme is 16-QAM, $m_1=16$, and if the modulation scheme is 64-QAM, $m_1=64$.

$$u_{0i} = \frac{z_0 - r_{01}c_{1i}}{r_{00}} \quad (10)$$

The first candidate group setting unit **431** detects, for example, the quadrant to which the estimate u_{0i} belongs, in order to determine the candidate for the transmitted signal x_0 that is closest to the estimate u_{0i} .

The quadrant detection will be described with reference to FIGS. 3A to 3C. As an example, it is assumed that the modulation scheme applied to the transmitted signal x_0 is 64-QAM. In FIGS. 3A to 3C, the abscissa represents the I signal component, and the ordinate represents the Q signal component. Points **301** are the signal points corresponding to the signal values that the transmitted signal x_0 can take. For example, point **301a** represents the signal value corresponding to symbol "101111". Asterisk **310** indicates the estimate u_{0i} obtained by substituting the symbol replica c_{1i} into equation (10). In the illustrated example, the I and Q signal components of the estimate u_{0i} are both negative values.

As depicted in FIG. 3A, the estimate u_{0i} is located in the third quadrant **320** because the I and Q signal components are

12

both negative values. Accordingly, the first candidate group setting unit **431** estimates that the transmitted signal x_0 is represented by one of the signal values belonging to the third quadrant.

Next, the first candidate group setting unit **431** detects the quadrant to which the estimate u_{0i} belongs in a coordinate plane that has its origin O' at a point represented by a signal value $(-4/\sqrt{42}, -4/\sqrt{42})$ corresponding to the center of the third quadrant to which the estimate u_{0i} belongs. That is, the first candidate group setting unit **431** obtains an estimate u'_{0i} by subtracting from the estimate u_{0i} the signal value $(-4/\sqrt{42}, -4/\sqrt{42})$ corresponding to the center of the third quadrant, and checks whether the I and Q signal components of the estimate u'_{0i} are positive or negative. In the illustrated example, the estimate u_{0i} is located in the first quadrant **330** of the plane centered at the origin O' , as depicted in FIG. 3B. Accordingly, the first candidate group setting unit **431** estimates that the transmitted signal x_0 is represented by one of the signal values belonging to the first quadrant **330** of the plane centered at the origin O' .

The first candidate group setting unit **431** repeats the above quadrant detection process until the signal value closest to the estimate u_{0i} is found. In the illustrated example, the first candidate group setting unit **431** detects the quadrant to which the estimate u_{0i} belongs in a coordinate plane that has its origin O'' at a point represented by a signal value $(-2/\sqrt{42}, -2/\sqrt{42})$ corresponding to the center of the first quadrant **330** to which the estimate u_{0i} belongs in the plane centered at the origin O' . That is, the first candidate group setting unit **431** obtains an estimate u''_{0i} by subtracting from the estimate u_{0i} the signal value $(-2/\sqrt{42}, -2/\sqrt{42})$ corresponding to the center of the first quadrant **330**, and checks whether the I and Q signal components of the estimate u''_{0i} are positive or negative. As depicted in FIG. 3C, the estimate u_{0i} is located in the second quadrant **340** of the plane centered at the origin O'' . The second quadrant **340** corresponds to one symbol "110001". Therefore, the signal value corresponding to the symbol "110001" is the closest to the estimate u_{0i} .

Then, when the transmitted signal x_1 is c_{1i} , the first candidate group setting unit **431** sets the signal value corresponding to the symbol "110001" as the candidate for the transmitted signal x_0 . Hereinafter, the candidate for the transmitted signal x_0 thus set when the transmitted signal x_1 is c_{1i} is denoted by $x_0^{(min)}(c_{1i})$.

In this way, by using the quadrant detection, the first candidate group setting unit **431** can reduce the number of calculations, such as multiplications, that involve a larger amount of computation, and can thus reduce the amount of computation for finding $x_0^{(min)}(c_{1i})$.

When calculating the estimate u_{0i} in accordance with equation (10), an operation to divide $(z_0 - r_{01}c_{1i})$ by r_{00} is performed. In view of this, the first candidate group setting unit **431** may calculate the estimate u_{0i} as the numerator term $(z_0 - r_{01}c_{1i})$ on the right-hand side of equation (10), and may set the origin in the second and later quadrant detections by taking a point represented by a value obtained by multiplying by r_{00} the signal value corresponding to the center of the quadrant to which the estimate u_{0i} is detected to belong. Since this serves to reduce the number of division operations, the first candidate group setting unit **431** can reduce the amount of computation for finding $x_0^{(min)}(c_{1i})$.

By repeating the above process for each symbol replica c_{1i} ($i=0, 1, \dots, m_1-1$), the first candidate group setting unit **431** obtains a first candidate group ϕ_1 which is a collection of

13

candidate sets for the transmitted signals x_0 and x_1 . The first candidate group ϕ_1 is expressed as

$$\phi_1 = \{(x_0^{(min)}(c_{10}), c_{10}), (x_0^{(min)}(c_{11}), c_{11}), \dots, (x_0^{(min)}(c_{1m1-1}), c_{1m1-1})\}$$

The first candidate group ϕ_1 contains the same number of candidates as the number, m_1 , of values that can be taken in the modulation scheme applied to the transmitted signal x_1 .

Similarly to the first candidate group setting unit **431**, the second candidate group setting unit **432** obtains a set of candidates for the likely transmitted signals by using the unitary transformed vector z' and upper triangular matrix R' calculated based on the channel matrix H' . Referring to equation (9), it is seen that the element z'_0 in the unitary transformed vector contains the components of both transmitted signals x_0 and x_1 . Therefore, based on equation (9), the second candidate group setting unit **432** obtains as an estimate of the transmitted signal x_1 the residual component calculated by canceling the component of the transmitted signal x_0 from the unitary transformed signal z'_0 . Then, the second candidate group setting unit **432** obtains a pair made up of a given candidate c_{0i} for the transmitted signal x_0 and the value that is closest, among the values that the transmitted signal x_1 can take, to the estimate of the transmitted signal x_1 when the transmitted signal x_0 is represented by that given candidate, and sets this pair as the transmitted signal candidate set.

When the transmitted signal x_0 is a symbol replica c_{0i} ($i=0, 1, \dots, m_0-1$), the estimate u_{1i} of the transmitted signal x_1 is expressed by the following equation. Here, c_{0i} is a symbol replica of the transmitted signal x_0 . On the other hand, m_0 represents the number of values that can be taken in the modulation scheme applied to the transmitted signal x_0 .

$$u_{1i} = \frac{z'_0 - r'_{01}c_{0i}}{r'_{00}} \quad (11)$$

Similarly to the first candidate group setting unit **431**, the second candidate group setting unit **432** repeats the process for detecting the quadrant to which the estimate u_{1i} belongs, and determines the signal value of the symbol closest to the estimate u_{1i} as being the candidate for the transmitted signal x_1 when the transmitted signal x_0 is represented by c_{0i} . In the following, the candidate for the transmitted signal x_1 when the transmitted signal x_0 is c_{0i} is denoted by $x_1^{(min)}(c_{0i})$. Then, by determining the candidate for the transmitted signal x_1 for each symbol replica c_{0i} ($i=0, 1, \dots, m_0-1$), the second candidate group setting unit **432** obtains a second candidate group ϕ_2 which is a collection of candidate sets for the transmitted signals x_0 and x_1 . Here, the second candidate group ϕ_2 is expressed as

$$\phi_2 = \{(c_{00}, x_1^{(min)}(c_{00})), (c_{01}, x_1^{(min)}(c_{01})), \dots, (c_{0m0-1}, x_1^{(min)}(c_{0m0-1}))\}$$

The candidate group setting unit **43** passes the first and second candidate groups ϕ_1 and ϕ_2 to the common group searching unit **44** and the additional metric calculating unit **47**.

The common group searching unit **44** searches for the candidate sets of the transmitted signals x_0 and x_1 that are common to the first and second candidate groups ϕ_1 and ϕ_2 . The first and second candidate groups ϕ_1 and ϕ_2 are each a collection of candidate sets for the transmitted signals x_0 and x_1 and are obtained in accordance with different mathematical relations based on the same channel matrix. As a result, it is highly likely that the actually transmitted signal set is contained in both of the candidate groups. In view of this, the

14

common group searching unit **44** searches for the transmitted signal candidate sets that are contained in both of the two candidate groups and, using these candidate sets, constructs a common group on which metric calculations are to be performed.

FIG. **4** is a conceptual diagram illustrating the first and second candidate groups ϕ_1 and ϕ_2 and the candidate sets of the transmitted signals x_0 and x_1 that are common to the two groups. As an example, in FIG. **4**, both of the transmitted signals x_0 and x_1 are signals modulated by 64-QAM.

In FIG. **4**, the first and second candidate groups ϕ_1 and ϕ_2 each contain m transmitted signal candidate sets. Of these candidate sets, the candidate set **401** in the first candidate group ϕ_1 and the candidate set **411** in the second candidate group ϕ_2 both contain "010001" as the transmitted signal x_0 and "010100" as the transmitted signal x_1 . Therefore, the common group searching unit **44** selects ("010001", "010100") as the transmitted signal candidate set for the transmitted signals (x_0, x_1). Further, the candidate set **402** in the first candidate group ϕ_1 and the candidate set **412** in the second candidate group ϕ_2 both contain "111010" as the transmitted signal x_0 and "000101" as the transmitted signal x_1 . Therefore, the common group searching unit **44** also selects ("111010", "000101") as the transmitted signal candidate set for the transmitted signals (x_0, x_1). The common group searching unit **44** passes the thus constructed common group to the metric calculating unit **45**.

The number of transmitted signal candidate sets contained in the common group varies between 1 at minimum and $\min(m_0, m_1)$ at maximum, depending on channel variation or noise. Here, m_0 and m_1 each represent the number of values that the transmitted signal x_0 or x_1 , respectively, can take in the modulation scheme applied to the transmitted signals x_0 and x_1 . The function $\min(a, b)$ is a function that outputs a or b , whichever is smaller in value. Noting the estimate u_{0i} , the earlier given equation (10) can be rewritten as

$$u_{0i} = \frac{z_0 - r_{01}c_{1i}}{r_{00}} = \frac{z_0}{r_{00}} - \frac{|r_{01}|}{r_{00}} \cdot \frac{r_{01}}{|r_{01}|} c_{1i} \quad (12)$$

As can be seen from equation (12), the estimate u_{0i} corresponds to a signal point that is obtained by rotating c_{1i} by an amount equal to the phase $\arg(r_{01})$ of the average power $|r_{01}/r_{00}|^2$ centered at a point z_0/r_{00} . When the average power $|r_{01}/r_{00}|^2$ is small, i.e., when the interference of the transmitted signal x_1 to the transmitted signal x_0 is small, the estimate u_{0i} is located near the point z_0/r_{00} , regardless of the value of c_{1i} . As a result, the number of candidates for the transmitted signal x_0 is small. On the other hand, when the average power $|r_{01}/r_{00}|^2$ is large, i.e., when the interference of the transmitted signal x_1 to the transmitted signal x_0 is large, the estimate u_{0i} varies greatly, depending on c_{1i} . As a result, the number of candidates for the transmitted signal x_0 increases. Similarly, the estimate u_{1i} corresponds to a signal point that is obtained by rotating c_{0i} by an amount equal to the phase $\arg(r'_{01})$ of the average power $|r'_{01}/r'_{00}|^2$ centered at a point z'_0/r'_{00} . Accordingly, as the average power $|r'_{01}/r'_{00}|^2$ decreases, i.e., as the interference of the transmitted signal x_0 to the transmitted signal x_1 decreases, the number of candidates for the transmitted signal x_1 decreases. In this way, as the interference of one transmitted signal to the other transmitted signal decreases, the number of transmitted signal candidates decreases. More specifically, as the interference of one transmitted signal to the other transmitted signal decreases, the receiving apparatus **3** can further reduce the amount of computation needed to demultiplex the transmitted signals.

