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Valley et al.

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(54) **SYSTEMS AND METHODS FOR CONVERTING WIDEBAND SIGNALS IN THE OPTICAL DOMAIN**

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H03M 1/00 (2006.01)

(52) **U.S. Cl.** **341/137; 341/155**

(58) **Field of Classification Search** **341/137, 341/155**

See application file for complete search history.

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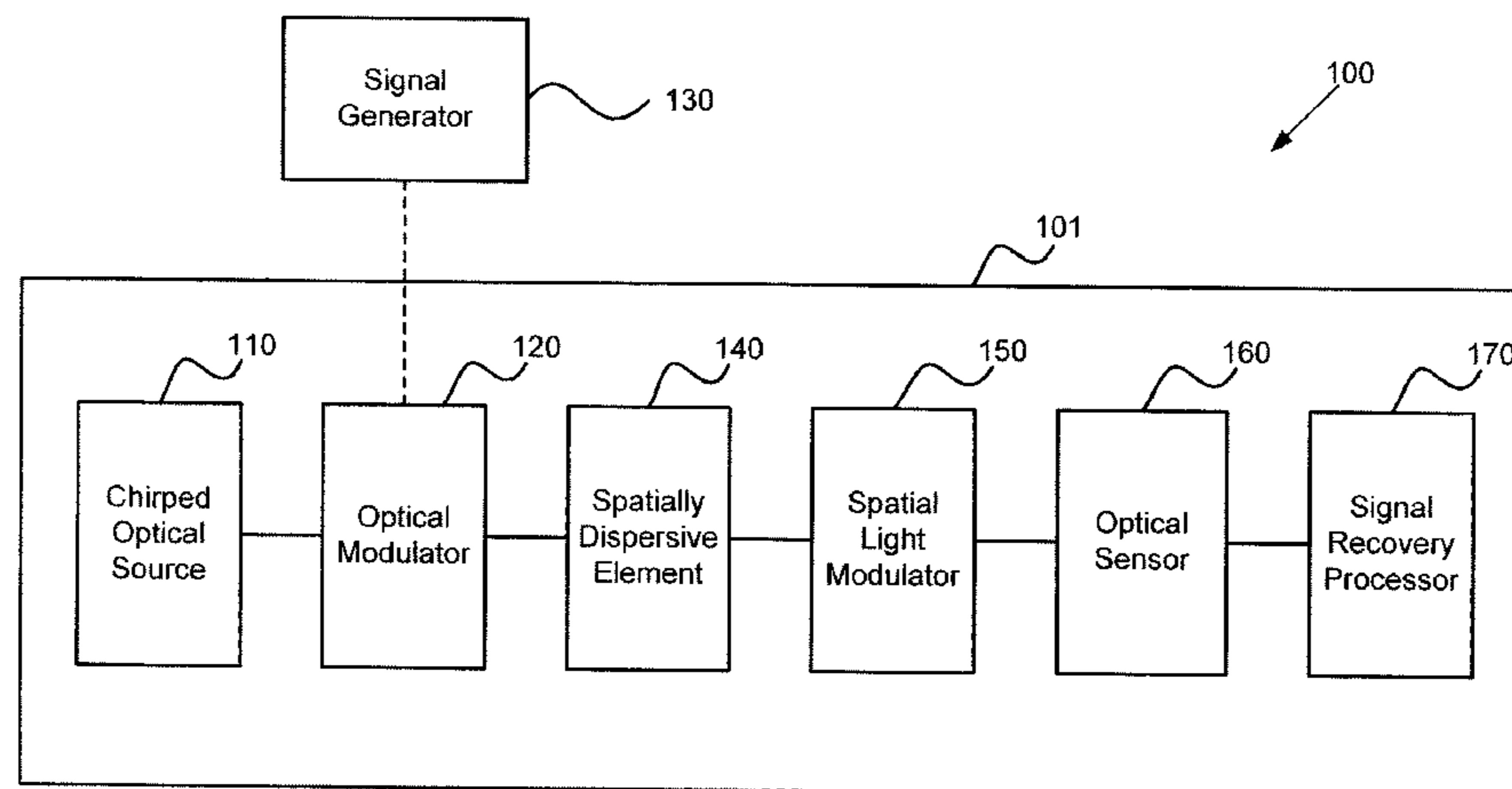
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(57) **ABSTRACT**

Systems and methods for converting wideband signals in the optical domain are provided. A device for obtaining a digital representation of a received signal may include a spatially dispersive element that may be configured to spatially disperse frequencies in an optical-domain representation of the received signal; a spatial light modulator that may be configured to mix the dispersed optical frequencies by imposing a mixing matrix on an optical intensity of the dispersed optical frequencies; an optical sensor that may be configured to obtain an electrical representation of the mixed dispersed optical frequencies; and a signal recovery processor that may be configured to obtain a digital representation of the received signal based on the electrical representation and the mixing matrix. The signal recovery processor may be further configured to determine a modulation format of the digital representation and may demodulate the digital representation based on the modulation format.

20 Claims, 18 Drawing Sheets



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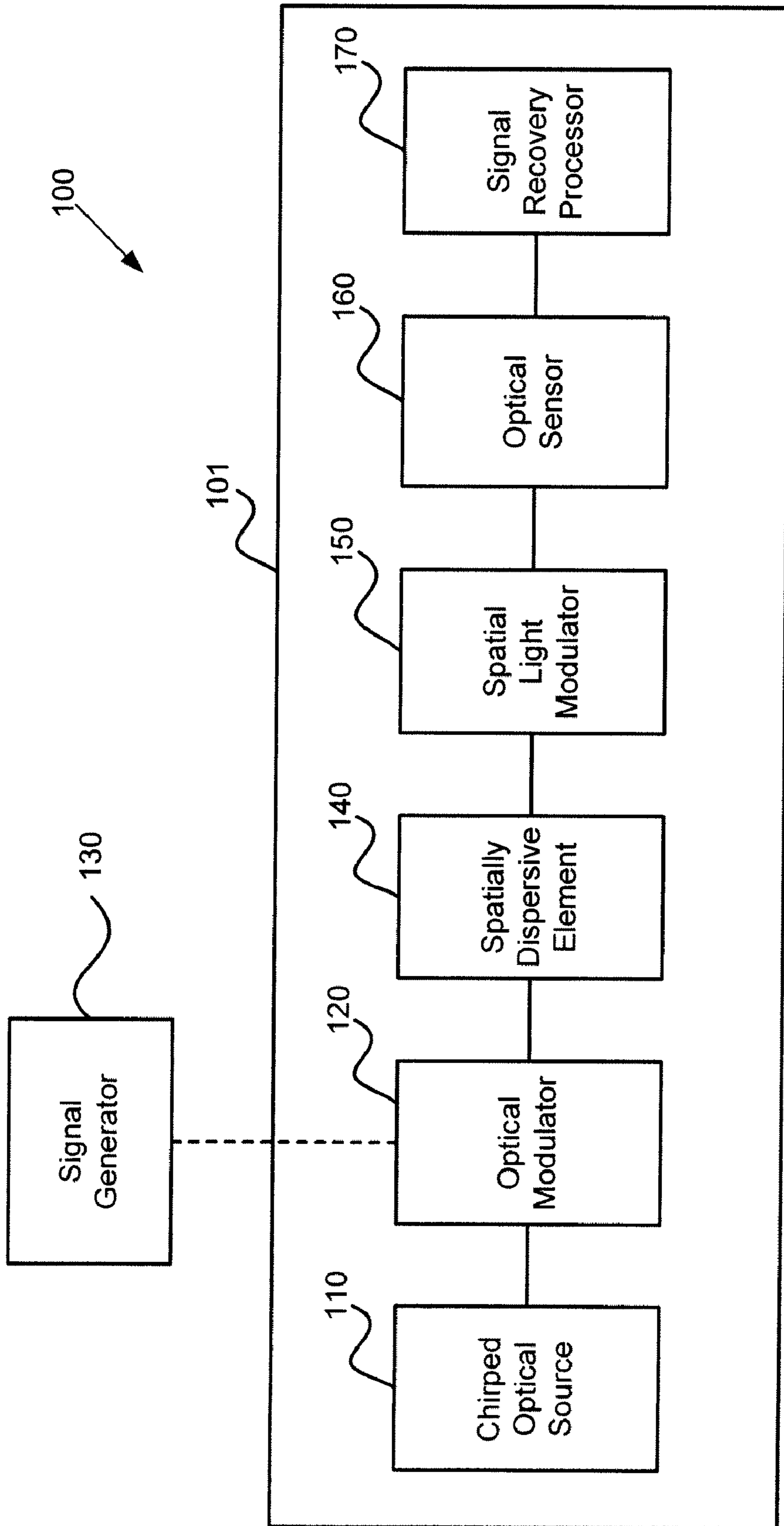