15

For each transmitted signal candidate set contained in the common group, the metric calculating unit 45 calculates a metric that indicates a measure of the likelihood of the transmitted signal candidate set representing the actually transmitted signal set. The metric indicates the distance between the actually received signals and the received signals estimated by assuming that one particular transmitted signal candidate set represents the actually transmitted signal set. For example, the metric calculating unit 45 calculates the metric d_j as shown in the following equation by taking the sum of the squared Euclidian distances calculated between the unitary transformed signals z_0 and z_1 and the estimated received signals obtained by substituting each transmitted signal candidate set (c_{0j}, c_{1j}) ($j=0, 1, \dots, k-1$) into the first term on the right-hand side of equation (7).

$$d_j = |z_1 - r_{11}c_{1j}|^2 + |z_0 - r_{01}c_{1j} - r_{00}c_{0j}|^2 \quad (13)$$

Here, k indicates the total number of transmitted signal candidate sets contained in the common group. The metric calculating unit 45 may use equation (9) instead of equation (7).

Alternatively, the metric calculating unit 45 may calculate the metric d_j as shown in the following equation by calculating the Manhattan distance between the unitary transformed signals z_0 and z_1 and the estimated received signals obtained by substituting each transmitted signal candidate set (c_{0j}, c_{1j}) into the first term on the right-hand side of equation (7).

$$d_j = |Re(z_1 - r_{11}c_{1j})| + |Im(z_1 - r_{11}c_{1j})| + |Re(z_0 - r_{01}c_{1j} - r_{00}c_{0j})| + |Im(z_0 - r_{01}c_{1j} - r_{00}c_{0j})| \quad (14)$$

The function $Re(\alpha)$ is a function that outputs the real component of a variable u , and the function $Im(\alpha)$ is a function that outputs the imaginary component of the variable α . Further, the metric calculating unit 45 may calculate as the metric some other measure that indicates the distance between the unitary transformed signals z_0 and z_1 and the transmitted signal candidate set (c_{0j}, c_{1j}) .

The metric calculating unit 45 passes each transmitted signal candidate set contained in the common group and its metric d_j to the minimum value searching unit 46.

The minimum value searching unit 46 is an example of a transmitted signal estimator, and finds the minimum value among the metrics d_j calculated for the transmitted signal candidates. The minimum value searching unit 46 then assumes that the transmitted signal candidate set (c_{0min}, c_{1min}) corresponding to the minimum value d_{min} of the metrics d_j represents the actually transmitted signal set (x_0, x_1) . Hereinafter, the transmitted signal candidate set (c_{0min}, c_{1min}) assumed to be the actually transmitted signal set (x_0, x_1) is referred to as the most likely symbol set, and the symbols $(x_0^{(ML)}, x_1^{(ML)})$ corresponding to the symbol replicas contained as the transmitted signal candidates in the most likely symbol set are called the most likely symbols.

The minimum value searching unit 46 passes the minimum value d_{min} and the most likely symbol set (c_{0min}, c_{1min}) to the logarithmic likelihood ratio computing unit 48. Further, the minimum value searching unit 46 passes each transmitted signal candidate set and the metric d_j calculated for each candidate set to the additional metric calculating unit 47.

For each of the most likely symbols, the additional metric calculating unit 47 detects, from among the symbols defined by inverting any one of the bits of the most likely symbol, any symbol that is located within a prescribed distance of the most likely symbol, and identifies such a symbol as an inverted bit symbol. Then, for the symbol replica x_{0p} corresponding to the inverted bit symbol s_{0p} ($p=1, 2, \dots, m$) obtained for the transmitted signal x_0 , the additional metric calculating unit 47 identifies the symbol replica $x_1^{(min)}(x_{0p})$ of the transmitted

16

signal x_1 that corresponds to the symbol replica x_{0p} . For example, the additional metric calculating unit 47 detects a candidate set containing the symbol replica x_{0p} from among the transmitted signal candidate sets contained in the second candidate group ϕ_2 . Then, based on the detected transmitted signal candidate set, the additional metric calculating unit 47 identifies the symbol replica $x_1^{(min)}(x_{0p})$ of the transmitted signal x_1 that corresponds to the symbol replica x_{0p} . Similarly, for the symbol replica x_{1p} corresponding to the inverted bit symbol s_{1p} obtained for the transmitted signal x_1 , the additional metric calculating unit 47 identifies the symbol replica $x_0^{(min)}(x_{1p})$ of the transmitted signal x_0 that corresponds to the symbol replica x_{1p} by referring to the first candidate group ϕ_1 .

The additional metric calculating unit 47 calculates an additional metric $d^{(additional)}$ between the unitary transformed signals z_0 and z_1 and the symbol replica set $(x_{0p}, x_1^{(min)}(x_{0p}))$ associated with the inverted bit symbol s_{0p} obtained for the transmitted signal x_0 . Similarly, the additional metric calculating unit 47 calculates an additional metric $d^{(additional)}$ between the unitary transformed signals z_0 and z_1 and the symbol replica set $(x_0^{(min)}(x_{1p}), x_{1p})$ associated with the inverted bit symbol s_{1p} obtained for the transmitted signal x_1 . The additional metric calculating unit 47 can calculate these additional metrics, for example, in accordance with equation (13) or (14). The additional metrics are used to compute the logarithmic likelihood ratio that the decoding unit 36 uses when performing error-correction decoding. Therefore, the additional metric calculating unit 47 passes the additional metric obtained for each inverted bit symbol to the logarithmic likelihood ratio computing unit 48.

If the metric d has already been calculated by the metric calculating unit 45 for one of the symbol replica sets $(x_0^{(min)}(x_{1p}), x_{1p})$ and $(x_{0p}, x_1^{(min)}(x_{0p}))$, the additional metric calculating unit 47 passes that metric d to the logarithmic likelihood ratio computing unit 48.

FIG. 5 is a diagram depicting the inverted bit symbols when, for each inverted bit, the closest symbol is selected as the inverted bit symbol, for example, for the case where the transmitted signal x_0 is modulated by 64-QAM and where the most likely symbol corresponding to the transmitted signal x_0 is "000000". As depicted in FIG. 5, the symbols located in blocks 501 to 506 are selected as the inverted bit symbols. For example, when the inverted bit is the rightmost bit, the symbol "000001" in block 501 is closest to the most likely bit. Therefore, "000001" is selected as the inverted bit symbol. On the other hand, when the inverted bit is the leftmost bit, the symbol "100010" in block 506, which is closest to the most likely symbol among the symbols whose leftmost bit is "1", is selected as the inverted bit symbol.

FIG. 6 is a diagram depicting the inverted bit symbols when, for each inverted bit, the closest symbol and the second closest symbol are selected as the inverted bit symbols for the case where the most likely symbol corresponding to the transmitted signal x_0 is "000000". As depicted in FIG. 6, the symbols located in blocks 601 to 614 are selected as the inverted bit symbols.

Since the position of the signal point corresponding to each symbol is predetermined, the inverted bit symbols for each most likely symbol can be determined in advance. Therefore, a reference table defining the corresponding inverted bit symbols for each most likely symbol may be stored in advance in a memory circuit incorporated in the additional metric calculating unit 47. The additional metric calculating unit 47 can then identify the inverted bit symbols corresponding to each most likely symbol by referring to the reference table.

The logarithmic likelihood ratio computing unit **48** computes the logarithmic likelihood ratio (LLR) for each bit. The logarithmic likelihood ratio computing unit **48** computes in accordance with the following equation the bit $LLR_r(n)$ which is the LLR for the n -th bit from the left of the transmitted signal x_r .

$$LLR_r(n) = \sqrt{d_{r,min}(b_n = 1)} - \sqrt{d_{r,min}(b_n = 0)} \quad (15)$$

$$d_{r,min}(b_n = \text{bit}(x_r^{(ML)}, n)) = d_{min} = d(x_0^{(ML)}, x_1^{(ML)})$$

$$d_{r,min}(b_n = \text{invbit}(x_r^{(ML)}, n)) =$$

$$\min \left[\begin{array}{l} \min_{\text{bit}(c_{0j}^{(common)}, n) = \text{invbit}(x_r^{(ML)}, n)} \{d(c_{0j}^{(common)}, c_{1j}^{(common)})\} \\ \min_{\text{bit}(x_{0p}^{(inv)}, n) = \text{invbit}(x_0^{(ML)}, n)} \{d^{(additional)}(x_{0p}^{(inv)}, x_{1p}^{(min)}(x_{0p}^{(inv)}))\} \\ \min_{\text{bit}(x_{1p}^{(inv)}, n) = \text{invbit}(x_1^{(ML)}, n)} \{d^{(additional)}(x_{0p}^{(min)}(x_{1p}^{(inv)}), x_{1p}^{(inv)})\} \end{array} \right]$$

where d_{min} is the metric calculated for the most likely symbol set $(x_0^{(ML)}, x_1^{(ML)})$. The function $\text{bit}(x_r^{(ML)}, n)$ indicates the value of the n -th bit from the left of the most likely symbol $x_r^{(ML)}$ ($r=0, 1$). On the other hand, the function $\text{invbit}(x_r^{(ML)}, n)$ indicates the inverted value of the n -th bit from the left of the most likely symbol $x_r^{(ML)}$ ($r=0, 1$). The function $\min_{a=b}(d)$ is a function that outputs a minimum value selected from among the metrics d that satisfy the condition $a=b$. Further, $d(c_{0j}^{(common)}, c_{1j}^{(common)})$ ($j=0, 1, \dots, k-1$) is the metric calculated for the transmitted signal candidate set $(c_{0j}^{(common)}, c_{1j}^{(common)})$ contained in the common group. On the other hand, $d^{(additional)}(x_{0p}^{(inv)}, x_{1p}^{(min)}(x_{0p}^{(inv)}))$ is the additional metric calculated for a pair made up of the inverted bit symbol $x_{0p}^{(inv)}$ of the most likely symbol $x_0^{(ML)}$ and the symbol $x_{1p}^{(min)}(x_{0p}^{(inv)})$ corresponding to that inverted bit symbol. Likewise, $d^{(additional)}(x_{0p}^{(min)}(x_{1p}^{(inv)}), x_{1p}^{(inv)})$ is the additional metric calculated for a pair made up of the inverted bit symbol $x_{1p}^{(inv)}$ of the most likely symbol $x_1^{(ML)}$ and the symbol $x_{0p}^{(min)}(x_{1p}^{(inv)})$ corresponding to that inverted bit symbol.

Alternatively, the logarithmic likelihood ratio computing unit **48** may compute the bit $LLR_r(n)$ in accordance with the following equation.

$$LLR_r(n) = d_{r,min}(b_n = 1) - d_{r,min}(b_n = 0) \quad (16)$$

The logarithmic likelihood ratio computing unit **48** passes each bit $LLR_r(n)$ and its corresponding inverted bit symbols to the decoding unit **36**.

If the logarithmic likelihood ratio is not used in the error-correction decoding process performed by the decoding unit **36**, the additional metric calculating unit **47** and the logarithmic likelihood ratio computing unit **48** may be omitted.

FIGS. 7A and 7B and FIG. 8 are operation flowcharts illustrating the transmitted signal demultiplexing process. The transmitted signal demultiplexing process is performed under control of the stream demultiplexer **35**, and is initiated each time the receiving apparatus **3** receives a signal.

The first QR-decomposition unit **421** in the QR-decomposition unit **42** QR-decomposes the channel matrix H into the unitary matrix Q and the upper triangular matrix R (step S101). Then, the first QR-decomposition unit **421** generates the unitary transformed vector z ($= (z_0, z_1)$) of the received signal vector Y by multiplying the received signal vector Y by the Hermitian conjugate Q^H of the unitary matrix Q (step S102). The first QR-decomposition unit **421** passes the uni-

tary transformed vector z and the upper triangular matrix R to the candidate group setting unit **43**.

For the particular transmitted signal x_0 , the first candidate group setting unit **431** in the candidate group setting unit **43** calculates the residual component by canceling the component relating to the symbol replica c_{1i} of the other transmitted signal x_1 from the unitary transformed signal z_0 and thus calculates the estimate u_{0i} of that particular transmitted signal x_0 (step S103). Here, the first candidate group setting unit **431** calculates the estimate u_{0i} for each symbol replica c_{1i} ($i=0, 1, 2, \dots, m_1-1$). Then, the first candidate group setting unit **431** generates a first candidate group of transmitted signal candidate sets, each designated as $(x_0^{(min)}(c_{1i}), c_{1i})$ and made up of the symbol replica $x_0^{(min)}(c_{1i})$ closest to the estimate u_{0i} and the corresponding symbol replica c_{1i} of the transmitted signal x_1 (step S104). The first candidate group setting unit **431** passes the first candidate group to the common group searching unit **44** and the additional metric calculating unit **47**.

As illustrated in FIG. 7B, the channel interchanging unit **41** creates the transformed channel matrix H' by interchanging the order of the columns in the channel matrix H (step S105). Then, the channel interchanging unit **41** passes the transformed channel matrix H' to the QR-decomposition unit **42**.

The second QR-decomposition unit **422** in the QR-decomposition unit **42** QR-decomposes the transformed channel matrix H' into the unitary matrix Q' and the upper triangular matrix R' (step S106). Then, the second QR-decomposition unit **422** generates the unitary transformed vector z' ($= (z'_0, z'_1)$) of the received signal vector Y by multiplying the received signal vector Y by the Hermitian conjugate Q'^H of the unitary matrix Q' (step S107). The second QR-decomposition unit **422** passes the unitary transformed vector z' and the upper triangular matrix R' to the candidate group setting unit **43**.

For the particular transmitted signal x_1 , the second candidate group setting unit **432** in the candidate group setting unit **43** calculates the residual component by canceling the component relating to the symbol replica c_{0i} of the other transmitted signal x_0 from the unitary transformed signal z'_0 and thus calculates the estimate u_{1i} of that particular transmitted signal x_1 (step S108). The second candidate group setting unit **432** calculates the estimate u_{1i} for each symbol replica c_{0i} ($i=0, 1, 2, \dots, m_0-1$). Then, the second candidate group setting unit **432** generates a second candidate group of transmitted signal candidate sets, each designated as $(c_{0i}, x_1^{(min)}(c_{0i}))$ and made up of the symbol replica $x_1^{(min)}(c_{0i})$ closest to the estimate u_{1i} and the corresponding symbol replica c_{0i} of the transmitted signal x_0 (step S109). The second candidate group setting unit **432** passes the second candidate group to the common group searching unit **44** and the additional metric calculating unit **47**.

The common group searching unit **44** searches for the transmitted signal candidate sets that are common between the first and second candidate groups (step S110). The common group searching unit **44** passes the common group containing the common transmitted signal candidate sets to the metric calculating unit **45**.

As illustrated in FIG. 8, for each transmitted signal candidate set contained in the common group, the metric calculating unit **45** calculates the metric for evaluating the distance between the received signal set and the estimated received signal set obtained based on the transmitted signal candidate set (step S111).

The minimum value searching unit **46** estimates that the transmitted signal candidates contained in the candidate set corresponding to the minimum metric value represent the actually transmitted signals (step S112). The minimum value

searching unit **46** passes the minimum metric value and the estimated transmitted signals to the logarithmic likelihood ratio computing unit **48**. The minimum value searching unit **46** also passes the estimated transmitted signals to the additional metric calculating unit **47**.

From among the symbols having inverted bits with respect to each most likely symbol, the additional metric calculating unit **47** selects as inverted bit symbols those symbols that are located within a prescribed distance of the most likely symbol (step **S113**). Then, the additional metric calculating unit **47** determines the symbol replica sets corresponding to the inverted bit symbols by referring to the first and second candidate groups (step **S114**). The additional metric calculating unit **47** calculates the metric for each inverted bit symbol (step **S115**). The additional metric calculating unit **47** passes the metrics and the inverted bit symbols to the logarithmic likelihood ratio computing unit **48**.

The logarithmic likelihood ratio computing unit **48** computes the logarithmic likelihood ratio for each inverted bit of each most likely symbol by calculating the difference between the square root of the minimum metric and the square root of the minimum value of the metric corresponding to the inverted bit symbol (step **S116**). Then, the logarithmic likelihood ratio computing unit **48** outputs the estimated transmitted signal, the logarithmic likelihood ratio, and the inverted bit symbol used for the computation of the logarithmic likelihood ratio.

After that, the stream demultiplexer **35** terminates the transmitted signal demultiplexing process. The stream demultiplexer **35** may perform the process from step **S101** to step **S104** in parallel with the process from step **S105** to step **S109**.

Table 1 provides a comparison between the number of metric calculations performed in the transmitted signal demultiplexing process according to the present embodiment and the number of metric calculations performed in the transmitted signal demultiplexing process according to the prior art, for the case where the two transmitted signals are both modulated by 64-QAM. In Table 1, it is assumed that the metric is calculated as the squared Euclidian distance in accordance with equation (13), and that one norm calculation equals one metric calculation. It is also assumed that the additional metric calculating unit **47** calculates the metric by selecting only the symbol closest to the most likely symbol as the inverted bit symbol for each inverted bit from among the symbols containing that inverted bit.

TABLE 1

COMPARISON OF NUMBER OF METRIC CALCULATIONS BETWEEN VARIOUS METHODS	
METHOD OF RECEPTION	NUMBER OF METRIC CALCULATIONS
METHOD OF PRESENT EMBODIMENT	26-128
QRM-MLD METHOD	4160
ASESS METHOD	128
LORD METHOD	256

According to the method of the present embodiment, the number of metric calculations is 26 at minimum and 128 at maximum. When there is only one transmitted signal candidate set that is common between the first and second candidate groups, the number of metric calculations becomes minimum. In this case, two metric calculations are performed for that common candidate set and, since there are \log_{264} (=6)

inverted bit symbols for each transmitted signal, 24 metric calculations are performed for the inverted bit symbols.

On the other hand, when there are 64 transmitted signal candidate sets that are common between the first and second candidate groups, that is, when the two candidate groups are equal, the number of metric calculations becomes maximum. In this case, 128 (=2×64) metric calculations are performed for the common candidate sets. The number of metric calculations for the inverted bit symbols is 0, since the transmitted signal sets containing the inverted bit symbols are contained in the common group.

As can be seen from Table 1, even when the number of metric calculations is maximum, the number of metric calculations according to the method of the present embodiment is smaller than the number of metric calculations according to any prior art transmitted signal demultiplexing method.

As has been described above, when demultiplexing the transmitted signals, the receiving apparatus according to the first embodiment obtains two channel matrices by interchanging the order of the channels between them. Then, the receiving apparatus obtains sets of transmitted signal candidates for each channel matrix. For each particular transmitted signal, the receiving apparatus determines the transmitted signal candidate by selecting the symbol replica that is closest to the residual component calculated by canceling the component corresponding to the other transmitted signal candidate from the unitary transformed signal of the received signal having components relating to all of the transmitted signals. The receiving apparatus estimates the transmitted signals by calculating the metrics only for the candidate sets common to the two groups of transmitted signal candidate sets obtained for the two channel matrices. In this way, since the receiving apparatus can determine each transmitted signal candidate set without calculating the metric that involves a large amount of computation, the number of metric calculations can be reduced. As a result, the receiving apparatus can reduce the amount of computation when demultiplexing the transmitted signals.

Next, a receiving apparatus according to a second embodiment will be described. When performing the transmitted signal demultiplexing process, the receiving apparatus according to the second embodiment allocates priorities to the transmitted signal candidate sets that are common between the first and second candidate groups, and calculates the metrics only for high priority candidate sets. The only difference between the receiving apparatus according to the second embodiment and the receiving apparatus according to the first embodiment lies in the stream demultiplexer. Therefore, the following description deals only with the stream multiplexer.

FIG. 9 is a diagram schematically illustrating the configuration of the stream demultiplexer **351** in the receiving apparatus according to the second embodiment. The stream demultiplexer **351** includes a channel interchanging unit **41**, a QR-decomposition unit **42**, a candidate group setting unit **43**, a common group searching unit **44**, a metric calculating unit **45**, a minimum value searching unit **46**, an additional metric calculating unit **47**, a logarithmic likelihood ratio computing unit **48**, and a ranking unit **51**.

These units constituting the stream demultiplexer **351** may be implemented as separate computing circuits. Alternatively, these units constituting the stream demultiplexer **351** may be integrated into a single computing circuit implementing the functions of the respective units.

In FIG. 9, the units constituting the stream demultiplexer **351** are designated by the same reference numerals as those used to designate the corresponding component elements of

21

the stream demultiplexer **35** according to the first embodiment depicted in FIG. 2. The stream demultiplexer **351** differs from the stream demultiplexer **35** according to the first embodiment by the inclusion of the ranking unit **51**.

The ranking unit **51** includes a first signal ranking unit **511** and a second signal ranking unit **512**.