FIG. 1

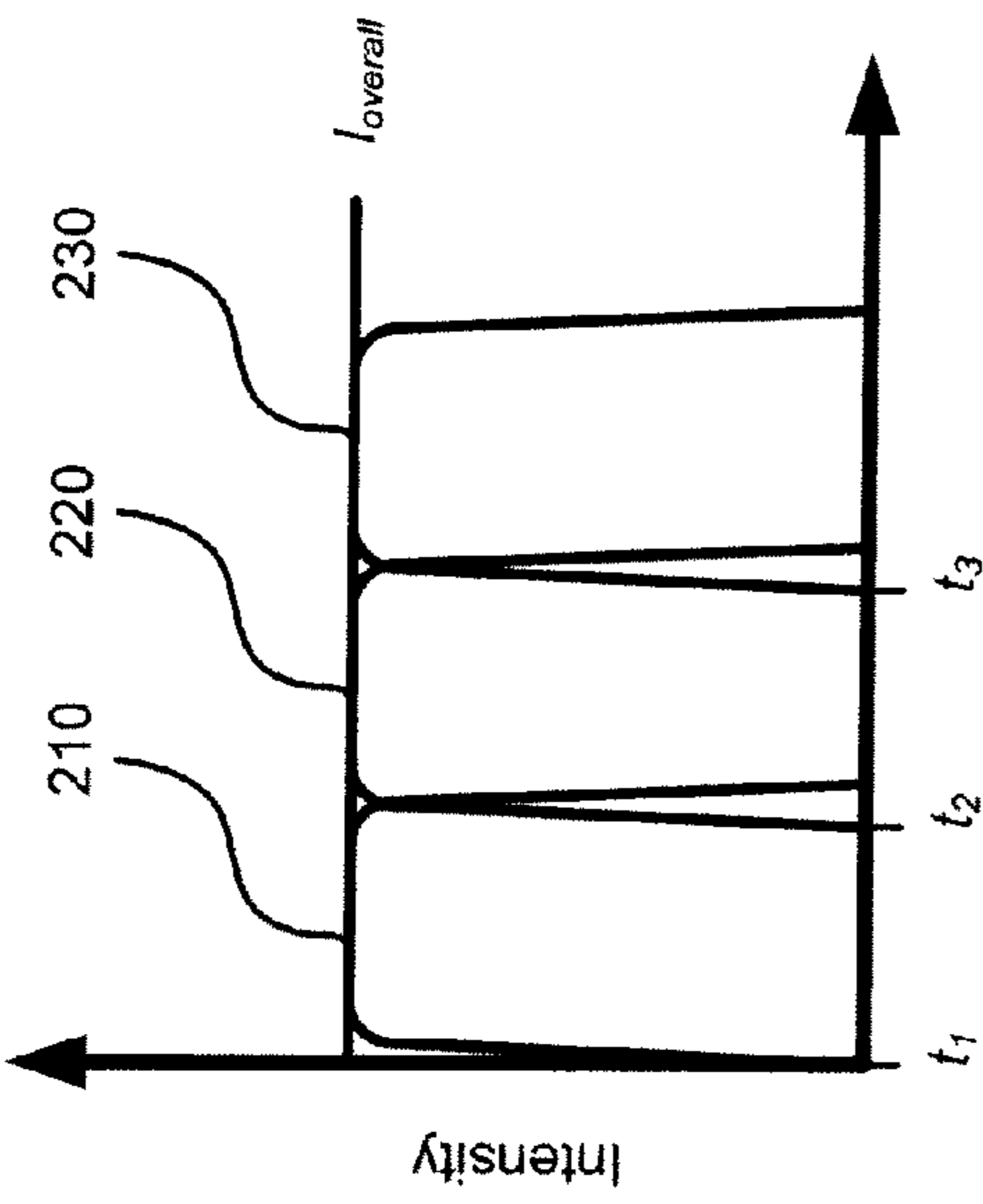


FIG. 2A

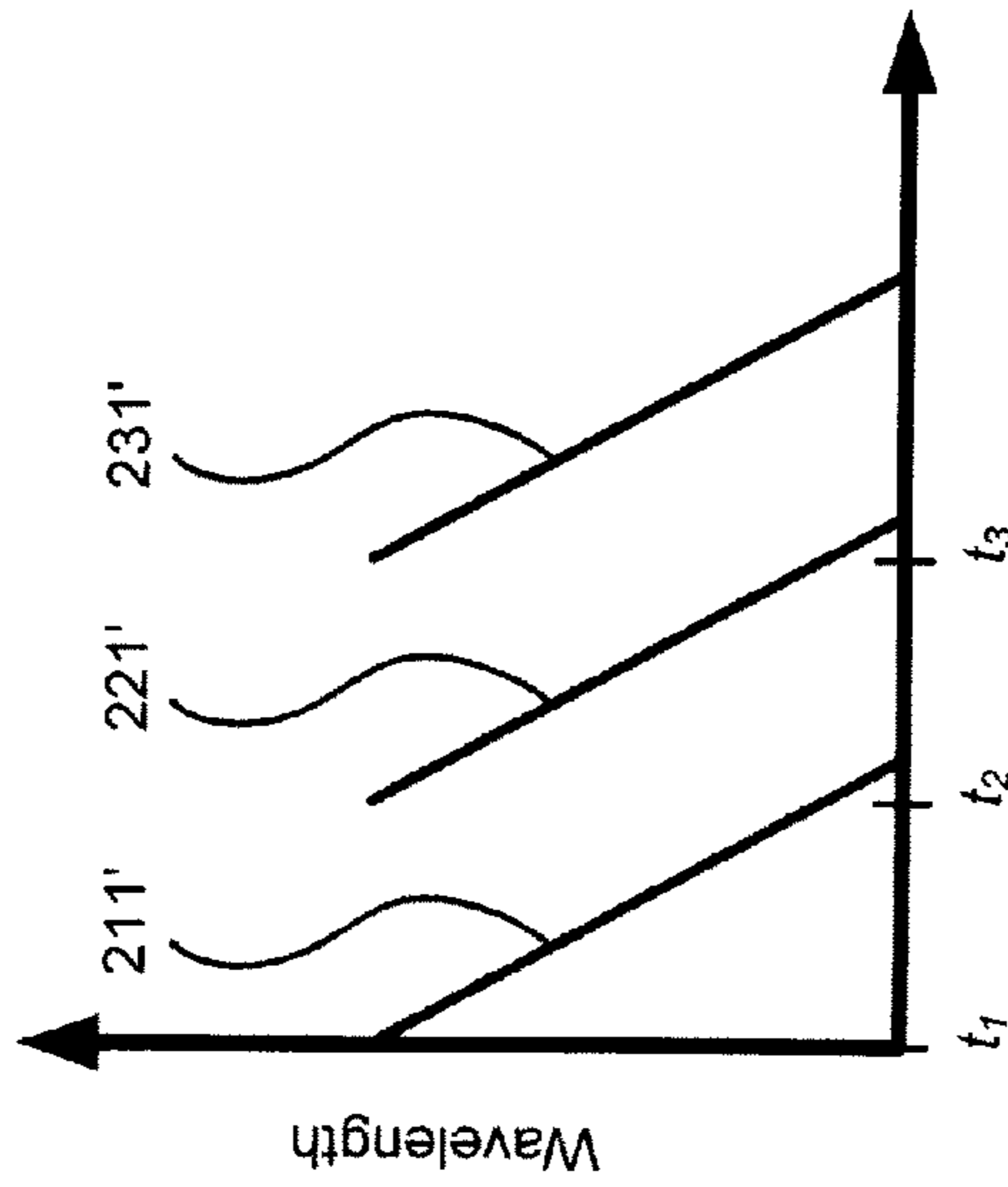


FIG. 2C

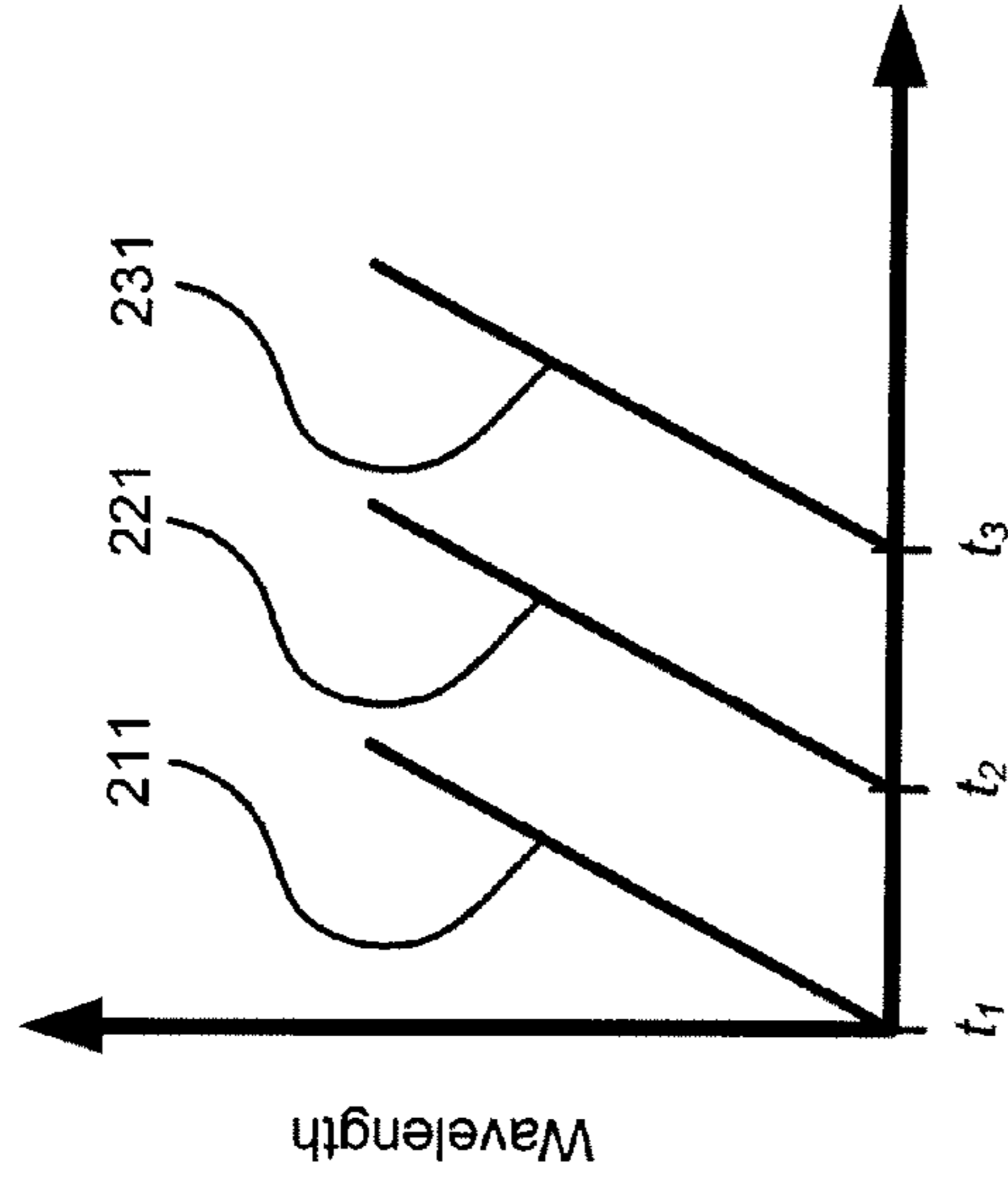


FIG. 2B

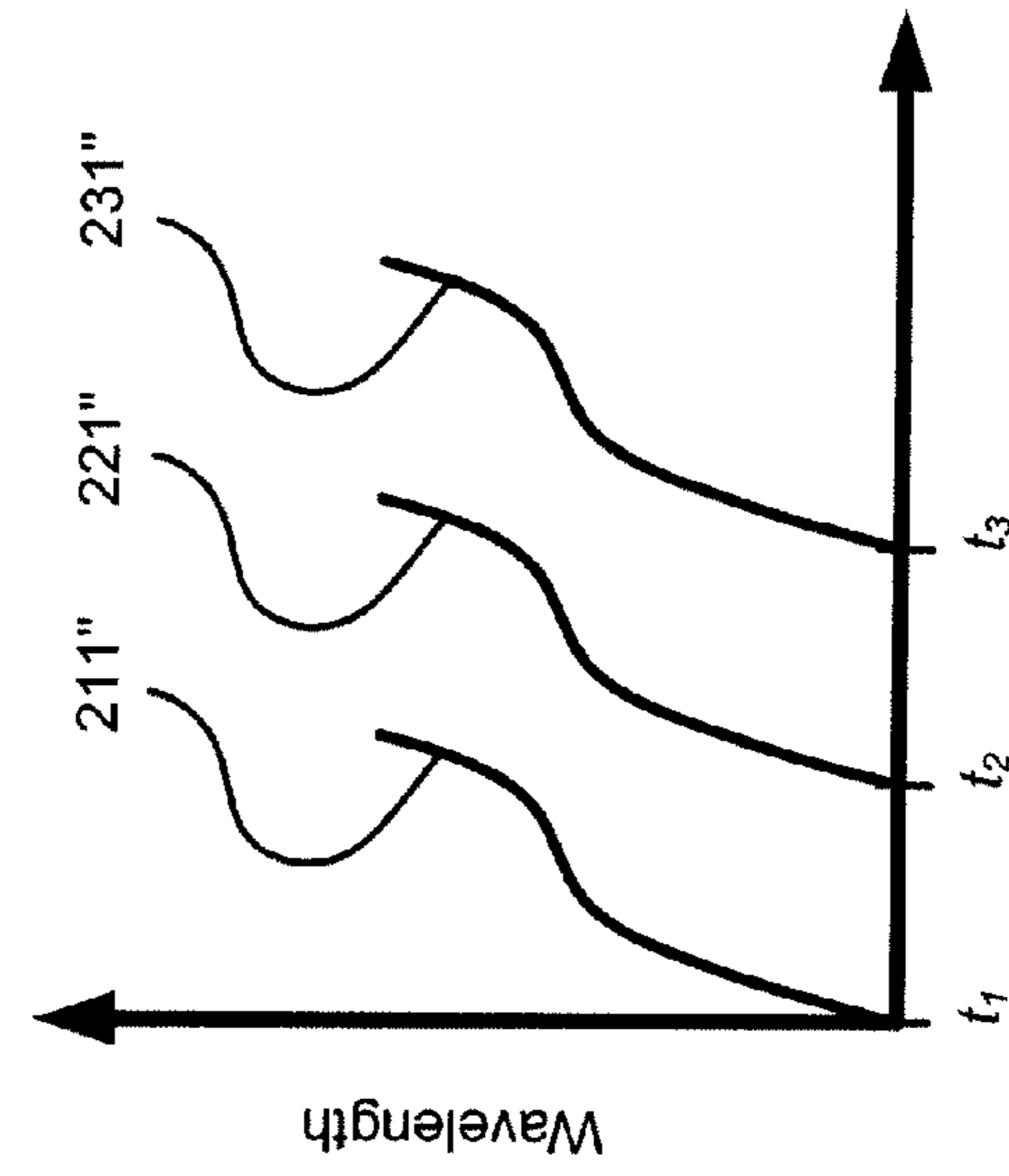


FIG. 2D