The first signal ranking unit **511** calculates ranking values for prioritizing the transmitted signal candidate sets contained in the first candidate group. As shown in equation (7) defining the relationship between the unitary transformed vector z , the upper triangular matrix R , and the transmitted signal vector X , the transmitted signal x_1 is expressed as shown in the following equation by using the unitary transformed vector z_1 .

$$x_1 = \frac{z_1}{r_{11}} - \frac{q_{01}^* n_0 + q_{11}^* n_1}{r_{11}} \quad (17)$$

The first term (z_1/r_{11}) on the right-hand side of equation (17) indicates the estimate v_1 of the transmitted signal x_1 .

That is, if the noise component is small, then the closer to the estimate v_1 the signal value is, the more likely that the signal value represents the actually transmitted signal x_1 .

Therefore, the first signal ranking unit **511** determines the ranking value according to the closeness to the estimate v_1 for each of the symbol replicas c_{1i} corresponding to the signal values that the transmitted signal x_1 can take. For example, the first signal ranking unit **511** assigns a smaller ranking value to a signal value closer to the estimate v_1 . The ranking value is a measure of the likelihood that the signal value represents the transmitted signal x_1 . In the illustrated example, the smaller the ranking value, the greater the likelihood.

To determine the ranking value, the first signal ranking unit **511** detects the quadrant to which the estimate v_1 ($=z_1/r_{11}$) of the transmitted signal x_1 belongs in a coordinate system that defines the I and Q signals representing the signal values that the transmitted signal x_1 can take. Then, the first signal ranking unit **511** determines how close to the estimate v_1 each signal value is, by performing the quadrant detection iteratively a number $((1/2)\log_2 m_1)$ of times, each time by setting its origin at the center of the quadrant to which the estimate v_1 belongs. Here, m_1 represents the number of values that can be taken in the modulation scheme applied to the transmitted signal x_1 ; for example, when the modulation scheme is QPSK, $m_1=2$.

FIGS. **10A** and **10B** are diagrams depicting an example of the positional relationship between the estimate v_1 of the transmitted signal x_1 and the values that the transmitted signal x_1 can take. As an example, it is assumed that the modulation scheme applied to the transmitted signal x_1 is QPSK. In FIGS. **10A** and **10B**, the abscissa represents the I signal component, and the ordinate represents the Q signal component. Points **1001a** to **1001d** are the signal points corresponding to the signal values that the transmitted signal x_1 can take. For example, point **1001a** represents the signal value corresponding to the symbol “00”. On the other hand, point **1010** indicates the estimate v_1 . In the illustrated example, the I and Q signal components of the estimate v_1 are both positive values. As can be seen, of the four signal values, the signal value corresponding to the symbol “00” is closest to the estimate v_1 . On the other hand, the signal value corresponding to the symbol “11”, whose I and Q components are both different from those of the estimate v_1 , is farthest from the estimate v_1 .

22

Therefore, the first signal ranking unit **511** assigns, for example, a ranking value “1” to the symbol replica corresponding to the symbol “00” and a ranking value “4” to the symbol replica corresponding to the symbol “11”. As for the symbol replica corresponding to the symbol “01” and the signal value corresponding to the symbol “10”, it is not yet known, at the end of the first quadrant detection, which signal value is closer to the estimate v_1 . Therefore, the first signal ranking unit **511** assigns a ranking value “2” to both the symbol replica corresponding to the symbol “01” and the symbol replica corresponding to the symbol “10”.

The first signal ranking unit **511** may perform the quadrant detection iteratively more than $((1/2)\log_2 m_1)$ times. The first signal ranking unit **511** can then determine the order of closeness to the estimate v_1 for all the signal values.

For example, as depicted in FIG. **10B**, by performing the second quadrant detection on the estimate v_1 , it can be seen that the estimate v_1 is located in a region **1020** which is one of 16 regions. The region **1020** is nearer to the signal value corresponding to the symbol “01” than to the signal value corresponding to the symbol “10”. Accordingly, the first signal ranking unit **511** can determine that the signal value corresponding to the symbol “01” is closer to the estimate v_1 than the signal value corresponding to the symbol “10” is. Therefore, the first signal ranking unit **511** assigns the ranking values “1”, “2”, “3”, and “4”, respectively, to the symbol replicas corresponding to the respective symbols “00”, “01”, “10”, and “11”.

The second signal ranking unit **512** calculates ranking values for ranking the transmitted signal candidate sets contained in the second candidate group. Here, the second signal ranking unit **512**, similarly to the first signal ranking unit **511**, calculates (z'_1/r'_{11}) based on equation (9) and takes it as the estimate v_0 of the transmitted signal x_0 . Then, by detecting the quadrant to which the estimate v_0 belongs, the second signal ranking unit **512** determines the ranking value according to the closeness to the estimate v_0 for each of the symbol replicas c_{0i} corresponding to the signal values that the transmitted signal x_0 can take.

The ranking unit **51** passes to the candidate group setting unit **43** the ranking value R_{0i} assigned to each of the symbol replicas c_{0i} corresponding to the signal values that the transmitted signal x_0 can take and the ranking value R_{1i} assigned to each of the symbol replicas c_{1i} corresponding to the signal values that the transmitted signal x_1 can take.

The candidate group setting unit **43**, similarly to the candidate group setting unit **43** in the first embodiment, obtains the first and second candidate groups each made up of sets of candidates for the transmitted signals x_0 and x_1 .

The first candidate group setting unit **431** receives the ranking value R_{1i} assigned to the symbol replica c_{1i} contained in each of the transmitted signal candidate sets in the first candidate group, and takes it as the ranking value that indicates the degree of likelihood of that candidate set representing the actually transmitted signal set. Likewise, the second candidate group setting unit **432** receives the ranking value R_{0i} assigned to the symbol replica c_{0i} contained in each of the transmitted signal candidate sets in the second candidate group, and takes it as the ranking value that indicates the degree of likelihood of that candidate set representing the actually transmitted signal set.

The candidate group setting unit **43** passes the first and second candidate groups and the ranking values of the candidate sets contained in the respective candidate groups to the additional metric calculating unit **47**.

The common group searching unit **44** searches for the transmitted signal candidate sets that are common between

23

the first and second candidate groups, and constructs a common group using these common transmitted signal candidate sets. Then, the common group searching unit **44** allocates priorities according to the ranking values (R_{0i} and R_{1i}) assigned to the common transmitted signal candidate sets.

For example, the common group searching unit **44** allocates priority to each common transmitted signal candidate set by calculating the sum R_{sum} of the ranking values ($=R_{0i}+R_{1i}$). Then, the common group searching unit **44** selects a number, S , of candidate sets in decreasing order of priority, i.e., in increasing order of the sum R_{sum} of the ranking values.

Alternatively, the common group searching unit **44** may allocate priority to each common transmitted signal candidate set by calculating the product R_{pro} of the ranking values ($=R_{0i}*R_{1i}$). Then, the common group searching unit **44** may select a number, S , of candidate sets in increasing order of the product R_{pro} of the ranking values.

If the number of transmitted signal candidate sets contained in the common group is smaller than S , the common group searching unit **44** selects all of the transmitted signal candidate sets contained in the common group. Here, S is an integer not smaller than 1, and is chosen to be smaller than m_0 or m_1 , whichever is smaller, which represents the number of values that can be taken in the modulation scheme applied to the transmitted signal x_0 or x_1 . For example, when the modulation scheme applied to the transmitted signal x_0 or x_1 is 64-QAM, S is set, for example, to 16.

The common group searching unit **44** passes the selected transmitted signal candidate sets to the metric calculating unit **45**. The metric calculating unit **45** calculates the metrics only for the transmitted signal candidate sets selected by the common group searching unit **44**.

FIGS. 11A and 11B are an operation flowchart illustrating the transmitted signal demultiplexing process according to the second embodiment, which is performed instead of the transmitted signal demultiplexing process of steps S101 to S110 illustrated in FIGS. 7A and 7B. The transmitted signal demultiplexing process is performed under control of the stream demultiplexer **351**, and is initiated each time the receiving apparatus **3** receives a signal.

The first QR-decomposition unit **421** in the QR-decomposition unit **42** QR-decomposes the channel matrix H into the unitary matrix Q and the upper triangular matrix R (step S201). Then, the first QR-decomposition unit **421** generates the unitary transformed vector z ($=z_0, z_1$) of the received signal vector Y by multiplying the received signal vector Y by the Hermitian conjugate Q^H of the unitary matrix Q (step S202). The first QR-decomposition unit **421** passes the unitary transformed vector z and the upper triangular matrix R to the ranking unit **51** and the candidate group setting unit **43**.

The first signal ranking unit **511** in the ranking unit **51** determines the ranking value R_{1i} according to the closeness to the estimate v_1 ($=z_1/r_{11}$) of the transmitted signal x_1 for each of the symbol replicas c_{1i} representing the signal values that the transmitted signal x_1 can take (step S203). Then, the first signal ranking unit **511** passes the ranking value R_{1i} determined for each of the symbol replicas c_{1i} to the candidate group setting unit **43**.

For the particular transmitted signal x_0 , the first candidate group setting unit **431** in the candidate group setting unit **43** calculates the residual component by canceling the component relating to the symbol replica c_{1i} of the other transmitted signal x_1 from the unitary transformed signal z_0 and thus calculates the estimate u_{0i} of that particular transmitted signal x_0 (step S204). The first candidate group setting unit **431** calculates the estimate u_{0i} for each symbol replica c_{1i} ($i=0, 1, 2, \dots, m_1-1$). Then, the first candidate group setting unit **431**

24

generates a first candidate group of transmitted signal candidate sets, each designated as $(x_0^{(min)}(c_{1i}), c_{1i})$ and made up of the symbol replica $x_0^{(min)}(c_{1i})$ closest to the estimate u_{0i} and the corresponding symbol replica c_{1i} of that other transmitted signal x_1 (step S205). The first candidate group setting unit **431** receives the ranking value R_{1i} assigned to the symbol replica c_{1i} contained in each of the transmitted signal candidate sets in the first candidate group, and takes it as the ranking value for that candidate set. Then, the first candidate group setting unit **431** passes the first candidate group and the ranking values of the respective candidate sets contained in that group to the common group searching unit **44** and the additional metric calculating unit **47**.

The channel interchanging unit **41** creates the transformed channel matrix H' by interchanging the order of the columns in the channel matrix H (step S206). Then, the channel interchanging unit **41** passes the transformed channel matrix H' to the QR-decomposition unit **42**.

As illustrated in FIG. 11B, the second QR-decomposition unit **422** in the QR-decomposition unit **42** QR-decomposes the transformed channel matrix H' into the unitary matrix Q' and the upper triangular matrix R' (step S207). Then, the second QR-decomposition unit **422** generates the unitary transformed vector z' ($=z'_0, z'_1$) by multiplying the received signal vector Y by the Hermitian conjugate Q'^H of the unitary matrix Q' (step S208). The second QR-decomposition unit **422** passes the unitary transformed vector z' and the upper triangular matrix R' to the ranking unit **51** and the candidate group setting unit **43**.