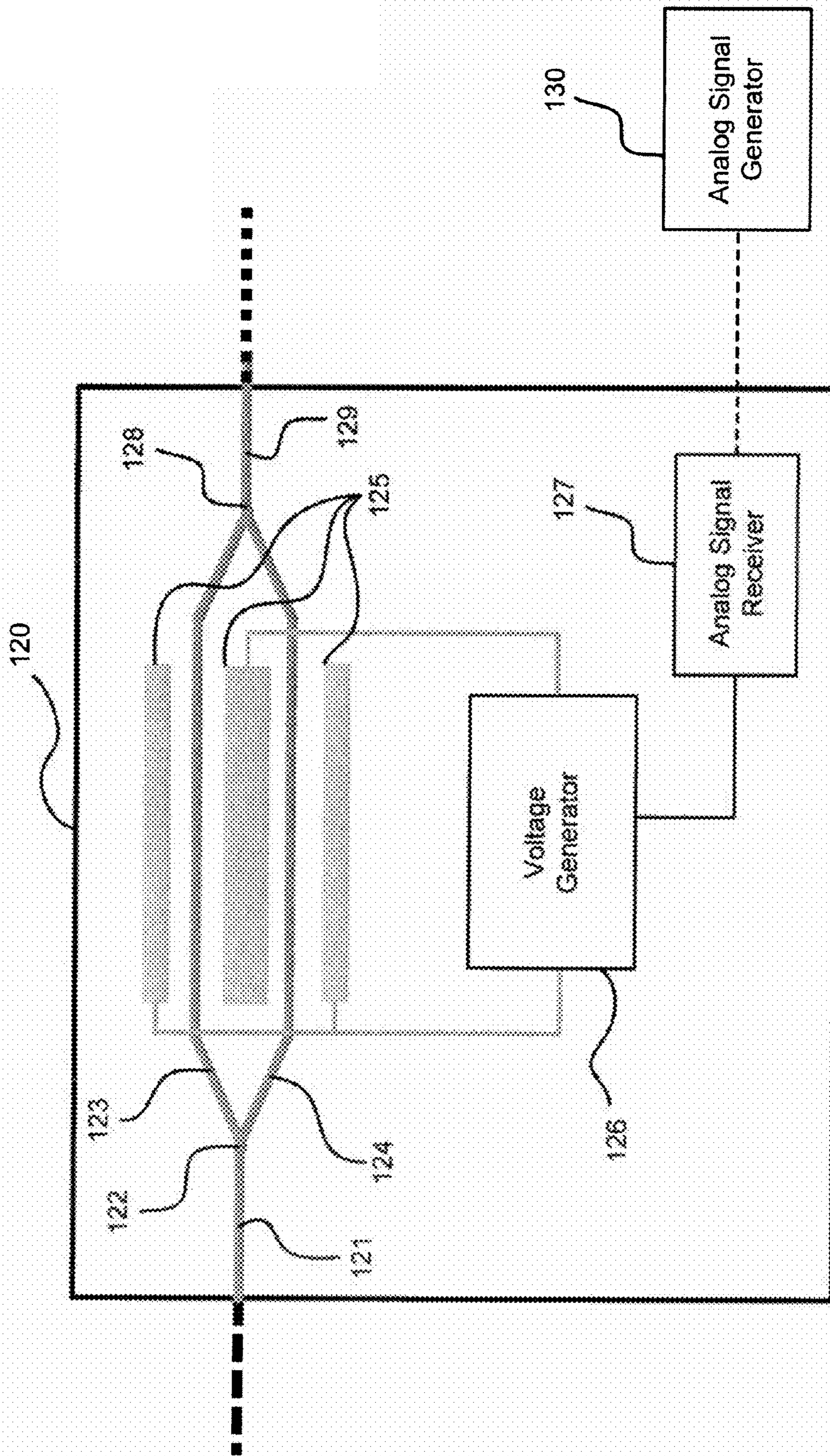


FIG. 3

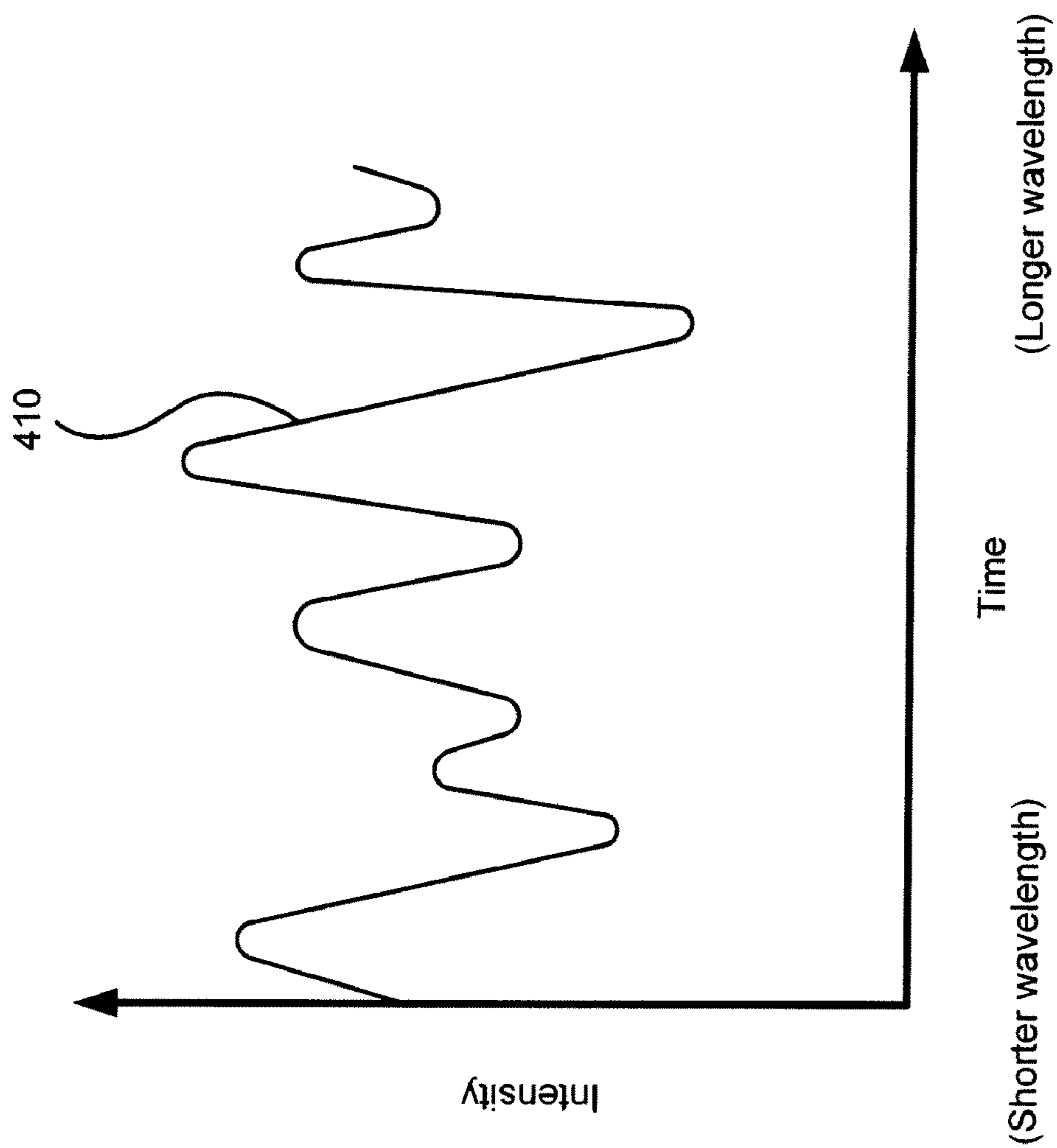


FIG. 4

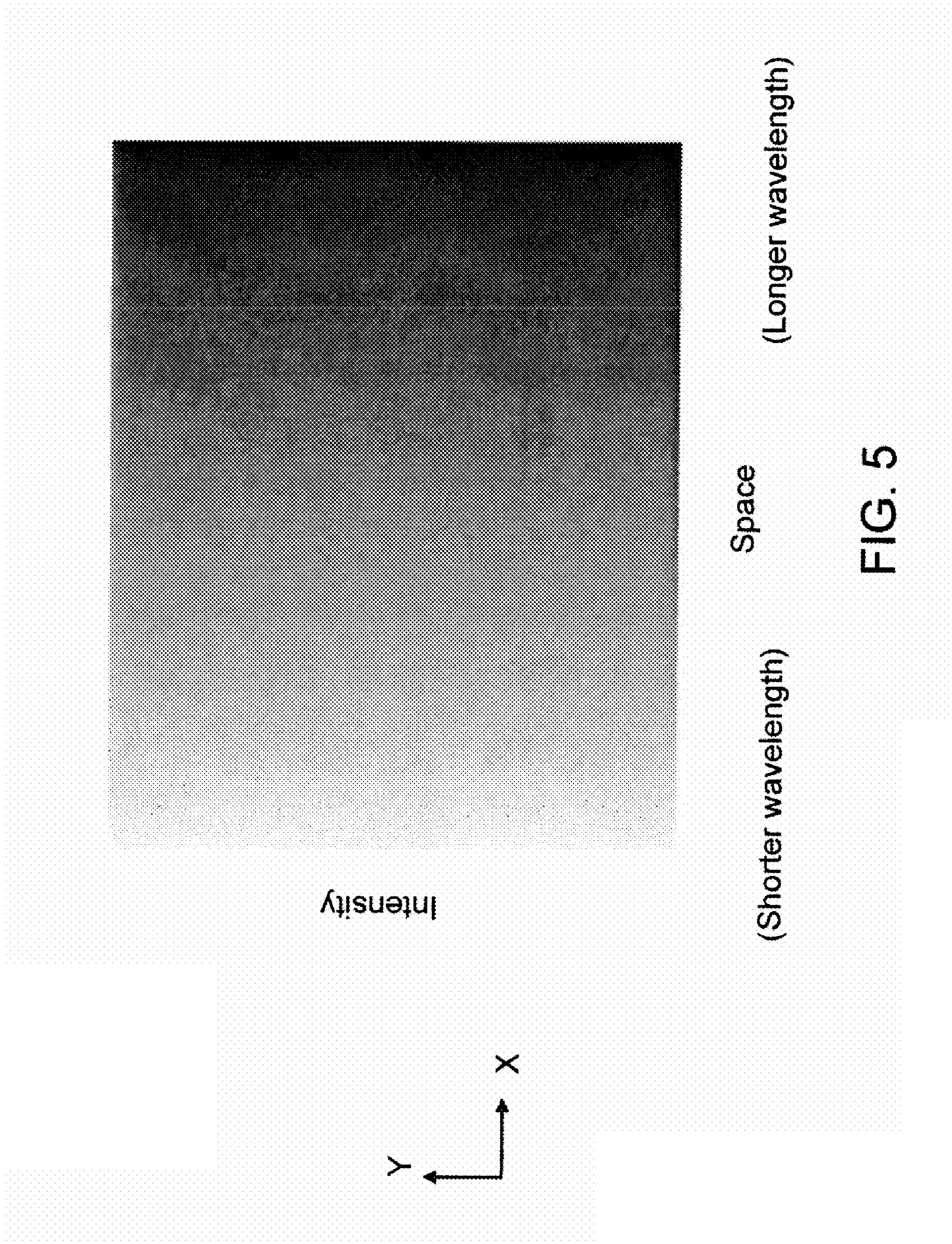


FIG. 5

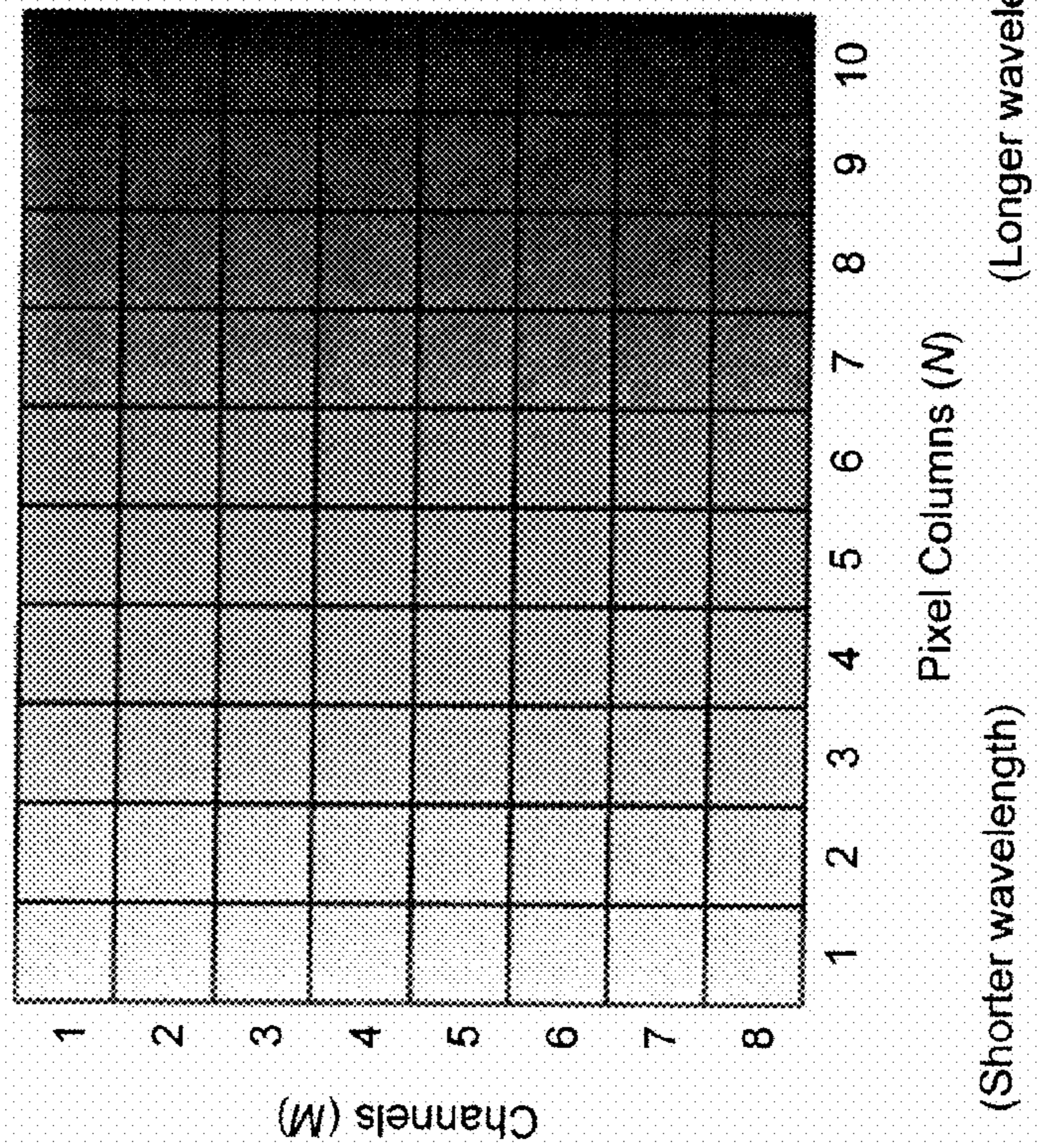
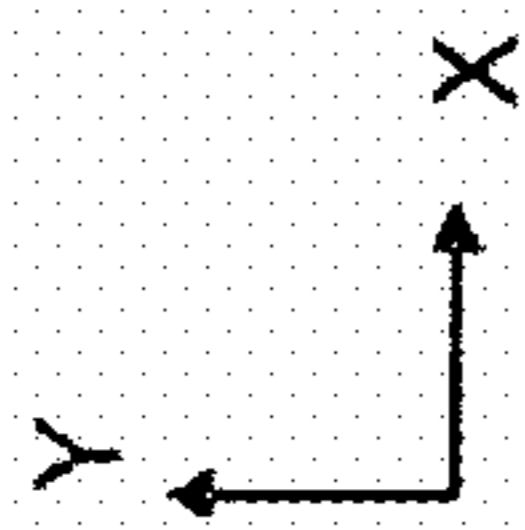