The second signal ranking unit **512** in the ranking unit **51** determines the ranking value R_{0i} according to the closeness to the estimate v_0 ($=z'_1/r'_{11}$) of the transmitted signal x_0 for each of the symbol replicas c_{0i} representing the signal values that the transmitted signal x_0 can take (step S209). Then, the second signal ranking unit **512** passes the ranking value R_{0i} determined for each of the symbol replicas c_{0i} to the candidate group setting unit **43**.

For the particular transmitted signal x_1 , the second candidate group setting unit **432** calculates the residual component by canceling the component relating to the symbol replica c_{0i} of the other transmitted signal x_0 from the unitary transformed signal z'_0 and thus calculates the estimate u_{1i} of that particular transmitted signal x_1 (step S210). The second candidate group setting unit **432** calculates the estimate u_{1i} for each symbol replica c_{0i} ($i=0, 1, 2, \dots, m_0-1$). Then, the second candidate group setting unit **432** generates a second candidate group of transmitted signal candidate sets, each designated as $(c_{0i}, x_1^{(min)}(c_{0i}))$ and made up of the symbol replica $x_1^{(min)}(c_{0i})$ closest to the estimate u_{1i} and the corresponding symbol replica c_{0i} of that other transmitted signal x_0 (step S211). The second candidate group setting unit **432** receives the ranking value R_{0i} assigned to the symbol replica c_{0i} contained in each of the transmitted signal candidate sets in the second candidate group, and takes it as the ranking value for that candidate set. Then, the second candidate group setting unit **432** passes the second candidate group and the ranking values of the respective candidate sets contained in that group to the common group searching unit **44** and the additional metric calculating unit **47**.

The common group searching unit **44** searches for the transmitted signal candidate sets that are common between the first and second candidate groups, and constructs a common group using the common transmitted signal candidate sets (step S212). The common group searching unit **44** allocates priorities to the transmitted signal candidate sets contained in the common group according to the ranking values (R_{0i} and R_{1i}) assigned to the respective transmitted signal

candidate sets. Then, the common group searching unit **44** selects a predetermined number of candidate sets in decreasing order of priority (step **S213**). The common group searching unit **44** passes the thus selected transmitted signal candidate sets to the metric calculating unit **45**.

After that, the stream demultiplexer **351** proceeds to perform the process starting from step **S111** illustrated in FIG. **8**. The stream demultiplexer **351** may perform the process from step **S201** to step **S205** in parallel with the process from step **S206** to step **S211**.

In the second embodiment, the maximum number of transmitted signal candidates for which the metric is to be calculated is defined by the predetermined number S . That is, the number of metric calculations in the metric calculating unit **45** is $2S$ at maximum. On the other hand, the number of metric calculations in the additional metric calculating unit **47** is $(\log_2 m_0 + \log_2 m_1) \times 2$ at maximum. Here, m_0 and m_1 each represent the number of values that can be taken in the modulation scheme applied to the transmitted signal x_0 or x_1 , respectively. Accordingly, the maximum number of metric calculations in the second embodiment is given as $(2S + (\log_2 m_0 + \log_2 m_1) \times 2)$. For example, if the conditions for computing the number of metric calculations are the same as those provided in Table 1, and if S is set to 16, then the maximum number of metric calculations is 56. In this way, compared with the receiving apparatus according to the first embodiment, the receiving apparatus according to the second embodiment can further reduce the maximum number of metric calculations.

As described above, if the ranking value of any one of the symbol replicas c_{0i} and c_{1i} of the transmitted signals x_0 and x_1 is large, the priority of the transmitted signal candidate set concerned is low, and as a result, the metric is not calculated for such a candidate set. It is therefore preferable to reduce the amount of computation needed to obtain such a candidate set.

In view of the above, the first candidate group setting unit **431** may determine the transmitted signal candidate sets by performing the quadrant detection only on the symbol replicas c_{1i} whose ranking values calculated by the first ranking unit **51** fall within the Y_1 highest ranks. Similarly, the second candidate group setting unit **432** may determine the transmitted signal candidate sets by performing the quadrant detection only on the symbol replicas c_{0i} whose ranking values calculated by the second ranking unit **52** fall within the Y_0 highest ranks.

Since this serves to reduce the number of times that the quadrant detection is performed, the stream demultiplexer **351** can further reduce the total amount of computation in the transmitted signal demultiplexing process. For example, when the modulation scheme applied to the transmitted signals x_0 and x_1 is 64-QAM, and when $\sigma_0 = \Sigma_1 = 32$, the amount of computation in the quadrant detection process performed by the candidate group setting unit **43** can be reduced by a factor of 2, compared with the first and second embodiments.

On the other hand, if the modulation scheme applied to the transmitted signal x_0 differs from the modulation scheme applied to the transmitted signal x_1 , Y_0 and Σ_1 may be set to different values. For example, if the modulation scheme applied to the transmitted signal x_0 is 16-QAM, and the modulation scheme applied to the transmitted signal x_1 is 64-QAM, then Σ_0 is set to 8, while Σ_1 is set to 32. Alternatively, the values of Σ_0 and Σ_1 may be varied according to the modulation scheme applied to the transmitted signals x_0 and x_1 . For example, if the modulation scheme applied is QPSK, Σ_0 and Σ_1 are each set to 3; if the modulation scheme applied is 16-QAM, Σ_0 and Σ_1 are each set to 8; and if the modulation scheme applied is 64-QAM, Σ_0 and Σ_1 are each set to 32.

In the above modified example, since the transmitted signal candidate sets are not obtained for all of the values that the transmitted signals x_0 and x_1 can take, there can occur cases where neither the first candidate group nor the second candidate group contains any transmitted signal candidate sets corresponding to the inverted symbols. In view of this, if neither the first candidate group nor the second candidate group contains any transmitted signal candidate sets corresponding to the inverted symbols, the additional metric calculating unit **47** determines the transmitted signal candidate sets containing the inverted symbols by performing the same processing as the candidate group setting unit **43** does.

Next, a receiving apparatus according to a third embodiment will be described. In the receiving apparatus according to the third embodiment, when performing the transmitted signal demultiplexing process, one candidate group setting unit refers to the candidate group constructed by the other candidate group setting unit. Then, the one candidate group setting unit obtains the transmitted signal candidate sets only for the symbol replicas corresponding to the transmitted signal candidates contained in the candidate group referred to by it.

FIG. **12** is a diagram schematically illustrating the configuration of the stream demultiplexer **352** in the receiving apparatus according to the third embodiment. The stream demultiplexer **352** includes a channel interchanging unit **41**, a QR-decomposition unit **42**, a candidate group setting unit **43**, a common group searching unit **44**, a metric calculating unit **45**, a minimum value searching unit **46**, an additional metric calculating unit **47**, and a logarithmic likelihood ratio computing unit **48**.

These units constituting the stream demultiplexer **352** may be implemented as separate computing circuits. Alternatively, these units constituting the stream demultiplexer **352** may be integrated into a single computing circuit implementing the functions of the respective units.

In FIG. **12**, the units constituting the stream demultiplexer **352** are designated by the same reference numerals as those used to designate the corresponding component elements of the stream demultiplexer **35** according to the first embodiment depicted in FIG. **2**. The stream demultiplexer **352** differs from the stream demultiplexer **35** according to the first embodiment in that the second candidate group setting unit **432** in the candidate group setting unit **43** refers to the first candidate group constructed by the first candidate group setting unit **431**.

The second candidate group setting unit **432** refers to each transmitted signal candidate set $(x_0^{(min)}(c_{1i}), (i=0, 1, 2, \dots, m-1))$ contained in the first candidate group ϕ_1 . Then, the second candidate group setting unit **432** obtains the corresponding candidate for the transmitted signal x_1 only for one of the symbol replicas $x_0^{(min)}(c_{1i})$.

FIG. **13** is a diagram depicting one example of the first candidate group ϕ_1 . Here, the transmitted signals x_0 and x_1 are both modulated by QPSK. As depicted in FIG. **13**, $x_0^{(min)}(c_{1i})$ ($m=0$ to 3) is a symbol replica corresponding to one of the symbols "01", "10", and "11". Therefore, the symbol replica that gives symbol "00" for the transmitted signal x_0 is not a candidate for the transmitted signal x_0 . Accordingly, the second candidate group setting unit **432** obtains the corresponding candidate for the transmitted signal x_1 only for the symbol replica corresponding to one of the symbols "01", "10", and "11" of the transmitted signal x_0 . In this way, the receiving apparatus according to the third embodiment can reduce the amount of computation in the transmitted signal demultiplex-

27

ing process by reducing the number of times that the second candidate group setting unit **432** has to perform the quadrant detection.

Alternatively, after the second candidate group setting unit **432** has constructed the second candidate group, the first candidate group setting unit **431** may obtain the corresponding candidate for the transmitted signal x_0 only for the candidate for the transmitted signal x_1 contained in the second candidate group.

Next, a receiving apparatus according to a fourth embodiment will be described. The receiving apparatus according to the fourth embodiment has three or more antennas and receiving units coupled to the respective antennas, and demultiplexes the transmitted signals from the signals received by the respective antennas. As an example, the following description is given by assuming that the receiving apparatus has three antennas and three receiving units coupled to the respective antennas.

FIG. **14** is a diagram schematically illustrating the configuration of the stream demultiplexer **353** in the receiving apparatus according to the fourth embodiment. The stream demultiplexer **353** includes a channel interchanging unit **41**, a QR-decomposition unit **42'**, a candidate group setting unit **43'**, a common group searching unit **44**, a metric calculating unit **45**, a minimum value searching unit **46**, an additional metric calculating unit **47**, and a logarithmic likelihood ratio computing unit **48**.

These units constituting the stream demultiplexer **353** may be implemented as separate computing circuits. Alternatively, these units constituting the stream demultiplexer **353** may be integrated into a single computing circuit implementing the functions of the respective units.

In FIG. **14**, the units constituting the stream demultiplexer **353** are designated by the same reference numerals as those used to designate the corresponding component elements of the stream demultiplexer **35** according to the first embodiment depicted in FIG. **2**.

The QR-decomposition unit **42'** QR-decomposes the channel matrix estimated by the channel estimator **34** or the transformed channel matrix generated by the channel interchanging unit **41**.

The relationship between the transmitted signals and the received signals is expressed by the following equation using the channel matrix.

$$Y = HX + n \quad (18)$$

$$\begin{pmatrix} y_0 \\ y_1 \\ y_2 \end{pmatrix} = \begin{pmatrix} h_{00} & h_{01} & h_{02} \\ h_{10} & h_{11} & h_{12} \\ h_{20} & h_{21} & h_{22} \end{pmatrix} \begin{pmatrix} x_0 \\ x_1 \\ x_2 \end{pmatrix} + \begin{pmatrix} n_0 \\ n_1 \\ n_2 \end{pmatrix}$$

where x_0 to x_2 represent the signals transmitted out from the three antennas of the transmitting apparatus. The transmitted signal vector X is a vector whose elements are the transmitted signals x_0 to x_2 . On the other hand, y_0 to y_2 represent the signals received via the respective antennas of the receiving apparatus. The received signal vector Y is a vector whose elements are the received signals y_0 to y_2 . The matrix H indicates the channel matrix whose elements h_{ij} are each obtained, for example, as a channel impulse response to a pilot signal. The vector n indicates the noise vector whose elements n_0 to n_2 represent the noise components contained in the received signals y_0 to y_2 , respectively.