FIG. 6A

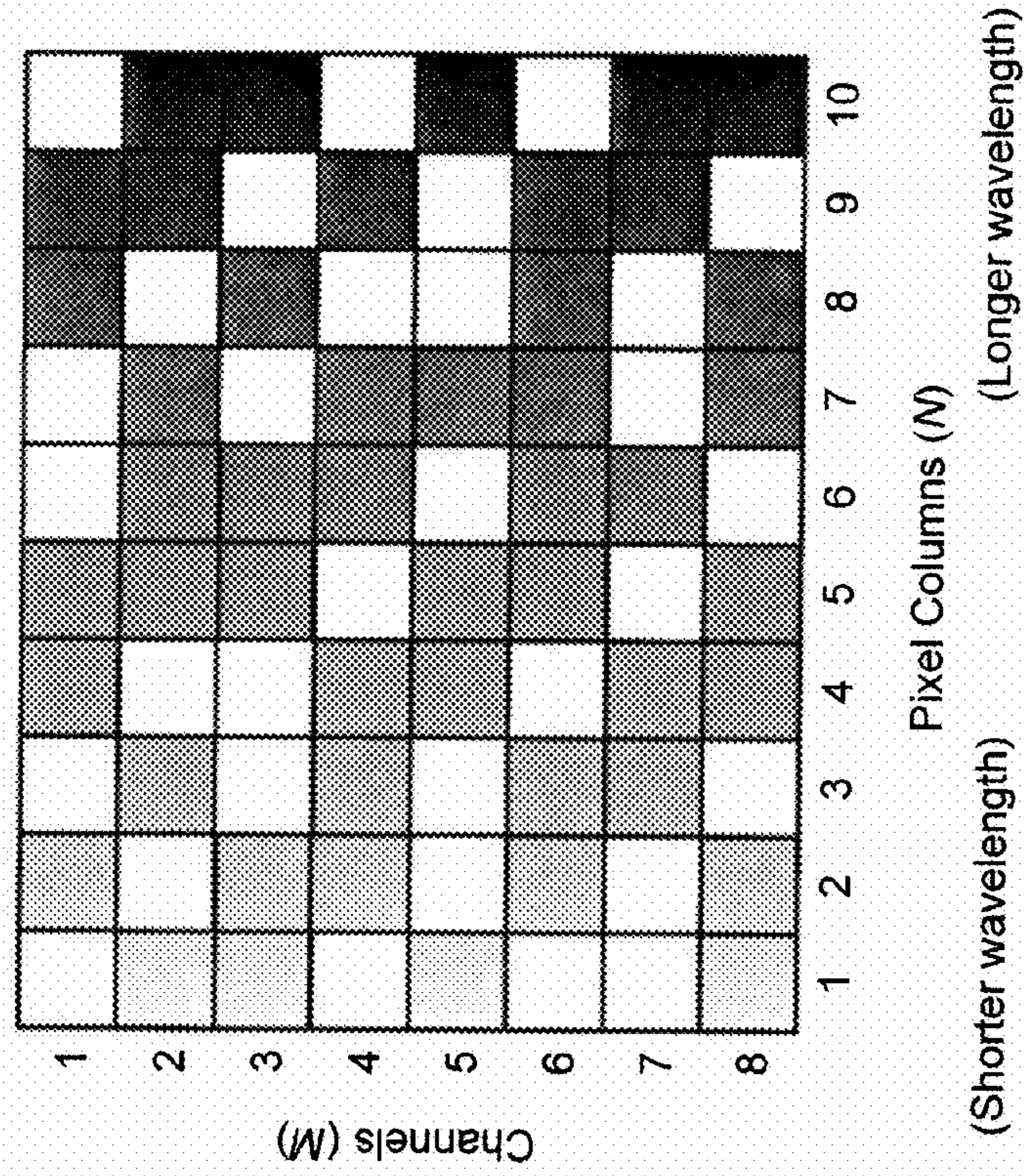


FIG. 6B

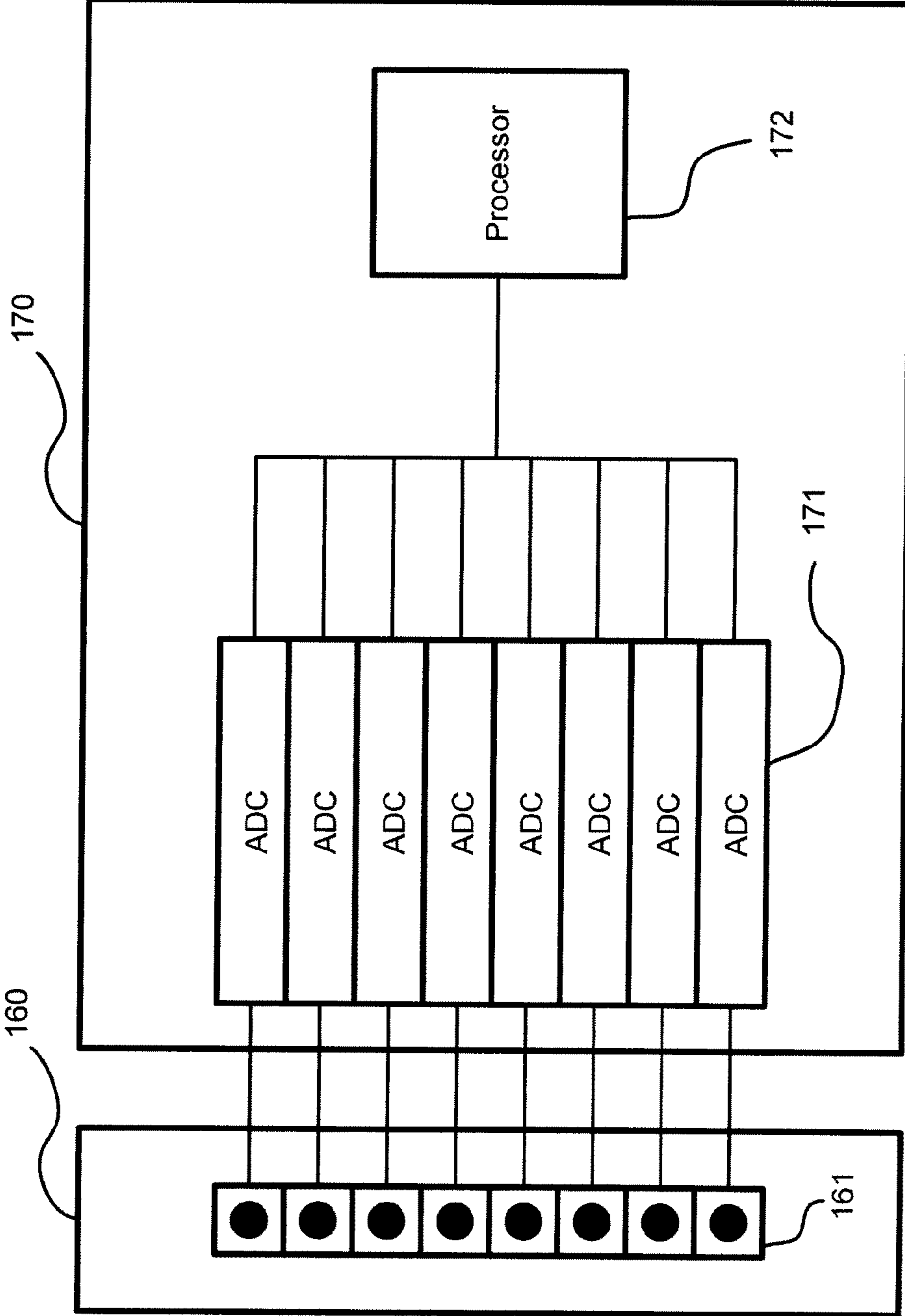


FIG. 7

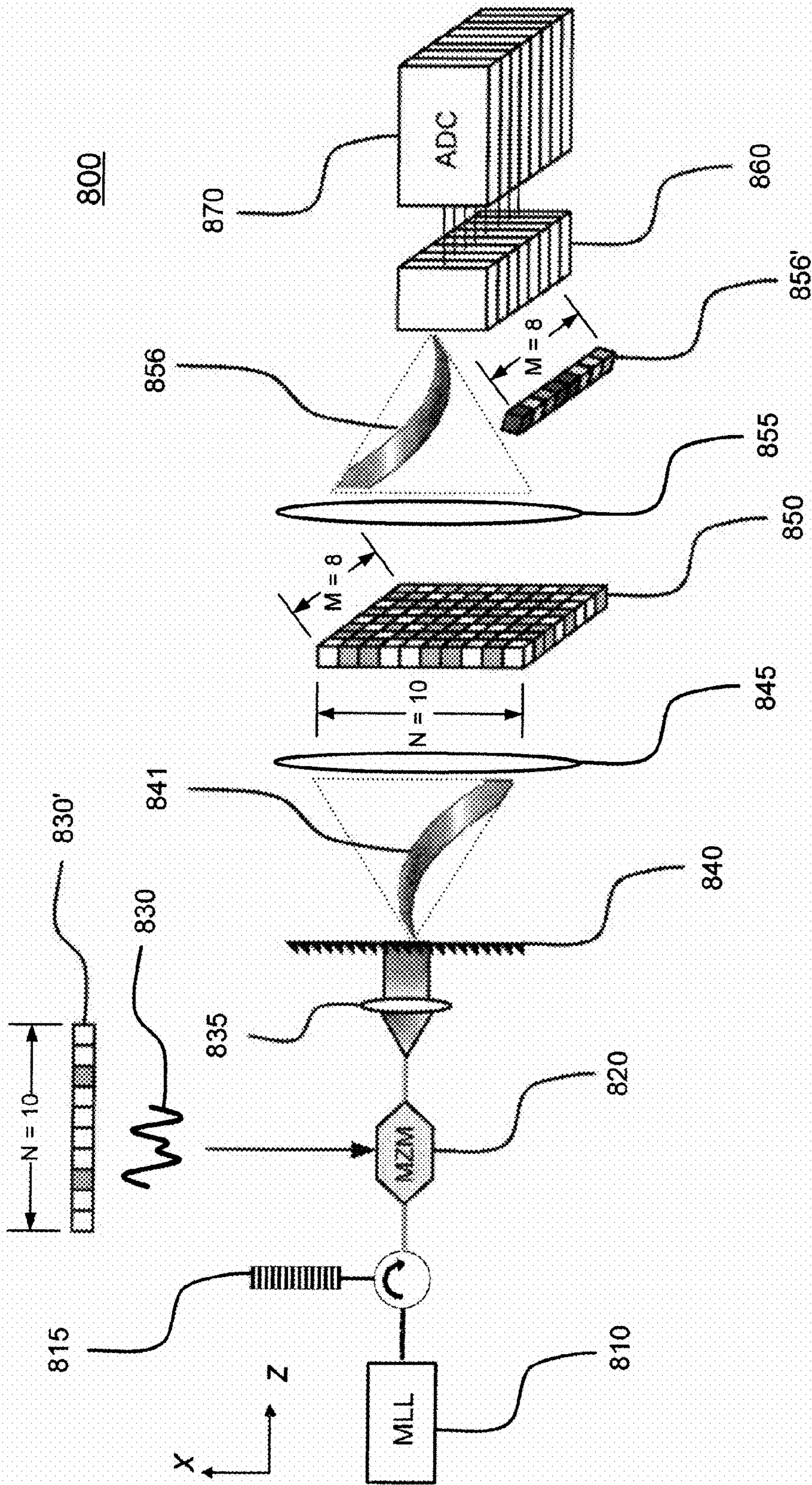


FIG. 8

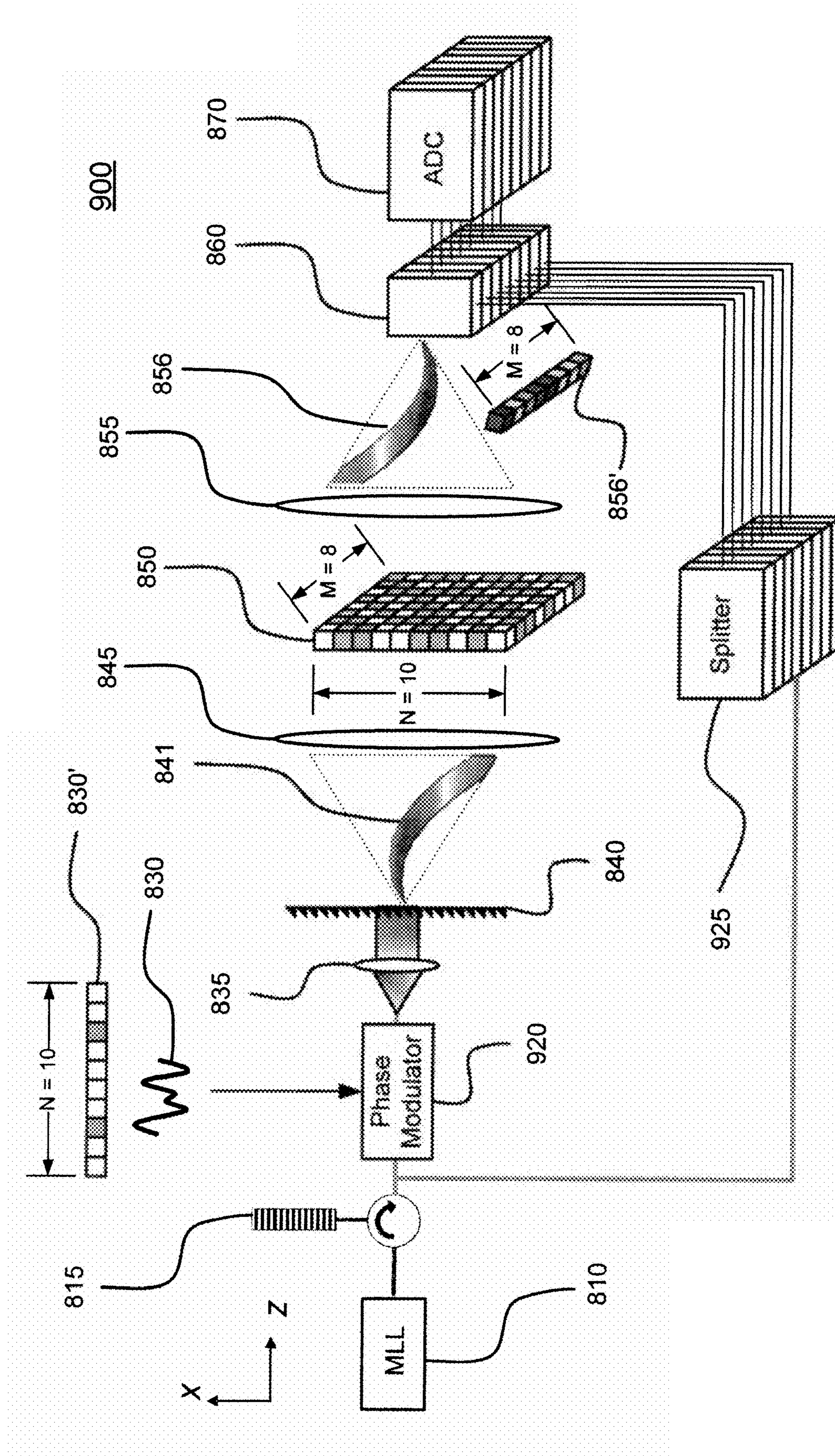


FIG. 9

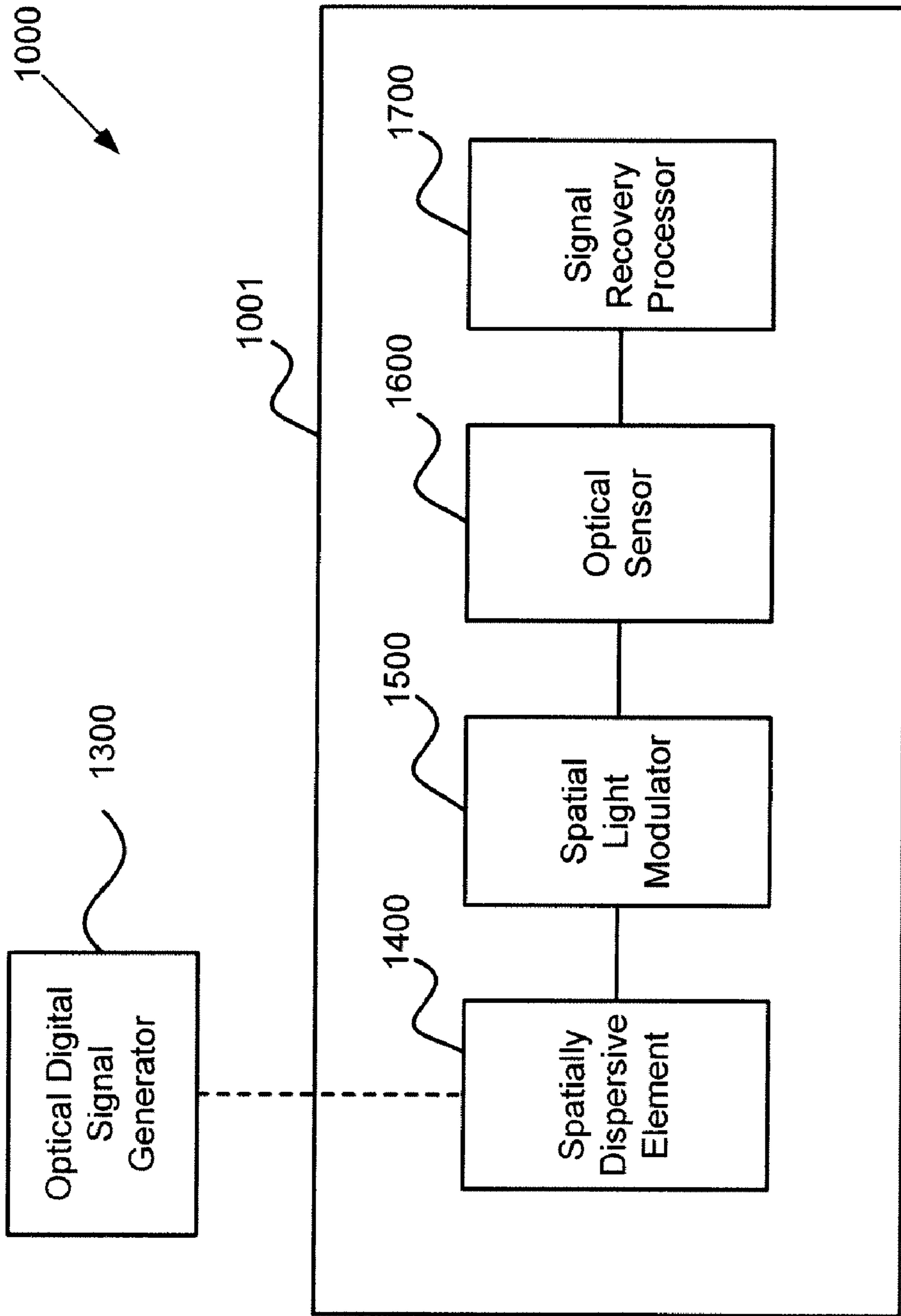


FIG. 10

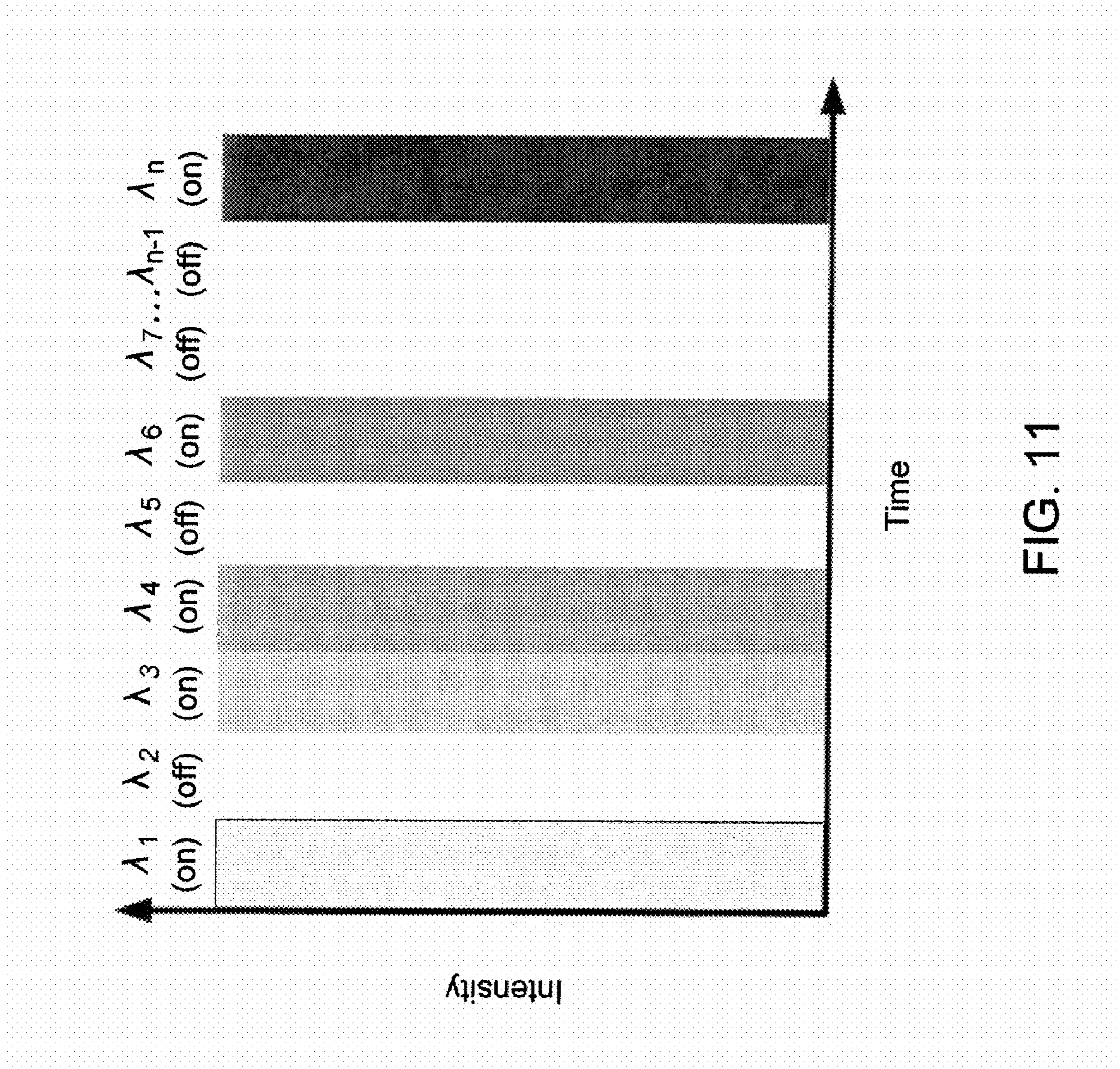


FIG. 11

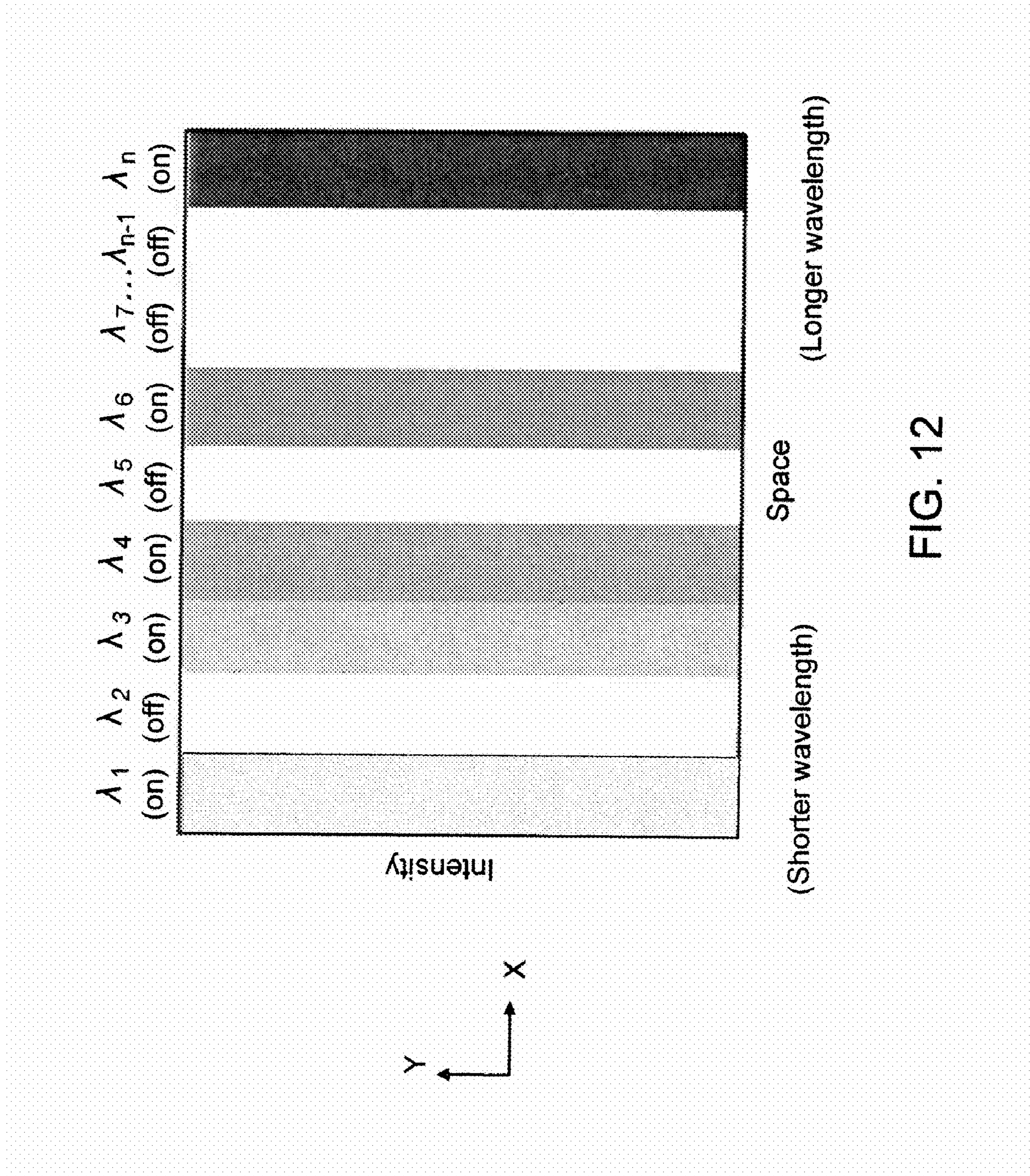


FIG. 12

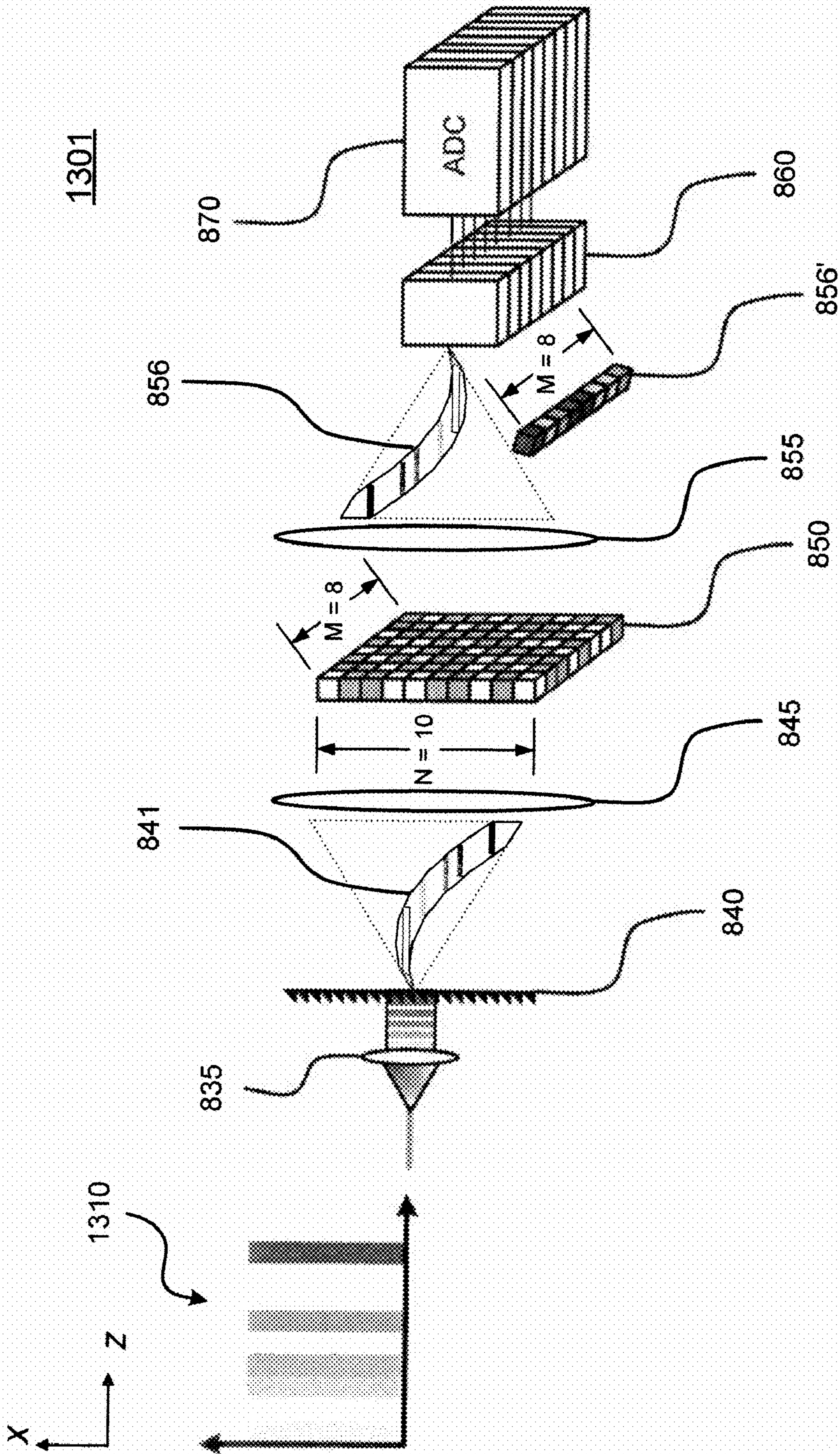


FIG. 13

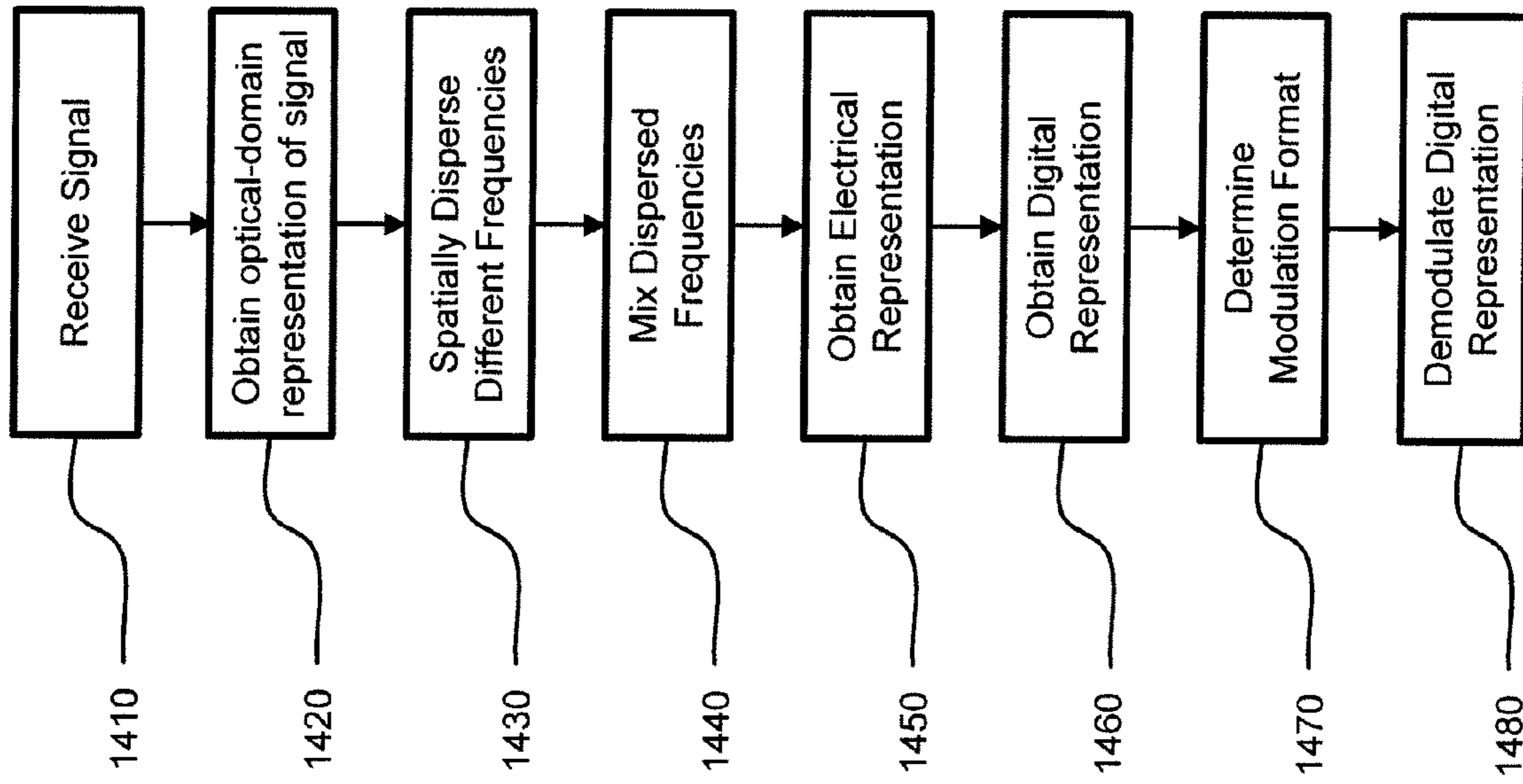


FIG. 14

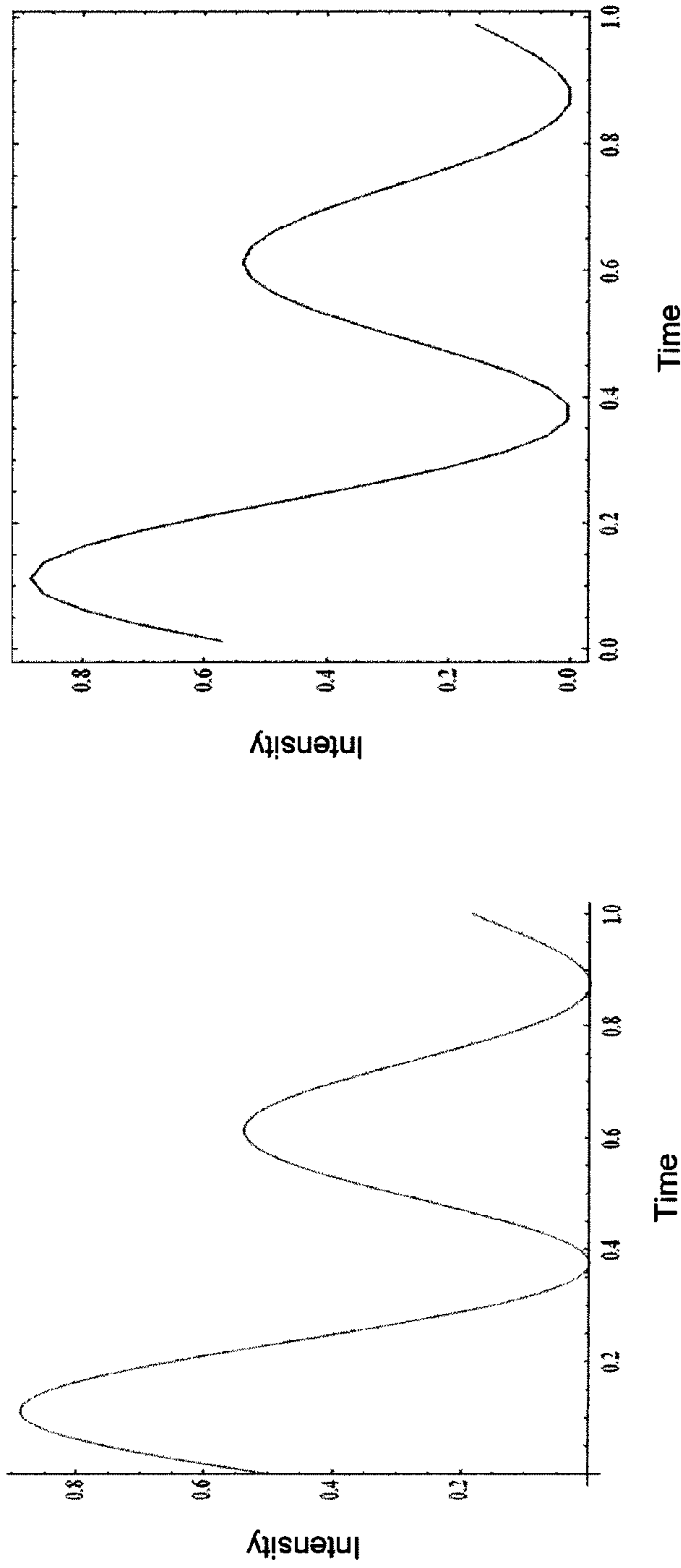


FIG. 15C

FIG. 15A

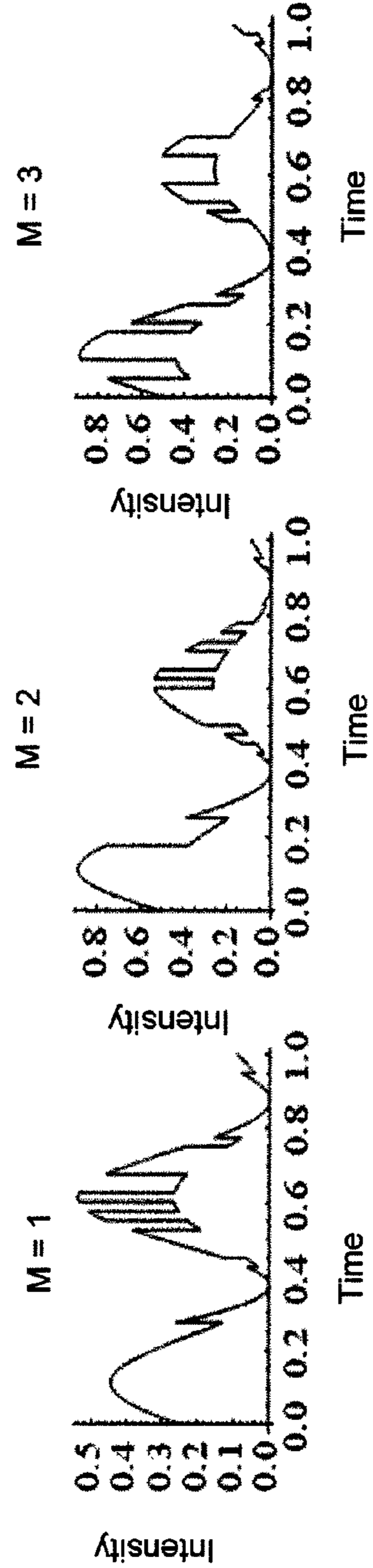


FIG. 15B

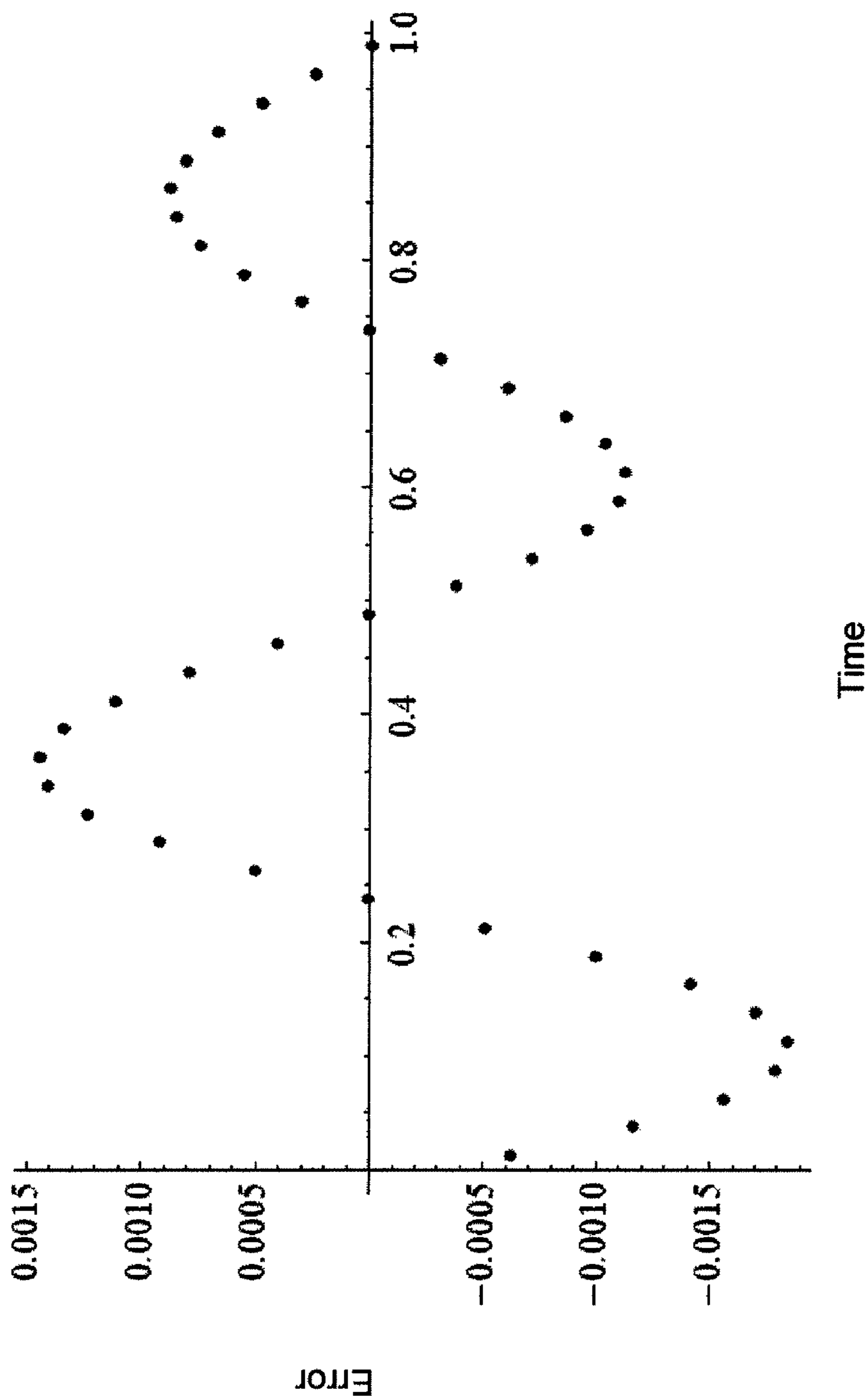


FIG. 15D

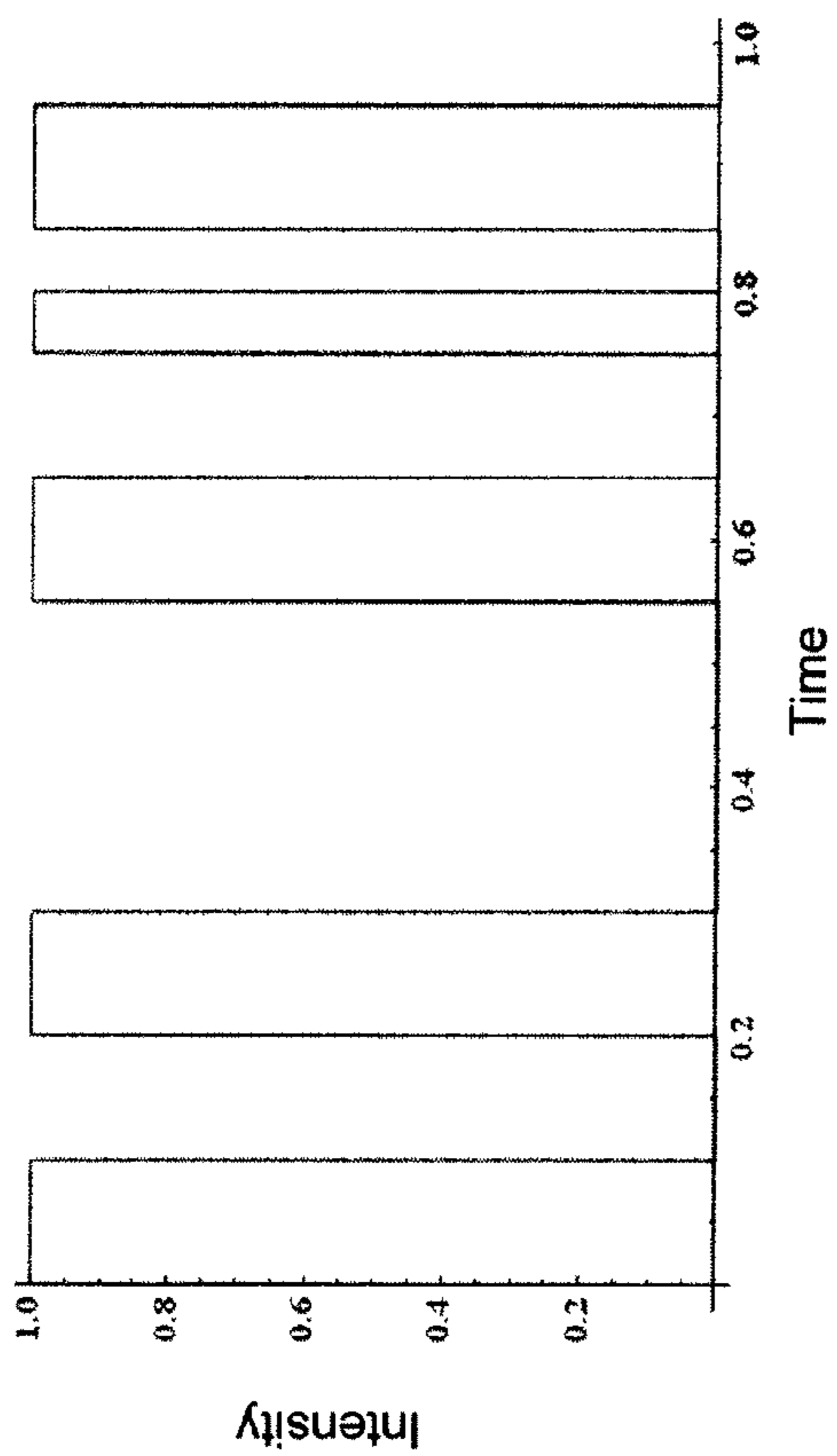


FIG. 16A

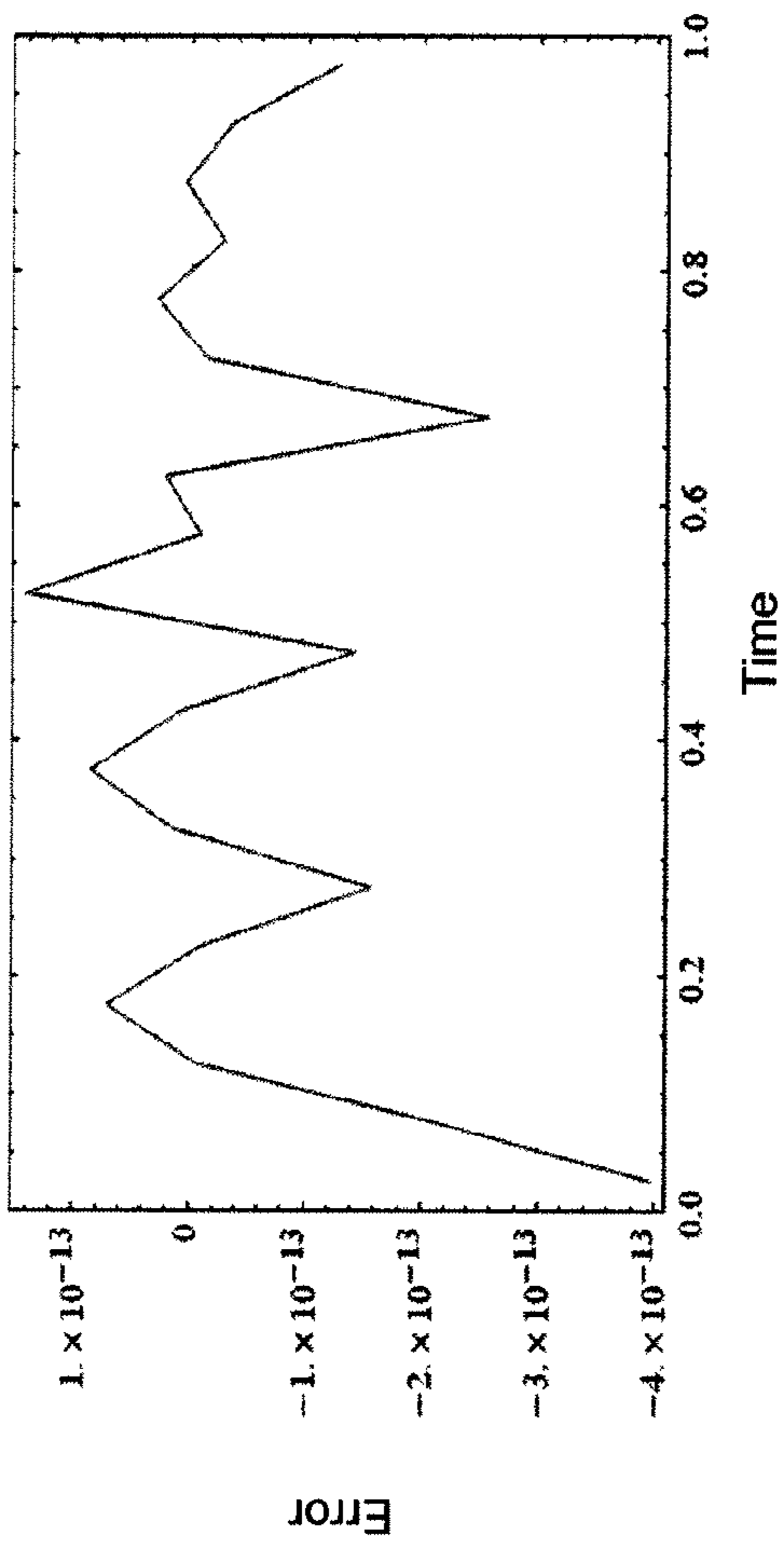


FIG. 16B

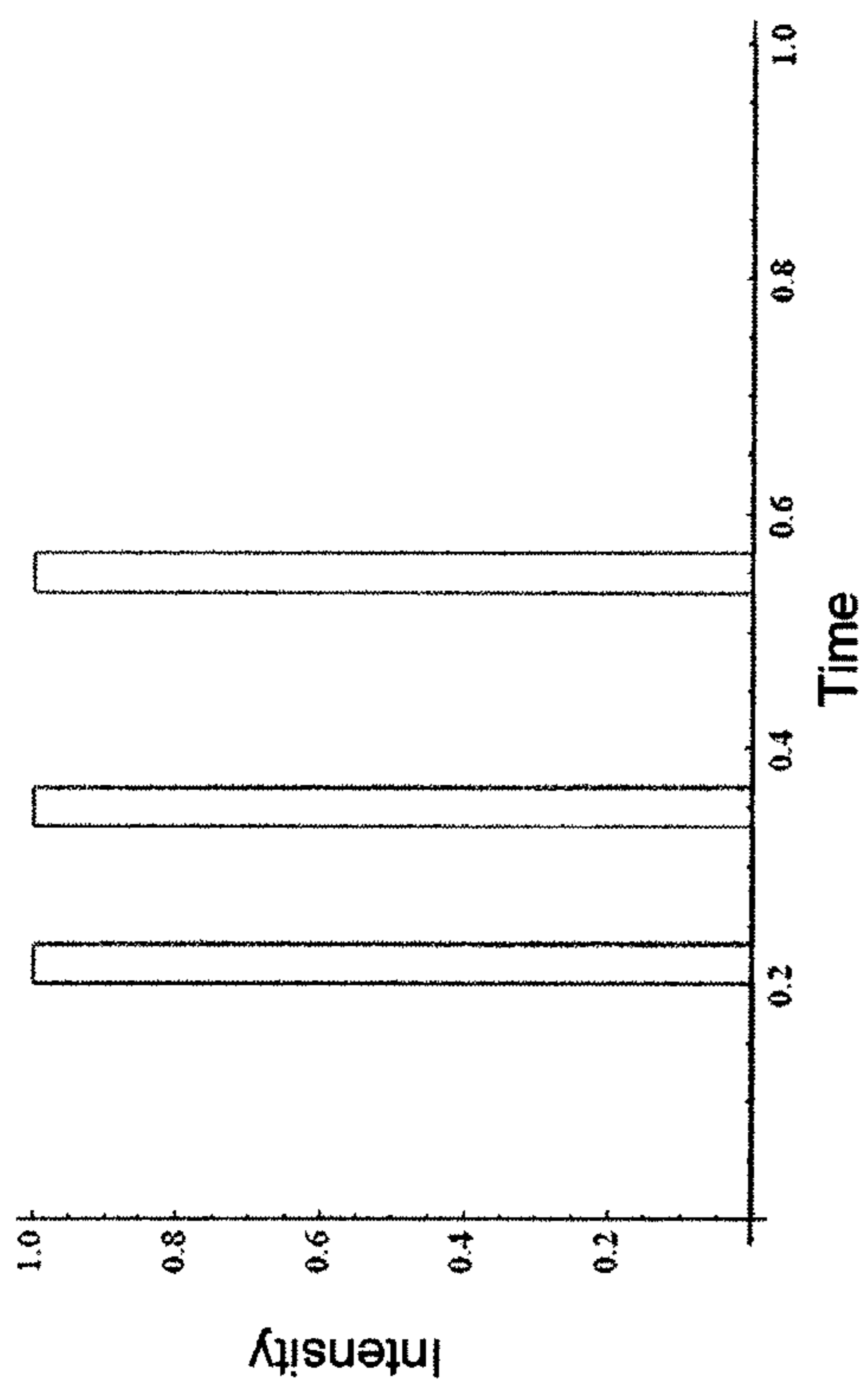


FIG. 17A

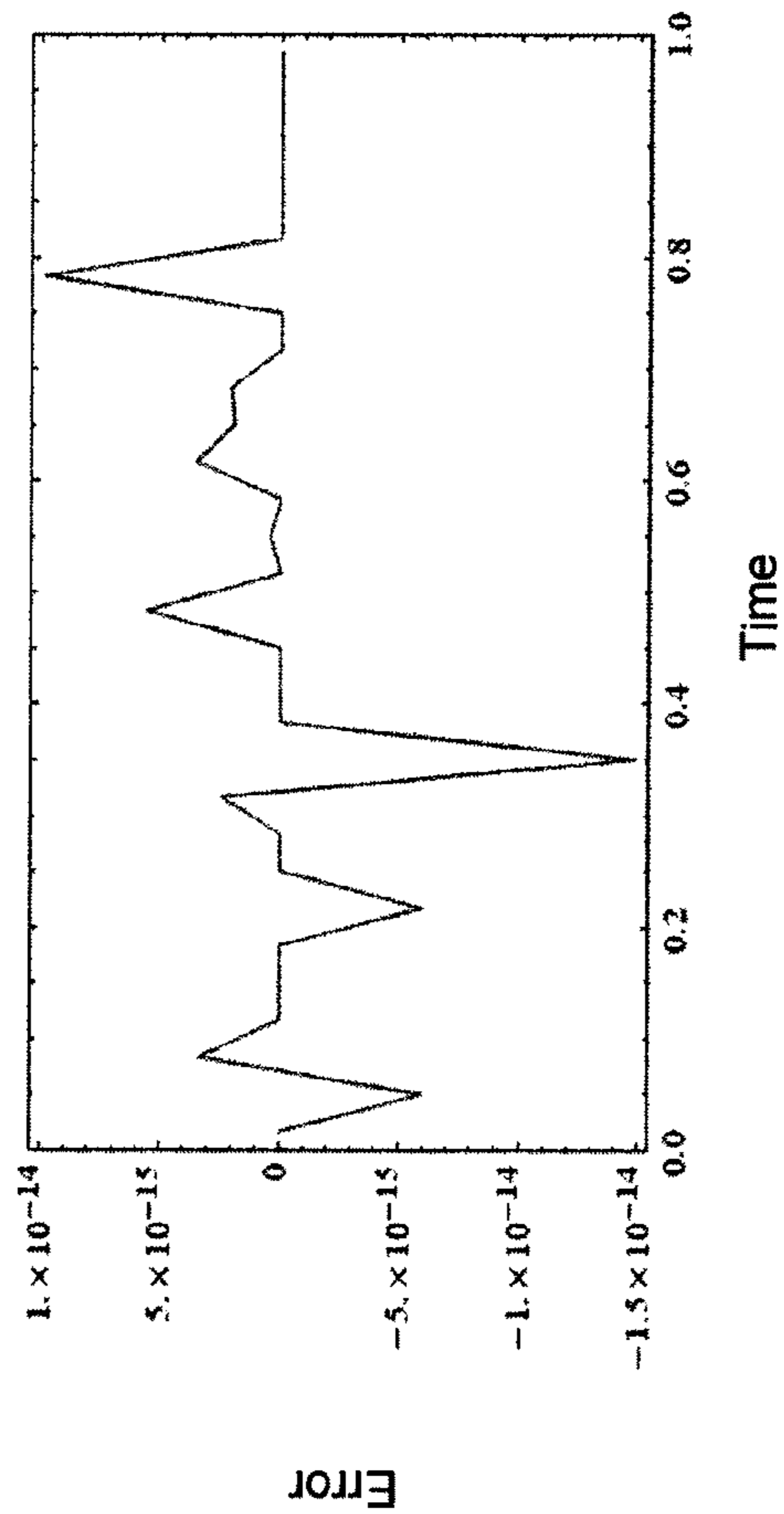


FIG. 17B

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SYSTEMS AND METHODS FOR CONVERTING WIDEBAND SIGNALS IN THE OPTICAL DOMAIN

STATEMENT OF GOVERNMENT INTEREST

This invention was made with Government support under Contract No. FA88002-09-C-0001 awarded by the Department of the Air Force. The Government has certain rights in the invention.

FIELD OF THE INVENTION

This application generally relates to systems and methods for converting wideband signals.

BACKGROUND OF THE INVENTION

An analog-to-digital converter (ADC) is a device that converts continuous analog signals to discrete digital numbers. Generally, an ADC samples an input signal at a predetermined sampling rate calculated using the Nyquist-Shannon Sampling Theorem. Under that theorem, perfect reconstruction of a continuous time signal may be obtained if the sampling rate is greater than twice the highest frequency of the signal. Sampling at twice the highest frequency may, however, not be possible, especially for wideband signals or the resolution (number of bits) obtained at this rate may not be sufficient. A wideband signal may be defined as a signal operating at a wide range of frequencies, e.g., above 1 GHz. For these reasons, previously-known ADCs may be inadequate to handle wideband applications in, for example, electronic warfare, radar, cognitive radio, signals intelligence, telecommunications, and signal sampling in space. Moreover, previously-known ADCs rely on high-speed, high-power electronics that may be cumbersome, power-hungry, and expensive.

SUMMARY OF THE INVENTION

Embodiments of the present invention provide systems and methods for converting wideband signals using optical-domain processing. Specifically, a received signal, e.g., a wideband signal, may be modulated in the optical domain so as to convert the received signal into a digital signal using, for example, commercially available, low cost, low data rate, low power analog-to-digital converters (ADCs).

In accordance with one aspect of the invention, a device for obtaining a digital representation of a received signal includes a spatially dispersive element that may be configured to spatially disperse optical frequencies in an optical-domain representation of the received signal; a spatial light modulator that may be configured to mix the dispersed optical frequencies by imposing a mixing matrix on an optical intensity of the dispersed optical frequencies; an optical sensor that may be configured to obtain an electrical representation of the mixed dispersed optical frequencies; and a signal recovery processor that may be configured to obtain a digital representation of the received signal based on the electrical representation and the mixing matrix.

In some embodiments, the signal recovery processor may be further configured to determine a modulation format of the digital representation and may demodulate the digital representation based on the modulation format.

In some embodiments, the received signal includes an optical digital signal. In some embodiments, the received signal

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includes an analog or digital signal. In some embodiments, the received signal includes a radio-frequency (RF) signal.

Some embodiments further include a chirped optical source that may be configured to generate a chirped repetitively pulsed optical signal and an optical modulator that may be configured to impose the analog RF signal on the chirped repetitively pulsed optical signal.

In some embodiments, the chirped optical source includes a laser and/or a dispersive optical element, such as a chirped fiber Bragg grating or a segment of dispersion-compensation fiber.

Some embodiments further include an analog signal receiver that may be configured to receive the analog radio-frequency signal.

In some embodiments, the optical modulator may be an intensity modulator. In other embodiments, the device further includes a splitter, and the optical modulator may be a phase modulator and the chirped repetitively pulsed optical signal may be divided into a first portion and a second portion. The first portion may travel to the phase modulator and the second portion may travel to the splitter. The splitter may be configured to split the second portion of the chirped repetitively pulsed optical signal based on the mixing matrix and transmit the split second portion of the chirped repetitively pulsed optical signal to interfere with the mixed dispersed optical frequencies of the first portion of the chirped repetitively pulsed optical signal from the spatial light modulator.

In some embodiments, the spatially dispersive element includes a diffraction grating.

In some embodiments, the spatially dispersive element includes a wavelength division demultiplexer.

In some embodiments, the spatial light modulator may be a partially transmissive optic that contains a fixed array of different transmission coefficients.

In some embodiments, the spatial light modulator may include channels and columns of pixels, each pixel being independently adjustable.

In some embodiments, the optical sensor may include an array of photodiodes. The photodiodes may include a low-pass filter.