28

The QR-decomposition unit **42'** QR-decomposes the channel matrix H received from the channel estimator **34** into a unitary matrix Q and an upper triangular matrix R as shown in the following equation.

$$H = QR \quad (19)$$

$$\begin{pmatrix} h_{00} & h_{01} & h_{02} \\ h_{10} & h_{11} & h_{12} \\ h_{20} & h_{21} & h_{22} \end{pmatrix} = \begin{pmatrix} q_{00} & q_{01} & q_{02} \\ q_{10} & q_{11} & q_{12} \\ q_{20} & q_{21} & q_{22} \end{pmatrix} \begin{pmatrix} r_{00} & r_{01} & r_{02} \\ 0 & r_{11} & r_{12} \\ 0 & 0 & r_{22} \end{pmatrix}$$

Then, the QR-decomposition unit **42'** multiplies both sides of equation (18) from the left by the Hermitian conjugate Q^H of the unitary matrix Q . In this way, the QR-decomposition unit **42'** obtains the unitary transformed vector z by unitary-transforming the received signal vector Y . The relationship between the unitary transformed vector z , the upper triangular matrix R , and the transmitted signal vector X is expressed by the following equation.

$$z = Q^H Y = Q^H Q R X + Q^H n = R X + Q^H n \quad (20)$$

$$\begin{pmatrix} z_0 \\ z_1 \\ z_2 \end{pmatrix} = \begin{pmatrix} r_{00} & r_{01} & r_{02} \\ 0 & r_{11} & r_{12} \\ 0 & 0 & r_{22} \end{pmatrix} \begin{pmatrix} x_0 \\ x_1 \\ x_2 \end{pmatrix} + \begin{pmatrix} q_{00}^* & q_{10}^* & q_{20}^* \\ q_{01}^* & q_{11}^* & q_{21}^* \\ q_{02}^* & q_{12}^* & q_{22}^* \end{pmatrix} \begin{pmatrix} n_0 \\ n_1 \\ n_2 \end{pmatrix}$$

where unitary transformed signals z_0 to z_2 are the elements of the unitary transformed vector z .

Further, the QR-decomposition unit **42'** QR-decomposes the transformed channel matrix $H^{(abc)}$ generated by the channel interchanging unit **41** into a unitary matrix $Q^{(abc)}$ and an upper triangular matrix $R^{(abc)}$ in like manner. Then, the QR-decomposition unit **42'** multiplies the equation expressing relationship between the received signal vector, the transformed channel matrix, and the transmitted signal vector by the Hermitian conjugate $Q^{(abc)H}$ of the unitary matrix $Q^{(abc)}$. In this way, the unitary transformed vector $z^{(abc)}$ is obtained by unitary-transforming the received signal vector Y . The relationship between the unitary transformed vector $z^{(abc)}$, the upper triangular matrix $R^{(abc)}$, and the transmitted signal vector $X^{(abc)}$ is expressed by the following equation.

$$z^{(abc)} = Q^{(abc)H} Y = \quad (21)$$

$$Q^{(abc)H} Q^{(abc)} R^{(abc)} X^{(abc)} + Q^{(abc)H} n = R^{(abc)} X^{(abc)} + Q^{(abc)H} n$$

$$\begin{pmatrix} z_0^{(abc)} \\ z_1^{(abc)} \\ z_2^{(abc)} \end{pmatrix} = \begin{pmatrix} r_{00}^{(abc)} & r_{01}^{(abc)} & r_{02}^{(abc)} \\ 0 & r_{11}^{(abc)} & r_{12}^{(abc)} \\ 0 & 0 & r_{22}^{(abc)} \end{pmatrix} \begin{pmatrix} x_a \\ x_b \\ x_c \end{pmatrix} +$$

$$\begin{pmatrix} q_{00}^{(abc)*} & q_{10}^{(abc)*} & q_{20}^{(abc)*} \\ q_{01}^{(abc)*} & q_{11}^{(abc)*} & q_{21}^{(abc)*} \\ q_{02}^{(abc)*} & q_{12}^{(abc)*} & q_{22}^{(abc)*} \end{pmatrix} \begin{pmatrix} n_a \\ n_b \\ n_c \end{pmatrix}$$

In equation (21), a , b , and c are each 0, 1, or 2, and $a \neq b \neq c$. The QR-decomposition unit **42'** passes the unitary transformed vectors z and $z^{(abc)}$, the upper triangular matrices R and $R^{(abc)}$, etc., to the candidate setting group **43'**.

The candidate group setting unit **43'** obtains a set of candidates for the likely transmitted signals. Referring to equation (20), it is seen that the unitary transformed vector signal z_0 is related to all of the transmitted signals. Therefore, based

on equation (20), the candidate group setting unit 43' obtains an estimate of the transmitted signal x_0 by canceling the components of the transmitted signals x_1 and x_2 from the unitary transformed signal z_0 .

When the transmitted signals x_1 and x_2 are c_{1i} and c_{2i} ($i=0, 1, \dots, m_1-1, j=0, 1, \dots, m_2-1$), respectively, the estimate u_{0ij} of the transmitted signal x_0 is expressed by the following equation. Here, m_1 and m_2 each represent the number of values that can be taken in the modulation scheme applied to the transmitted signal x_1 or x_2 , respectively.

$$u_{0ij} = \frac{z_0 - r_{01}c_{1i} - r_{02}c_{2j}}{r_{00}} \quad (22)$$

The candidate group setting unit 43', for example, similarly to the first candidate group setting unit 431, performs the quadrant detection on the estimate u_{0ij} and determines the symbol replica $x^{(min)}(c_{1i}, c_{2j})$ of the transmitted signal x_0 which is closest to the estimate u_{0ij} . Then, the candidate group setting unit 43' sets $\{x^{(min)}(c_{1i}, c_{2j}), c_{1i}, c_{2j}\}$ as the transmitted signal candidate set.

The candidate group setting unit 43' obtains the estimate u_{0ij} of the transmitted signal x_0 for each set of the symbol replicas c_{1i} and c_{2j} by substituting the symbol replicas c_{1i} and c_{2j} into equation (22). Then, by performing the above process on each of the thus obtained estimates u_{0ij} , the candidate group setting unit 43' obtains the first candidate group which is a collection of transmitted signal candidate sets.

Similarly, from the equation (21) obtained based on the transformed channel matrix $H^{(abc)}$, the candidate group setting unit 43' obtains the n -th candidate group which is a collection of transmitted signal candidate sets. Here, n is an integer not smaller than 2 but not larger than 6 which is the maximum number that the sum of a , b , and c can take. In this case, if the transmitted signals x_b and x_c are symbol replicas c_{bi} and c_{cj} ($i=0, 1, \dots, m_b-1, j=0, 1, \dots, m_c-1$), respectively, the estimate u_{aij} of the transmitted signal x_a is expressed by the following equation. Here, m_b and m_c each represent the number of values that can be taken in the modulation scheme applied to the transmitted signal x_b or x_c , respectively.

$$u_{aij} = \frac{z_0^{(abc)} - r_{01}^{(abc)}c_{bi} - r_{02}^{(abc)}c_{cj}}{r_{00}^{(abc)}} \quad (23)$$

The candidate group setting unit 43' performs the quadrant detection on the estimate u_{aij} and determines the symbol replica $x_a^{(min)}(c_{bi}, c_{cj})$ of the transmitted signal x_a which is closest to the estimate u_{aij} . Then, the candidate group setting unit 43' sets $\{x_a^{(min)}(c_{bi}, c_{cj}), c_{bi}, c_{cj}\}$ as the transmitted signal candidate set. Each time the candidate group is obtained, the candidate group setting unit 43' passes the candidate group to the common group searching unit 44.

The channel interchanging unit 41 creates at least one transformed channel matrix $H^{(abc)}$ by interchanging the order of the columns in the channel matrix H . Such transformed channel matrices $H^{(abc)}$ are created so that the order of the columns is different from one matrix to another. In the present embodiment, since the number of transmitted signals is 3, the number of transformed channel matrices $H^{(abc)}$ is 5 ($=_3P_3-1$) at maximum. If the number of transformed channel matrices $H^{(abc)}$ to be created is smaller than the number of transmitted signals, it is preferable that the channel interchanging unit 41 creates each transformed channel matrix $H^{(abc)}$ so that the

transmitted signal x_a located in the uppermost row in the above equation (21) is different from the transmitted signal x_0 as well as from x_a in the other transformed channel matrix. In this way, the transmitted signal whose estimate is obtained by the equation (22) or (23) can be made different for each channel matrix or each transformed channel matrix, respectively. As a result, since the candidate groups created according to the channel matrix and the transformed channel matrix are also different, the stream demultiplexer 353 can globally search for the transmitted signal candidate sets.

Each time the transformed channel matrix $H^{(abc)}$ is created, the channel interchanging unit 41 passes the created transformed channel matrix $H^{(abc)}$ to the QR-decomposition unit 42'. Further, the channel interchanging unit 41 stores the order of the columns in the created transformed channel matrix $H^{(abc)}$ into a buffer memory incorporated in the channel interchanging unit 41. Then, by referring to the order of the columns stored in the buffer memory, the channel interchanging unit 41 selects the order of the columns not yet stored, and interchanges the order of the columns in the channel matrix so as to match the selected order of the columns. The channel interchanging unit 41 can thus create a new transformed channel matrix which is different from any previously created transformed channel matrix $H^{(abc)}$.

Each time the candidate group is received from the candidate group setting unit 43', the common group searching unit 44 stores the candidate group into a buffer memory incorporated in the common group searching unit 44. Then, when the next candidate group is received, the common group searching unit 44 searches for transmitted signal candidate sets common to the two candidate groups. The common group searching unit 44 then groups together the transmitted signal candidate sets common to the two candidate groups and stores them as a common group into the buffer memory incorporated in the common group searching unit 44.

Thereafter, each time the subsequent candidate group is received, the common group searching unit 44 searches for transmitted signal candidate sets that are common between the received candidate group and the common group, and stores a group of such common transmitted signal candidate sets as a new common group into the buffer memory. After the transmitted signal candidate sets common to all the candidate groups have been extracted, the common group searching unit 44 passes the thus extracted transmitted signal candidate sets to the metric calculating unit 45. The metric calculating unit 45 calculates the metrics for the extracted transmitted signal candidate sets. The minimum value searching unit 46 obtains the minimum value among the thus calculated metrics, and estimates that the transmitted signal candidate set corresponding to the minimum value represents the actually transmitted signal set.

The operation flowchart of the transmitted signal demultiplexing process performed under control of the stream demultiplexer 353 is the same as the operation flowchart illustrated in FIGS. 7A, 7B, and 8, with the only difference that the process from step S105 to step S110 is repeated the same number of times as the number of transformed channel matrices to be created.