In some embodiments, the signal recovery processor includes an analog-to-digital converter.

Some embodiments further include a display unit that may display the digital representation of the received signal.

In accordance with another aspect of the invention, a method for obtaining a digital representation of a received signal includes obtaining an optical-domain representation of the received signal; spatially dispersing optical frequencies in the optical-domain representation; mixing the dispersed optical frequencies by imposing a mixing matrix on an optical intensity of the dispersed optical frequencies; obtaining an electrical representation of the mixed dispersed optical frequencies; and obtaining a digital representation of the signal based on the electrical representation and the mixing matrix.

Some embodiments further include determining a modulation format of the digital representation and may include demodulating the digital representation based on the modulation format.

In some embodiments, receiving the signal includes receiving an optical digital and/or radio-frequency signal.

In some embodiments, receiving the signal includes generating a chirped repetitively pulsed optical signal and modulating the chirped repetitively pulsed optical signal by imposing an analog signal on the chirped repetitively pulsed optical signal.

In some embodiments, generating a chirped repetitively pulsed optical signal includes generating a chirped repetitively pulsed optical signal with a laser.

In some embodiments, generating a chirped repetitively pulsed optical signal includes generating a chirped repetitively pulsed optical signal by dispersing a femtosecond (fs) class laser pulse with a dispersive optical component. The femtosecond class laser pulse may be in the range of 1 fs to 1000 fs at full-width half-maximum (FWHM), and may be within 10 fs to 100 fs FWHM.

In some embodiments, spatially dispersing frequencies includes spatially dispersing the frequencies with a diffraction grating.

In some embodiments, mixing the dispersed optical frequencies includes mixing the dispersed optical frequencies with a spatial light modulator.

In some embodiments, obtaining an electrical representation includes obtaining an electrical representation with an array of photodiodes.

In some embodiments, obtaining a digital representation includes converting the electrical representation from an analog representation to a digital representation.

In some embodiments, obtaining the digital representation includes recovering the signal based on the digital representation and the mixing matrix.

Some embodiments further include displaying the digital representation of the signal.

BRIEF DESCRIPTION OF THE DRAWINGS

FIG. 1 schematically illustrates an exemplary device for obtaining a representation of a signal in the optical domain, according to some embodiments of the present invention.

FIG. 2A is a plot illustrating the temporal variations in intensity of three exemplary chirped repetitively pulsed optical signals that may be generated by a chirped optical source.

FIGS. 2B-2D are plots illustrating temporal variations in wavelength of three exemplary chirped repetitively pulsed optical signals that may be generated by a chirped optical source, e.g., the temporal wavelength variations of the three chirped repetitively pulsed optical signals illustrated in FIG. 2A.

FIG. 3 schematically illustrates an exemplary optical modulator that is an intensity modulator configured to impose an analog signal on the chirped repetitively pulsed optical signal, according to some embodiments of the invention.

FIG. 4 is a plot illustrating a temporal intensity profile of an exemplary modulated chirped repetitively pulsed optical signal from an optical modulator.

FIG. 5 illustrates exemplary dispersed optical frequencies in a modulated chirped repetitively pulsed optical signal from a spatially dispersive element.

FIG. 6A illustrates the exemplary dispersed optical frequencies from FIG. 5 imposed on a grid of M channels by N pixel columns.

FIG. 6B illustrates the exemplary dispersed optical frequencies from FIG. 6A after imposing a mixing matrix on an optical intensity of the frequencies using a grid of M channels by N pixel columns.

FIG. 7 illustrates an exemplary optical sensor and an exemplary signal recovery processor.

FIG. 8 illustrates an exemplary apparatus for obtaining a representation of an analog signal.

FIG. 9 illustrates an exemplary apparatus for obtaining a representation of an analog signal that is a variation of the apparatus from FIG. 8.

FIG. 10 schematically illustrates an exemplary device for obtaining a representation of an optical digital signal in the optical domain, according to some embodiments of the present invention.

FIG. 11 is a plot illustrating a temporal intensity profile of an exemplary optical digital signal.

FIG. 12 illustrates exemplary dispersed optical frequencies in the optical digital signal of FIG. 11 after traveling through a spatially dispersive element.

FIG. 13 illustrates an exemplary apparatus for obtaining a representation of an optical digital signal.

FIG. 14 illustrates an exemplary method for obtaining a representation of a signal, according to some embodiments of the present invention.

FIG. 15A is a plot illustrating the intensity of an exemplary analog radio-frequency signal as input to the device.

FIG. 15B is three plots illustrating the intensity of three optical signals over normalized time after transmission through separate channels of a mixing matrix.

FIG. 15C is a plot illustrating the digital representation of the analog signal of FIG. 15A as digitized by the device using low rate ADCs.

FIG. 15D is a plot illustrating the difference between the signal intensity of the digital representation in FIG. 15C and the signal intensity of the analog signal of FIG. 15A.

FIG. 16A is a plot illustrating the intensity of an exemplary square-wave radio-frequency signal as input to the device.

FIG. 16B is a plot illustrating the difference between the signal intensity of the digital representation of the received signal as digitized by the device and the signal intensity of the signal of FIG. 16A.

FIG. 17A is a plot illustrating the intensity of an exemplary sparse square-wave radio-frequency signal as input to the device.

FIG. 17B is a plot illustrating the difference between the signal intensity of the digital representation of the received sparse signal as digitized by the device and the signal intensity of the sparse signal of FIG. 17A.

DETAILED DESCRIPTION

Embodiments of the present invention include systems and methods for obtaining a digital representation of a received signal, e.g., a digital or analog radio-frequency (RF) signal, or an optical digital signal, using optical-domain processing. First, different frequencies of an optical-domain representation of the received signal may be spatially dispersed so as to produce a time/wavelength to space mapping of the signal, which prepares the optical frequencies for mixing. The dispersed optical frequencies of the optical-domain representation then may be mixed in the optical domain by imposing a mixing matrix on an optical intensity of the dispersed optical frequencies, for example by varying the transmitted intensities and/or phases of different portions of the dispersed optical frequencies using a spatial light modulator (SLM). A digital representation of the received signal may then be obtained from the mixed frequencies using optical sensors coupled to a suitable signal recovery processor, e.g., as described in greater detail herein.

Previously-known signal processing techniques rely solely on high-speed, high power electronics to obtain a digital representation of a signal. In accordance with the principles of the present invention, a spatial light modulator is used to impose a mixing matrix on the optical intensities of dispersed optical frequencies of an optical-domain representation of an analog or digital signal, thereby enabling the received signal to be converted into a digital signal using, for example, com-

mercially available, low cost, low data rate, low power analog-to-digital converters (ADCs). The device disclosed herein may sample the received signal at a sampling rate at least M times greater than the sampling rate of a previously-known electronic ADC, where M is the number of channels in the spatial light modulator. This functionality may be especially important for converting wideband signals, e.g., signals operating at frequencies above 1 GHz, because previously-known ADCs may be inadequate to handle wideband applications in, for example, electronic warfare, radar, cognitive radio, signals intelligence, telecommunications, and signal sampling in space.

As described in greater detail below, the device further may be configured to determine the modulation format of the digital representation of the received signal after analog-to-digital conversion. Further still, the device may demodulate the digital representation based on the determined modulation format.

As discussed in greater detail herein, the received signal may be, for example, a radio-frequency signal, which may be an analog or digital signal, or may be an optical digital signal. Embodiments of the invention useful for obtaining digital representations of radio-frequency signals will first be described, and embodiments of the invention useful for obtaining digital representations of optical digital signals will then be described.

Radio-Frequency Signal

FIG. 1 schematically illustrates exemplary device 100 for obtaining a digital representation of a received signal using optical-domain processing, according to some embodiments of the present invention. Device 100 includes chirped optical source 110, optical modulator 120, spatially dispersive element 140, spatial light modulator 150, optical sensor 160, and signal recovery processor 170. In some embodiments, device 100 includes housing 101 configured to hold at least chirped optical source 110, optical modulator 120, spatially dispersive element 140, spatial light modulator 150, optical sensor 160, and signal recovery processor 170 as illustrated in FIG. 1. In other embodiments, device 100 includes more than one housing (not shown), each housing configured to hold at least one structure in device 100.

Chirped optical source 110 may be configured to generate a chirped repetitively pulsed optical signal. A chirped repetitively pulsed optical signal is an optical pulse that has a relatively constant intensity as a function of time and has temporal wavelength variations. FIG. 2A is a plot illustrating the temporal variations in intensity of three exemplary chirped repetitively pulsed optical signals that may be generated by chirped optical source 110. The plurality of chirped repetitively pulsed optical signals has a substantially continuous overall intensity in time as represented by $I_{overall}$. Temporal intensity profiles 210, 220, 230 illustrate three chirped repetitively pulsed optical signals that begin at times t_1 , t_2 , t_3 , respectively. Once a chirped repetitively pulsed optical signal begins, its intensity increases over time until the intensity levels off at a peak, e.g., at $I_{overall}$. The chirped repetitively pulsed optical signals may have substantially the same energy as one another and may overlap slightly in the temporal domain. For example, temporal intensity profile 210 begins to decrease after time t_2 , when temporal intensity profile 220 begins. Temporal intensity profiles 210 and 220 overlap slightly after time t_2 , after which temporal intensity profile 210 decreases to zero and temporal intensity profile 220 increases to $I_{overall}$.

FIG. 2B is a plot illustrating the temporal variations in wavelength of three exemplary linear, positively chirped repetitively pulsed optical signals that may be generated by

chirped optical source 110, e.g., the temporal wavelength variations of the three chirped repetitively pulsed optical signals illustrated in FIG. 2A. Temporal wavelength profiles 211, 221, 231 illustrate three chirped repetitively pulsed optical signals that begin at times t_1 , t_2 , t_3 , respectively, overlap slightly in the temporal domain, and have substantially uniform intensities. To generate temporal wavelength profiles 211, 221, 231, a grating, for example, may be arranged so that the short-wavelength component of the optical pulse travels a shorter path than does the long-wavelength component. After transmission through or reflection from the grating, the optical pulse becomes positively chirped, that is, the long-wavelength component lags behind the short-wavelength component in time.

FIG. 2C is a plot illustrating the temporal variations in wavelength of three exemplary linear, negatively chirped repetitively pulsed optical signals that may be generated by chirped optical source 110, e.g., the temporal wavelength variations of the three chirped repetitively pulsed optical signals illustrated in FIG. 2A. Temporal wavelength profiles 211', 221', 231' illustrate three chirped repetitively pulsed optical signals that begin at times t_1 , t_2 , t_3 , respectively, overlap slightly in the temporal domain, and have substantially uniform intensities. To generate temporal wavelength profiles 211', 221', 231', a grating, for example, may be arranged so that the long-wavelength component of the optical pulse travels a shorter path than does the short-wavelength component. After transmission through or reflection from the grating, the optical pulse becomes negatively chirped, that is, the short-wavelength component lags behind the long-wavelength component in time.

FIG. 2D is a plot illustrating the temporal variations in wavelength of three exemplary nonlinear, positively chirped repetitively pulsed optical signals that may be generated by chirped optical source 110, e.g., the temporal wavelength variations of the three chirped repetitively pulsed optical signals illustrated in FIG. 2A. Temporal wavelength profiles 211'', 221'', 231'' illustrate three chirped repetitively pulsed optical signals that begin at times t_1 , t_2 , t_3 , respectively, overlap slightly in the temporal domain, and have substantially uniform intensities. When the chirped repetitively pulsed optical signal is nonlinear, the angle of diffraction from spatially dispersive element 140 (described further below) may be nonlinear. Still, device 100 may be used when chirped optical pulses are nonlinear if spatial light modulator 150 (described further below) has a high resolution to compensate for the nonlinear angle of diffraction.

As shown in FIG. 1, chirped optical source 110 may include, for example, any suitable laser, e.g., a mode-locked laser, fiber laser, titanium-doped sapphire (Ti:Sapphire) solid-state laser, or dye laser. In some embodiments, the laser may be configured so as to generate chirped repetitively pulsed optical signals without the need for an additional component. Alternatively, chirped optical source 110 may further include one or more optical components for dispersing and hence chirping a pulse generated by the laser. Such an optical component may include, for example, a grating such as a chirped fiber Bragg grating (FBG), a dispersion compensating fiber (DCF), or a standard optical fiber. The laser may be, for example, bandwidth-limited, so as to produce ultrafast pulses (e.g., 1 picosecond Full Width at Half Maximum (FWHM) or less) at a high bandwidth (e.g., 10 nm FWHM or more), and the dispersive optical component may be configured to temporally disperse the bandwidth of those pulses such that the pulses temporally overlap with one another, resulting in a substantially uniform overall intensity $I_{overall}$ as illustrated in FIG. 2A. The laser may have, for example, a

repetition rate of 100 MHz, resulting in a period (time difference between t_2 and t_1 , and between t_3 and t_2) of 10 ns. In some embodiments, a chirped repetitively pulsed optical signal is generated by dispersing a femtosecond (fs) class laser pulse with a dispersive optical component. The femtosecond class laser pulse may be in the range of 1 fs to 1000 fs full-width at half-maximum (FWHM), and may be within 10 fs to 100 fs FWHM.

In one illustrative embodiment, chirped optical source **110** may be a theta laser such as disclosed in Shinwook Lee et al., *Extreme Chirped Pulse Oscillator (XCPO) Using a Theta Cavity Design*, IEEE Photonics Technology Letters, Vol. 18, No. 7, 799-801 (Apr. 1, 2006), the entire contents of which are incorporated by reference herein. The theta laser disclosed in Lee includes two optical circulators, an intensity modulator, an output coupler, a bandpass filter, a polarization controller, a semiconductor optical amplifier, an electric comb generator, and chirped FBG. The theta laser may be used to generate a chirped optical pulse.

Signal generator **130** may generate a radio-frequency signal, e.g., an analog radio-frequency or digital radio-frequency signal. The characteristics of the radio-frequency signal may be unknown. Signal generator **130** may be any device capable of generating a radio-frequency signal and may be remote from device **100**. For simplicity, generating an analog signal will be described below. The analog signal may be sparse under a known transformation, e.g., a Fourier or wavelet transform. In the frequency domain, a sparse signal is defined to be a signal that consists of a relatively small number of narrowband transmissions spread across a relatively wide spectrum range. A sparse signal may be represented by a vector, e.g., a vector having dimension $N \times 1$, having a relatively small number of nonzero elements.

After the analog signal is generated by signal generator **130**, the analog signal is received by any structure capable of receiving an analog signal, e.g., an antenna (not shown). In some embodiments described further below, device **100** includes the analog signal receiver which may be disposed within optical modulator **120**. In other embodiments, the analog signal receiver is disposed outside of device **100** and operatively coupled to device **100** such that the analog signal may be transmitted to optical modulator **120**.

Optical modulator **120** may be configured to impose the RF analog signal on the chirped repetitively pulsed optical signal generated by chirped optical source **110**. For example, FIG. 3 schematically illustrates an exemplary optical modulator **120** that is an intensity modulator configured to impose an RF analog signal on the intensity of the chirped repetitively pulsed optical signal, according to some embodiments of the invention. Optical modulator **120** illustrated in FIG. 3 includes input optical fiber **121**, electrodes **125**, voltage generator **126**, analog signal receiver **127**, and output optical fiber **129**. A chirped repetitively pulsed optical signal from chirped optical source **110** is introduced to optical modulator **120** through input optical fiber **121**. Junction **122** divides the chirped repetitively pulsed optical signal into two portions and respectively guides the portions into sections **123** and **124**. Electrodes **125** are positioned on either side of sections **123**, **124**. Voltage generator **126** may be programmed to independently apply voltages to different pairs of electrodes **125** so as to change the phase of the chirped repetitively pulsed optical signal traveling through the section adjacent to that pair. For example, voltage generator **126** may apply voltages proportional to the analog signal generated by signal generator **130** and received by analog signal receiver **127**. Analog signal receiver **127** may be operatively coupled to voltage

generator **126** and may be any structure capable of receiving an analog signal, e.g., an antenna.

In optical modulator **120** illustrated in FIG. 3, the two portions of the chirped repetitively pulsed optical signal in sections **123**, **124** may recombine at junction **128** where they interfere with one another. Because the relative phase of the chirped repetitively pulsed optical signal portions traveling through sections **123**, **124** may be controlled via voltage generator **126**, the intensity of the chirped repetitively pulsed optical signal at junction **128** may be modulated based on the analog signal. For example, if the portion of chirped repetitively pulsed optical signal in section **123** is phase delayed by an even multiple of π relative to that in section **124**, then the two portions of chirped repetitively pulsed optical signal will constructively interfere with each other, yielding maximum brightness. Or, for example, if the portion of the chirped repetitively pulsed optical signal in section **123** is phase delayed by an odd multiple of π relative to that in section **124**, then the two portions will completely interfere with each other, yielding minimal brightness. The output of optical modulator **120** is the analog signal imposed as an intensity modulation on the chirped repetitively pulsed optical signal, referred to as the modulated chirped repetitively pulsed optical signal. This output is coupled into a single output optical fiber **129**. Configurations such as that illustrated in FIG. 3 may be referred to as a Mach-Zehnder modulator (MZM). Other modulators, such as absorptive modulators based on the Franz-Keldysh effect or the quantum confined Stark effect, or other interferometric modulators, may also suitably be used.

FIG. 4 is a plot illustrating temporal intensity profile **410** of an exemplary modulated chirped repetitively pulsed optical signal from optical modulator **120**. Temporal intensity profile **410** is modulated so as to have varying intensities throughout the chirped repetitively pulsed optical signal based on the imposed analog signal. In this example, the optical pulse is positively chirped, that is, the long-wavelength component lags behind the short-wavelength component in time.

Referring back to FIG. 1, spatially dispersive element **140** is configured to spatially disperse different optical frequencies in the modulated chirped repetitively pulsed optical signal from optical modulator **120**. Spatially dispersive element **140** produces a time/wavelength to space mapping of the modulated chirped repetitively pulsed optical signal. The dispersive optical element, e.g., a chirped fiber Bragg grating or a segment of dispersion-compensation fiber, that may be included in optical source **110** may be engineered to complement spatially dispersive element **140** so as to provide a linear time/wavelength to space mapping. For example, the dispersive optical component may create timing errors on the optical pulse that are identical from pulse to pulse. If timing errors are detected, the spatially dispersive element may be calibrated to eliminate the timing errors using suitable techniques known in the art. Non-limiting examples of spatially dispersive element **140** include diffraction grating, e.g., transmission grating or reflection grating, a wavelength division demultiplexing (WDM) device, and a prism.

FIG. 5 illustrates an exemplary arrangement of dispersed optical frequencies in a modulated chirped repetitively pulsed optical signal that is dispersed by spatially dispersive element **140**. The frequencies are dispersed such that shorter wavelength frequencies, represented by light gray, are disposed on one end of the modulated chirped repetitively pulsed optical signal relative to the x-axis, and the wavelength of the frequencies increases along the x-axis up to longer wavelength

frequencies, represented by dark gray. The wavelength of the modulated chirped repetitively pulsed optical signal remains uniform relative to the y-axis.

Referring back to FIG. 1, spatial light modulator **150** may be configured to receive the dispersed optical frequencies from spatially dispersive element **140**, and to impose a mixing matrix on an optical intensity of the dispersed optical frequencies. Spatial light modulator **150** may be a device that imposes some form of spatially-varying modulation, e.g., a phase or intensity modulation, on different portions of a beam of light. FIG. 6A illustrates the exemplary dispersed optical frequencies from FIG. 5 imposed on a grid of M channels by N pixel columns. In this example, there are eight channels and ten columns of pixels resulting in 80 pixels, and the longer wavelength portions are dispersed at the higher pixel column numbers. Each channel (M) receives frequencies with varying wavelengths, e.g., from shorter wavelengths to longer wavelengths. The number of channels (M) may be selected for wideband applications, and may include 1000 channels or more. Each pixel column (N) receives frequencies with wavelengths that do not vary greatly, e.g., pixel column 1 receives only short wavelength frequencies. Each pixel column (N) has M pixels that may be independently controlled by a computer-operated electronic driver which manipulates the pixel voltage, allowing the pixel voltage to be easily programmed and/or reprogrammed.