The stream demultiplexer 353 may repeat the process from step S105 to step S110 a predetermined number of times. Alternatively, the stream demultiplexer 353 may stop repeating the process from step S105 to step S110 when the number of transmitted signal candidate sets contained in the common group has dropped to or below a predetermined number.

In the receiving apparatus according to the fourth embodiment also, since the metric is calculated only for the transmitted signal candidate sets extracted by the common group

searching unit, the amount of computation needed to demultiplex the transmitted signals from the signals received by three or more antennas can be reduced.

It will be appreciated that the present invention is not limited to the above specific embodiments. For example, the stream demultiplexer according to any one of the first, third, and fourth embodiments need not necessarily include the QR-decomposition unit. In that case, the candidate group setting unit obtains the first and second candidate groups by using the equation expressing relationship between the channel matrix or transformed channel matrix, the received signal vector, and the transmitted signal vector. For example, using equation (4), the estimate u_{0i} of the transmitted signal x_0 is obtained as a residual component as shown in the following equation by canceling the component relating to the symbol replica c_{1i} of the transmitted signal x_1 from the received signal y_0 .

$$u_{0j} = \frac{y_0 - h_{01}c_{1i}}{h_{00}} \quad (24)$$

Then, as in the above embodiments, the candidate group setting unit can obtain the symbol replica $x_0(c_{1i})$ of the transmitted signal x_0 that is closest to the estimate u_{0i} , and can thus set $(x_0(c_{1i}), c_{1i})$ as the transmitted signal candidate set to be included in the first candidate group. Likewise, using equation (5), the estimate u_{1i} of the transmitted signal x_1 is obtained as a residual component as shown in the following equation by canceling the component relating to the signal replica c_{0i} of the transmitted signal x_0 from the received signal y_1 .

$$u_{1j} = \frac{y_1 - h_{10}c_{0i}}{h_{11}} \quad (25)$$

Then, as in the above embodiments, the candidate group setting unit can obtain the symbol replica $x_1(c_{0i})$ of the transmitted signal x_1 that is closest to the estimate u_{1i} , and can thus set $(c_{0i}, x_1(c_{0i}))$ as the transmitted signal candidate set to be included in the second candidate group.

Alternatively, using equation (4), the candidate group setting unit may obtain the estimate u_{1i} of the transmitted signal x_1 by canceling the component relating to the signal replica c_{0i} of the transmitted signal x_0 from the received signal y_1 . In this way, when the candidate group setting unit obtains the estimate of the transmitted signal different for each received signal by noting the different received signals, the channel interchanging unit may also be omitted.

Further, by substituting the transmitted signal set, for example, into the first term on the right-hand side of equation (4), the metric calculating unit and the additional metric calculating unit can each calculate the estimated transmitted signal set.

The receiving apparatus according to the fourth embodiment may be combined with the receiving apparatus according to the second embodiment. In this case, the stream demultiplexer 353 includes the ranking unit for determining the ranks of the transmitted signal candidate sets. Then, from the unitary transformed signal z_2 or z_c that depends only on one transmitted signal, for example, in equation (20) or (21), the ranking unit obtains the estimate of the corresponding transmitted signal x_2 or x_c . Then, by performing the quadrant detection on the estimate, the ranking unit assigns the ranking values in order of closeness to the estimate to the symbol

replicas corresponding to the values that the transmitted signal x_2 or x_c can take. The common group searching unit then allocates priorities to the transmitted signal candidate sets contained in the common group in accordance with the ranking values assigned to the respective candidate sets, and selects a predetermined number of candidate sets in decreasing order of priority.

Alternatively, the receiving apparatus according to the fourth embodiment may be combined with the receiving apparatus according to the third embodiment. Further, the receiving apparatus according to any one of the first to third embodiments may include only one QR-decomposition unit and only one candidate group setting unit, as in the receiving apparatus according to the fourth embodiment. Then, this one QR-decomposition unit may QR-decompose not only the channel matrix but also the transformed channel matrix, and this one candidate group setting unit may create candidate groups according to the channel matrix and the transformed channel matrix, respectively.

Further, a computer program having instructions for causing a processor to implement the functions of the respective units constituting the stream demultiplexer in the receiving apparatus according to any one of the above embodiments may be delivered to the receiving apparatus via a radio link. Then, the receiving apparatus may cause the stream demultiplexer to perform the transmitted signal demultiplexing process by loading the computer program into the processor contained in the receiving apparatus.

A communication apparatus capable of both signal transmission and signal reception using MIMO technology is constructed by combining the component elements of the transmitting apparatus 2 with the component elements of the receiving apparatus 3. In this case, the antennas 21-1 and 21-2 of the transmitting apparatus 2 and the antennas 31-1 and 31-2 of the receiving apparatus 3 are replaced by a set of common antennas. Each common antenna is coupled by the action of a duplexer to one of the transmitting units 25-1 and 25-2 in the transmitting apparatus 2 or to one of the receiving units 32-1 and 32-2 in the receiving apparatus 3, whichever is selected.

Next, a description will be given of a mobile station and a base station apparatus in a mobile communication system that employs the receiving apparatus or communication apparatus according to any one of the above embodiments.

FIG. 15 is a diagram schematically illustrating the configuration of the base station apparatus incorporating the above-described transmitting apparatus and receiving apparatus. The base station apparatus 100 includes a line terminating unit 101, a baseband processing unit 102, a call control unit 103, a plurality of communication units 104-1 to 104-n, and a plurality of antennas 105-1 to 105-n. Here, n is a natural number not smaller than 2. The baseband processing unit 102, the call control unit 103, and the communication units 104-1 to 104-n may be provided as separate circuits or may be implemented together on a single integrated circuit.

The line terminating unit 101 has a communication interface for connecting to a core network. The line terminating unit 101 terminates the core network to which a host apparatus is connected. The line terminating unit 101 receives from the core network a downlink signal to be transmitted to a mobile station, and passes the downlink signal to the baseband processing unit 102. On the other hand, the baseband processing unit 102 passes an uplink signal received from the mobile station to the line terminating unit 101, which then outputs the uplink signal onto the core network.

The baseband processing unit 102 implements the functions of the codeword generating unit 22, encoding unit 23, modulation unit 24, and control unit 26 provided in the trans-

33

mitting apparatus 2 according to each of the above embodiments. The baseband processing unit 102 further implements the functions of the demodulation unit 33, decoding unit 36, and data combining unit 37 provided in the receiving apparatus 3 according to each of the above embodiments.

The baseband processing unit 102 determines the precoding matrix and the number of streams, MOD, and TBS for each codeword, based on the feedback information received from the mobile station apparatus. Further, the baseband processing unit 102 splits the downlink signal received from the core network into codewords each having a length defined by the transport block size TBS. The baseband processing unit 102 applies error correction coding to each codeword. The baseband processing unit 102 generates data streams by splitting the encoded codeword in accordance with the above determined number of streams. Then, the baseband processing unit 102 generates transmit signals by quadrature-modulating the data streams in accordance with the modulation mode MOD. The baseband processing unit 102 outputs each transmit signal to a corresponding one of the antennas 105-1 to 105-*n* by referring to the precoding matrix.

On the other hand, the uplink signal received via the antennas 105-1 to 105-*n* is passed via the respective communication units 104-1 to 104-*n* to the baseband processing unit 102, which then demultiplexes from the uplink signal the signals transmitted out from the respective antennas of the mobile station apparatus. The baseband processing unit 102 then reconstructs each encoded codeword by combining the transmitted signals thus demultiplexed. The baseband processing unit 102 applies error correction decoding to each encoded codeword. The baseband processing unit 102 combines the thus decoded codewords to recover the original uplink signal. Then, the baseband processing unit 102 outputs the uplink signal onto the core network via the line terminating unit 101.

Further, the baseband processing unit 102 calculates the feedback information, such as CQI value, rank value, and precoding vector, to be fed back to the mobile station apparatus, and transmits the feedback information to the mobile station apparatus via one of the communication units 104-1 to 104-*n*.

The call control unit 103 performs call control processing such as paging, call answering, call termination, handover, etc., between the base station apparatus 100 and the mobile station apparatus such as a portable terminal communicating via the base station apparatus 100. Then, the call control unit 103 instructs the baseband processing unit 102 to start or terminate the operation, in accordance with the result of the call control processing.

The communication units 104-1 to 104-*n* each include one of the transmitting units provided in the transmitting apparatus 2 according to each of the above embodiments and one of the receiving units provided in the receiving apparatus 3. The transmitting unit and receiving unit provided in each of the communication units 104-1 to 104-*n* are coupled via a duplexer (not illustrated) to one of the antennas 105-1 to 105-*n*. The communication units 104-1 to 104-*n* amplify the downlink signal received from the baseband processing unit 102, and transmit out the amplified downlink signal via the antennas 105-1 to 105-*n*.

Further, the communication units 104-1 to 104-*n* receive via the antennas 105-1 to 105-*n* the uplink signal transmitted from the mobile station apparatus. Then, the communication units 104-1 to 104-*n* amplify the received uplink signal and pass it to the baseband processing unit 102.

Each communication unit in the base station apparatus may be provided as an apparatus independent of the base station apparatus proper. In that case, each communication unit is

34

coupled to the base station apparatus proper, for example, by an optical fiber. Then, each communication unit and the base station apparatus proper communicate with each other in accordance with a communication standard such as Common

5 Public Radio Interface (CPRI).

FIG. 16 is a diagram schematically illustrating the configuration of the mobile station apparatus incorporating the above-described transmitting apparatus and receiving apparatus. The mobile station apparatus 200 includes a control unit 201, a baseband processing unit 202, a call control unit 203, a plurality of communication units 204-1 to 204-*n*, and a plurality of antennas 205-1 to 205-*n*. Here, *n* is a natural number not smaller than 2. The control unit 201, the baseband processing unit 202, the call control unit 203, and the communication units 204-1 to 204-*n* may be provided as separate circuits or may be implemented together on a single integrated circuit.

The control unit 201 controls the entire operation of the mobile station apparatus 200. The control unit 201 executes various application programs that run on the mobile station apparatus 200. For this purpose, the control unit 201 includes a processor, a nonvolatile memory, and a volatile memory. When an application for performing communications such as voice or data communications is started up by a user operation via an operation unit (not illustrated) such as a keypad incorporated in the mobile station apparatus 200, the control unit 201 operates the call control unit 203 in accordance with the application. Then, the control unit 201 applies information source coding to the voice signal acquired via a microphone (not illustrated) incorporated in the mobile station apparatus 200 or to the data requested for transmission by the application. The control unit 201 passes the thus processed signal as an uplink signal to the baseband processing unit 202. On the other hand, when a downlink signal is received from the baseband processing unit 202, the control unit 201 applies information source decoding to it and recovers the data or voice signal. The control unit 201 passes the voice signal to a speaker (not illustrated) incorporated in the mobile station apparatus 200. Or, the control unit 201 displays the acquired data on a display (not illustrated) incorporated in the mobile station apparatus 200.

The baseband processing unit 202 implements the functions of the codeword generating unit 22, encoding unit 23, modulation unit 24, and control unit 26 provided in the transmitting apparatus 2 according to each of the above embodiments. The baseband processing unit 202 further implements the functions of the demodulation unit 33, decoding unit 36, and data combining unit 37 provided in the receiving apparatus 3 according to each of the above embodiments.

The baseband processing unit 202 determines the precoding matrix and the number of streams, MOD, and TBS for each codeword, based on the feedback information received from the base station apparatus. Further, the baseband processing unit 202 splits the uplink signal into codewords each having a length defined by the transport block size TBS. The baseband processing unit 202 applies error correction coding to each codeword. The baseband processing unit 202 generates data streams by splitting the encoded codeword in accordance with the above determined number of streams. Then, the baseband processing unit 202 generates transmit signals by quadrature-modulating the data streams in accordance with the modulation mode MOD. The baseband processing unit 202 supplies each transmit signal to a corresponding one of the communication units 204-1 to 204-*n* by referring to the precoding matrix.

On the other hand, the downlink signal, when received, is passed via the respective communication units 204-1 to 204-*n*

35

to the baseband processing unit **202**, which then demultiplexes from the downlink signal the signals transmitted out from the respective antennas of the base station apparatus. The baseband processing unit **202** then reconstructs each encoded codeword by combining the transmitted signals thus demultiplexed. The baseband processing unit **202** applies error correction decoding to each encoded codeword. The baseband processing unit **202** combines the thus decoded codewords to recover the original downlink signal. Then, the baseband processing unit **202** passes the downlink signal to the control unit **201**.

Further, the baseband processing unit **202** calculates the feedback information, such as CQI value, rank value, and precoding vector, to be fed back to the base station apparatus, and transmits the feedback information to the base station apparatus via one of the antennas **205-1** to **205-n**.

The call control unit **203** performs call control processing such as paging, call answering, call termination, handover, etc., between the mobile station apparatus **200** and the base station apparatus. Then, the call control unit **203** instructs the baseband processing unit **202** to start or terminate the operation, in accordance with the result of the call control processing.

The communication units **204-1** to **204-n** each include one of the transmitting units provided in the transmitting apparatus **2** according to each of the above embodiments and one of the receiving units provided in the receiving apparatus **3**. The transmitting unit and receiving unit provided in each of the communication units **204-1** to **204-n** are coupled via a duplexer (not illustrated) to one of the antennas **205-1** to **205-n**. The communication units **204-1** to **204-n** amplify the uplink signal received from the baseband processing unit **202**, and transmit out the amplified uplink signal via the antennas **205-1** to **205-n**.

Further, the communication units **204-1** to **204-n** receive via the antennas **205-1** to **205-n** the downlink signal transmitted from the base station apparatus. Then, the communication units **204-1** to **204-n** amplify the received downlink signal and pass it to the baseband processing unit **202**.

The mobile station apparatus **200** may further include an interface unit for connecting the mobile station apparatus **200** to another apparatus via a data transmission link such as a Peripheral Component Interconnect (PCI) bus or a Universal Serial Bus (USB). In that case, the interface unit is coupled to the control unit **201**, and outputs signals received from the control unit **201** onto the data transmission link for transmission to that other apparatus. On the other hand, when a signal is received from that other apparatus via the data transmission link, the interface unit passes the signal to the control unit **201**.

All of the examples and conditional language recited herein are intended for pedagogical purposes to aid the reader in understanding the invention and the concepts contributed by the inventor to furthering the art, and are to be construed as being without limitation to such specifically recited examples and conditions, nor does the organization of such examples in the specification relate to a showing of superiority and inferiority of the invention. Although the embodiments of the present invention have been described in detail, it should be understood that the various changes, substitutions, and alterations could be made hereto without departing from the spirit and scope of the invention.

What is claimed is:

1. A communication apparatus comprising:

a plurality of antennas;

a plurality of receiving units which are each coupled to one of said plurality of antennas, and which respectively

36

acquire received signals by receiving, via said coupled antennas, a plurality of signals transmitted from a transmitting apparatus having a plurality of antennas;

a candidate group setting unit which, based on a first channel matrix describing a communication channel between said plurality of transmitted signals and said plurality of received signals, calculates a first residual component by canceling a component corresponding to a candidate or candidates for a first other transmitted signal or signals other than a first transmitted signal among said plurality of transmitted signals from a first signal corresponding to at least one of said plurality of received signals and having components corresponding to all of said plurality of transmitted signals, determines a candidate for said first transmitted signal by selecting a value closest to said first residual component from among values that said first transmitted signal can take, and constructs a first candidate group as a collection of candidate sets each comprising a candidate for said first transmitted signal and a candidate or candidates for said first other transmitted signal or signals, and

which, based on a second channel matrix describing a communication channel between said plurality of transmitted signals and said plurality of received signals, calculates a second residual component by canceling a component corresponding to a candidate or candidates for a second other transmitted signal or signals other than a second transmitted signal among said plurality of transmitted signals from a second signal corresponding to at least one of said plurality of received signals and having components corresponding to all of said plurality of transmitted signals, determines a candidate for said second transmitted signal by selecting a value closest to said second residual component from among values that said second transmitted signal can take, and constructs a second candidate group as a collection of candidate sets each comprising a candidate for said second transmitted signal and a candidate or candidates for said second other transmitted signal or signals;

a common group searching unit which constructs a common group by selecting any transmitted signal candidate set that is common between said first candidate group and said second candidate group;

a metric calculating unit which, for each transmitted signal candidate set contained in said common group, computes an estimated received signal set corresponding to said each transmitted signal candidate set, and calculates a distance between said estimated received signal set and said plurality of received signals; and

a signal estimating unit which estimates that the transmitted signal candidate set that minimizes said distance represents the set of said plurality of transmitted signals.

2. The communication apparatus according to claim 1, further comprising a channel interchanging unit which creates said second channel matrix by interchanging the order of columns in said first channel matrix.

3. The communication apparatus according to claim 1, wherein said first channel matrix and said second channel matrix are the same channel matrix.

4. The communication apparatus according to claim 1, further comprising a ranking unit which, for each of said transmitted signal candidate sets contained in said first candidate group, calculates a first ranking value that provides a measure of the likelihood that said each transmitted signal candidate set represents said plurality of transmitted signals, and which, for each of said transmitted signal candidate sets contained in said second candidate group, calculates a second

37

ranking value that provides a measure of the likelihood that said each transmitted signal candidate set represents said plurality of transmitted signals, and wherein

based on said first ranking value and said second ranking value, said common group searching unit allocates priority to each of said transmitted signal candidate sets contained in said common group, said priority increasing in increasing order of the likelihood of said each transmitted signal candidate set representing said plurality of transmitted signals, and

said metric calculating unit calculates said distance for a predetermined number of candidate sets selected in decreasing order of said priority.

5. The communication apparatus according to claim 4, further comprising a decomposition unit which decomposes said first channel matrix into a unitary matrix and a triangular matrix and obtains a plurality of unitary transformed signals by multiplying a received signal vector, whose elements are said plurality of received signals, by a Hermitian conjugate of said unitary matrix, and wherein

said candidate group setting unit calculates an estimate of a third transmitted signal based on said triangular matrix and on a unitary transformed signal selected as having a component only of said third transmitted signal from among said plurality of unitary transformed signals, said third transmitted signal being one of said plurality of transmitted signals but different from said first transmitted signal, and said first ranking value assigned to each of said transmitted signal candidate sets contained in said first candidate group is set so as to indicate that said likelihood is greater as a candidate for said third transmitted signal contained in said each transmitted signal candidate set is closer to said estimate.

6. The communication apparatus according to claim 5, wherein said candidate group setting unit constructs said first candidate group by using only a predetermined number of candidates for said third transmitted signal that are selected from among the candidates for said third transmitted signal in order of closeness to the estimate of said third transmitted signal.

7. The communication apparatus according to claim 1, wherein said candidate group setting unit constructs said second candidate group by including as the candidate or candidates for said second other transmitted signal or signals only the values selected, from among the values that said first transmitted signal can take, as the candidates for said first transmitted signal contained in said first candidate group.

8. The communication apparatus according to claim 1, wherein said candidate group setting unit detects a quadrant to which said first residual component belongs, based on the sign of a real component of said first residual component and the sign of an imaginary component thereof, and determines the value closest to said first residual component by judging that, of the values that said first transmitted signal can take, any value belonging to said quadrant is closer to said first residual component than a value not belonging to said quadrant.

9. The communication apparatus according to claim 1, further comprising:

an additional metric calculating unit which calculates said distance as a second distance for a set of candidates for transmitted signals including transmitted signals each having one inverted bit with respect to one of said transmitted signals contained in said estimated transmitted signal set; and

38

a logarithmic likelihood ratio computing unit which computes a logarithmic likelihood ratio by calculating a difference between said first distance and said second distance.

10. The communication apparatus according to claim 1 as a base station apparatus, further comprising:

a decoding unit which recovers an uplink signal by decoding said plurality of transmitted signals; and
a line terminating unit which outputs said uplink signal onto a core network.

11. The communication apparatus according to claim 1 as a mobile station apparatus, further comprising a decoding unit which recovers a downlink signal by decoding said plurality of transmitted signals.

12. A communication method performed by a receiving apparatus having a plurality of antennas that obtain a plurality of received signals by receiving a plurality of signals transmitted from a transmitting apparatus having a plurality of antennas, comprising:

based on a first channel matrix describing a communication channel between said plurality of transmitted signals and said plurality of received signals, calculating a first residual component by canceling a component corresponding to a candidate or candidates for a first other transmitted signal or signals other than a first transmitted signal among said plurality of transmitted signals from a first signal corresponding to at least one of said plurality of received signals and having components corresponding to all of said plurality of transmitted signals; determining a candidate for said first transmitted signal by selecting a value closest to said first residual component from among values that said first transmitted signal can take; and constructing a first candidate group as a collection of candidate sets each comprising a candidate for said first transmitted signal and a candidate or candidates for said first other transmitted signal or signals;

based on a second channel matrix describing a communication channel between said plurality of transmitted signals and said plurality of received signals, calculating a second residual component by canceling a component corresponding to a candidate or candidates for a second other transmitted signal or signals other than a second transmitted signal among said plurality of transmitted signals from a second signal corresponding to at least one of said plurality of received signals and having components corresponding to all of said plurality of transmitted signals;

determining a candidate for said second transmitted signal by selecting a value closest to said second residual component from among values that said second transmitted signal can take; and constructing a second candidate group as a collection of candidate sets each comprising a candidate for said second transmitted signal and a candidate or candidates for said second other transmitted signal or signals;

constructing a common group by selecting any transmitted signal candidate set that is common between said first candidate group and said second candidate group;

for each transmitted signal candidate set contained in said common group, computing an estimated received signal set corresponding to said each transmitted signal candidate set, and calculating a distance between said estimated received signal set and said plurality of received signals; and

estimating that the transmitted signal candidate set that minimizes said distance represents the set of said plurality of transmitted signals.

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