Spatial light modulator **150** mixes the dispersed optical frequencies by imposing a mixing matrix on an optical intensity of the dispersed optical frequencies. Specifically, spatial light modulator **150** may impose the mixing matrix by reducing or preventing selected light transmission of the dispersed optical frequencies by applying voltages to the individual pixels. Spatial light modulator **150** may be programmed to randomly prevent or reduce light transmission through certain pixels while never completely preventing light transmission of an entire pixel column (N). Spatial light modulator **150** may be programmed to prevent or reduce light transmission through the pixels by applying an appropriately chosen light transmission reduction coefficient between 0 and 1 to each of the selected pixels.

FIG. 6B illustrates the exemplary dispersed optical frequencies from FIG. 5 after spatial light modulator **150** imposes upon them a mixing matrix using the grid of M channels by N pixel columns illustrated in FIG. 6A. The white boxes represent pixels that completely or partially block light transmission of the dispersed optical frequencies, while the darker boxes represent pixels through which the dispersed optical frequencies are allowed to partially or substantially completely transmit. In the illustrated example, light transmission is completely blocked in the white boxes, meaning the chosen light transmission reduction coefficient is 0. In many embodiments, no column of pixels (N) is completely blocked by the mixing matrix, so that the mixed dispersed optical frequencies in FIG. 6B provide a useful representation of the dispersed optical frequencies in FIG. 5. In many embodiments, no row of the mixing matrix is identical to any other row of the mixing matrix.

Referring back to FIG. 1, spatial light modulator **150** may mix signals up to the maximum response Effective Input Bandwidth (EIB) for optical modulator **120**. Currently, optical modulators may modulate signals with an EIB up to approximately 100 GHz. As the maximum response for optical modulators increases in the future, the EIB of a signal that may be mixed by spatial light modulator **150** would increase.

Spatial light modulator **150** may be, for example, a fixed mask, a partially transmissive optic, or a programmable device such as a liquid crystal display (LCD) or a digital

micro-mirror device (DMD). The partially transmissive optic, e.g., transparency, plastic, and/or glass, may contain a fixed array of different transmission coefficients, e.g., via printing the transmission coefficients on the optic. The SLM may be configured, for example, so as to have a size of M Channels×N Pixel Columns. In one embodiment, the pixels of the SLM vary the intensity of light transmitted there-through. In one embodiment, the pixels of the SLM vary the intensity of the light reflected therefrom.

Referring again to FIG. 1, optical sensor **160** may be configured to obtain an electrical representation of the mixed dispersed optical frequencies. The mixed dispersed optical frequencies from spatial light modulator **150** may be transmitted, e.g., via a second spatially dispersive element such as a lens, a grating, or an Arrayed Waveguide Grating (AWG) (not shown), onto optical sensor **160**. Such an operation may be considered to be equivalent to multiplying the mixing matrix by the analog signal vector, resulting in a singular dot product. For example, a mixing matrix of dimension M×N may be multiplied by an analog signal of dimension N×1, resulting in a singular dot product of dimension M×1 that is received by optical sensor **160**. Optical sensor **160** then integrates the mixed dispersed optical frequencies in time to obtain an electrical representation of the mixed dispersed optical frequencies. Optical sensor **160** may be any device capable of converting light into current. Optical sensor **160** may be an inherently low-pass filter device. In some embodiments, optical sensor **160** includes at least one photodiode. In some embodiments, optical sensor includes a linear photodiode array matched to spatial light modulator **150** such that a focusing output grating and/or lens are not necessary.

FIG. 7 illustrates an exemplary optical sensor **160** and an exemplary signal recovery processor **170**. Optical sensor **160** includes linear photodiode array **161** that includes M photodiodes, where M is equal to the number of channels (M) in spatial light modulator **150**. In this example, there are eight channels in spatial light modulator **150** and thus, there are eight photodiodes in linear photodiode array **161**. The mixed dispersed optical frequencies from a channel (M) of spatial light modulator **150** are focused onto a corresponding element of linear photodiode array **161**. For example, the mixed dispersed optical frequencies from Channel 1 of spatial light modulator **150** are focused onto Photodiode 1 of linear photodiode array **161**. Linear photodiode array **161** then integrates the mixed dispersed optical frequencies as a function of time, e.g., so as to provide a vector of mixed dispersed optical frequencies having dimension M×1, thus providing an electrical representation of the mixed dispersed optical frequencies.

Referring back to FIG. 1, signal recovery processor **170** may be configured to obtain a digital representation of the analog signal based on the electrical representation obtained by optical sensor and further based on the mixing matrix. Signal recovery processor **170** may include any suitable device capable of converting analog signals into digital signals, e.g., an ADC. Additionally, signal recovery processor **170** may include any suitable device capable of signal recovery, e.g., a processor, and may include a memory device for storing the digital signals and/or the recovered signal. Signal recovery processor **170** receives an analog electrical representation of the mixed dispersed optical frequencies from optical sensor **160**, and converts this analog electrical representation into a digital representation of the mixed dispersed optical frequencies at a suitable sample rate. Signal recovery processor **170** then obtains a digital representation of the originally received signal based on the digital representation of the mixed dispersed optical frequencies and on the mixing

matrix. For example, if the mixing matrix is a square ($M=N$), signal recovery processor **170** may obtain the digital representation of the originally received signal by performing an operation that may be considered to be equivalent to multiplying the singular dot product from optical sensor **160** by the inverse of the mixing matrix. For example, a singular dot product of dimension $M \times 1$ (e.g., the electrical signal produced by the optical sensor) may be multiplied by the inverse of a mixing matrix of dimension $[M \times M]^{-1}$, resulting in a digital representation of the received signal, having dimension $M \times 1$.

Alternatively, if the mixing matrix is non-square ($M \neq N$), signal recovery processor **170** instead may obtain the representation of the received signal through techniques known in the art of compressive sensing, e.g., using suitable computer software. As will be familiar to those of ordinary skill in the art, compressive sensing is a methodology for preprocessing sparse data in the analog domain, e.g., an analog signal, prior to digitization in such a way that fewer digital resources, e.g., fewer ADCs, are required to obtain an accurate representation of the sparse data. See, for example, Candès et al., *An Introduction To Compressive Sampling*, IEEE Signal Processing Magazine, Vol. 25 No. 2, 21-30 (March 2008), the entire contents of which are incorporated by reference herein.

In some embodiments, the compressive sensing techniques employed in the present invention may use a new set of algorithms developed for sampling signals and images at rates much lower than the traditional Nyquist rate. See, for example, Loris, *L1Packv2: A Mathematica package for minimizing an l_1 -penalized functional*, pg. 1-17 (Aug. 20, 2008), the entire contents of which are incorporated by reference herein. Loris discloses the use in compressive sensing of a Mathematica® (Wolfram Research, Champaign, Ill.) package called L1 Packv2 that includes an algorithm called Find-Minimizer that may be used to obtain a representation of the received signal. The L1 Packv2 package, or any other suitable set of algorithms, may be used to obtain a digital representation of the originally received signal based on the mixing matrix and the electronic representation obtained by optical sensor **160**.

Signal recovery processor **170** may further determine the modulation format of the digital representation of the received signal, e.g., using suitable computer software. Non-limiting examples of analog modulation formats include amplitude modulation, double-sideband modulation, single-sideband modulation, vestigial sideband modulation, quadrature amplitude modulation, angle modulation, frequency modulation, pulse position modulation, and phase modulation.

Signal recovery processor **170** may demodulate the digital representation based on the determined modulation format, e.g., using suitable computer software. Signal recovery processor **170** may determine the modulation format and demodulate the determined modulation format after converting the electrical representation of the mixed dispersed optical frequencies from optical sensor **160** into a digital representation meaning device **100** may digitize the entire modulation format and then demodulate the digitized signal with, for example, suitable high speed digital demodulation software.

Signal recovery processor **170** illustrated in FIG. 7 includes linear ADC array **171** and processor **172**. Linear ADC array **171** includes M ADCs, and in this example M equals eight. Each ADC is operatively coupled to a corresponding photodiode in linear photodiode array **161** such that each ADC receives the corresponding electrical representation of the mixed dispersed optical frequencies. Each ADC

converts the received electrical representation from an analog representation to a digital representation. The digital representation is transmitted from linear ADC array **171** to processor **172** for signal recovery. Processor **172** obtains a representation of the analog signal based on the digital representation and the mixing matrix. Processor **172** may be any suitable processing unit capable of signal recovery, determining a modulation format, and/or demodulating a digital signal based on a demodulation format, e.g., a dedicated circuit, a computer, and may be configured to run a program for signal recovery, determining a modulation format, and/or demodulating a digital signal based on a demodulation format in suitable software, e.g., Matlab® (The MathWorks, Inc., Natick, Mass.) or Mathematica® (Wolfram Research, Champaign, Ill.). Processor **172** may obtain the representation of the received signal using known techniques in the art of signal recovery and digital demodulation.

Device **100** may sample the received signal at a sampling rate at least M times greater than the sampling rate of an electronic ADC used in the device, where M is the number of channels in the spatial light modulator. For example, a device using signal recovery processor **170** illustrated in FIG. 7 would be able to sample a received signal at a rate at least eight times greater than the sampling rate of each ADC in ADC array **171**. As a result, wideband signals may be converted into digital signals at signal recovery processor **170** using, for example, commercially available, low cost, low data rate (e.g., less than 500 Megasamples/second), low power (e.g., less than 0.1 picojoules per conversion step), ADCs.

Device **100** may include a display unit configured to display the representation of the received signal based on the digital representation and the mixing matrix. The display unit may be any device capable of displaying a signal representation.

Device **100** may be used to obtain a representation of a received signal, including wideband signals, in applications including, but not limited to, electronic warfare, radar, cognitive radio, signals intelligence, telecommunications, and signal sampling in space.

FIG. 8 illustrates an exemplary apparatus **800** for obtaining a representation of an RF signal, which in the illustrated embodiment is an analog signal, although the embodiment may also be used to obtain a representation of an RF digital signal. Apparatus **800** includes mode-locked laser (MLL) **810**, chirped fiber Bragg grating (FBG) **815**, Mach-Zehnder modulator (MZM) **820** which receives analog signal **830**, transmissive diffraction grating **840**, spatial light modulator (SLM) **850**, linear photodiode array **860**, and linear ADC array **870**. Mode-locked laser (MLL) **810** generates an optical pulse, which is in some embodiments time-bandwidth limited, and chirped FBG **815** chirps the optical pulse. As discussed above with respect to FIGS. 2A-2D, the optical pulse may be linearly or nonlinearly chirped, and may be positively or negatively chirped. Chirped FBG **815** further may be calibrated to eliminate any detected timing errors.

The chirped optical pulse travels via fiber from chirped FBG **815** to MZM **820**, which imposes RF signal **830** on the chirped repetitively pulsed optical signal by modulating the intensity of the chirped repetitively pulsed optical signal in accordance with temporal and frequency characteristics of analog signal **830**. Analog signal **830** may be generated by a remote apparatus and received by MZM **820** using any suitable means. Analog signal **830'** is a representation of analog signal **830** in vector form having dimension $N \times 1$. In this example, N equals ten. Analog signal **830'** is sparse, as represented by eight white squares and two gray squares,

because the signal contains a small number of significant frequencies (gray squares) relative to the band limit (N).

The modulated chirped repetitively pulsed optical signal travels from MZM **820** through an optical fiber and spreads out after it exits the fiber but before it reaches lens **835**. Lens **835** collimates the modulated chirped repetitively pulsed optical signal, such that the pulse is substantially collimated as it is incident on diffraction grating **840**. Diffraction grating **840** spatially disperses the different optical frequencies in the modulated chirped repetitively pulsed optical signal such that wavelengths vary along the N dimension, but not along the M dimension (referred to as dispersed optical frequencies **841**), where M is the number of channels/rows and N is the number of pixel columns in SLM **850**. In this example, M equals eight and N equals ten. Dispersed optical frequencies **841** travel through lens **845** which performs a spatial Fourier transform on the dispersed optical frequencies in the plane of SLM **850**.

SLM **850** imposes a mixing matrix on an optical intensity of dispersed optical frequencies **841**. The mixing matrix reduces or prevents light transmission of random portions of dispersed optical frequencies **841**, as represented by white boxes. Preferably, no column of pixels (N) is completely blocked. The mixing matrix may be adjusted and programmed using SLM **850**. Mixed dispersed optical frequencies **856** then travel through lens **855**, which focuses frequencies **856** onto linear photodiode array **860**. Lens **855** may be, for example, a cylindrical lens; in other embodiments, lens **855** may be replaced with another suitable optical component performing an analogous function, such as a grating, or an integrated optic component, e.g., an AWG. When analog signal **830'**, in the illustrated embodiment a vector of dimension 10×1, is multiplied by the mixing matrix (an 8×10 matrix), a vector of mixed dispersed optical frequencies **856'** having dimension 8×1 are obtained. Mixed dispersed optical frequencies **856** are a compressed version of dispersed optical frequencies **841**. For example, the highest box, M=1, of mixed dispersed optical frequencies **856'** contains the entire dispersed optical frequencies **841** from the highest channel, M=1, of SLM **850** in compressed form. Unlike analog signal **830**, which is sparse, mixed dispersed optical frequencies **856** are substantially all significant frequencies (represented by gray squares of varying shades). Further, mixed dispersed optical frequencies **856** are a useful representation of dispersed optical frequencies **841**.

Lens **855** focuses mixed dispersed optical frequencies **856** onto linear photodiode array **860**. There are eight photodiodes in linear photodiode array **860**, and each photodiode receives the corresponding portion of mixed dispersed optical frequencies **856** to generate an electrical representation based on the intensity of the light in frequencies **856**. For example, the highest box, M=1, of mixed dispersed optical frequencies **856'** is focused on the highest photodiode, M=1, on linear photodiode array **860**. Each photodiode integrates the corresponding mixed dispersed optical frequencies in time so as to obtain the electrical representation. The electrical representation travels to the corresponding one of eight ADCs in linear ADC array **870** where the electrical representation is converted from an analog representation to a digital representation. Because apparatus **800** may sample the received signal at a sampling rate at least M times greater than the sampling rate of each ADC in ADC array **870**, analog signal **830** may be converted into digital signals at linear ADC array **870** using eight commercially available, low cost, low rate, low power ADCs. The digital representation may then be sent to signal recovery using a process known in the art in order to obtain a digital representation of analog signal **830**.

Although the embodiments described above with respect to FIGS. **1-8** primarily utilize amplitude modulation of the chirped repetitively pulsed optical signal, phase modulation may also be used to impose a received signal onto the chirped repetitively pulsed optical signal. For example, optical modulator **120** may be a suitable phase modulator configured to impose an analog signal on the chirped repetitively pulsed optical signal. In this embodiment, the chirped repetitively pulsed optical signal may be divided into a first portion and a second portion after being generated by chirped optical source **110**. The first portion travels to the phase modulator while the second portion travels to a splitter. The splitter is configured to split the second portion of the chirped repetitively pulsed optical signal based on a mixing matrix. The second portion is split into M signals, where M is the number of channels in spatial light modulator **150** and a dimension in the mixing matrix. The splitter then transmits the split second portion of the chirped repetitively pulsed optical signal to interfere with the mixed dispersed optical frequencies of the first portion from spatial light modulator **150**.

The phase modulator receives the first portion of the chirped repetitively pulsed optical signal. Electrodes are positioned within the phase modulator and are coupled to a voltage generator. The voltage generator may be programmed to independently apply voltages to the electrodes so as to change the phase of the first portion of the chirped repetitively pulsed optical signal traveling through the phase modulator. For example, the voltage generator may apply voltages proportional to the analog signal generated by signal generator **130** and received by an analog signal receiver. The signal receiver may be operatively coupled to the voltage generator and may be any structure capable of receiving an analog signal, e.g., an antenna. The output of the phase modulator is the analog signal imposed on the first portion of the chirped repetitively pulsed optical signal, referred to as the modulated chirped repetitively pulsed optical signal.

FIG. **9** illustrates an exemplary apparatus **900** for obtaining a representation of an analog signal that is a phase-modulating variation of apparatus **800** from FIG. **8**. Apparatus **900** is similar to apparatus **800** except apparatus **900** includes phase modulator **920** in place of MZM **820** and further includes splitter array **925**. Phase modulator **920** is configured to impose an analog signal on the chirped repetitively pulsed optical signal from chirped FBG **815**. The chirped repetitively pulsed optical signal is divided into a first portion and a second portion, the first portion travels to phase modulator **920** while the second portion travels to splitter array **925**. Splitter array **925** is configured to split the second portion of the chirped repetitively pulsed optical signal based on the mixing matrix, e.g., an 8×10 mixing matrix, in SLM **850**. There are eight splitters in splitter array **925**, each of which sends the split second portion to a corresponding photodiode. For example, the highest splitter, M=1, of splitter array **925** transmits the split second portion of the chirped repetitively pulsed optical signal to the highest photodiode, M=1, of linear photodiode array **860**. The split second portion of the chirped repetitively pulsed optical signal interferes with mixed dispersed optical frequencies **856** of the first portion of the chirped repetitively pulsed optical signal at linear photodiode array **860**.

In some embodiments, spatial light modulator **150** may be used to adjust the mixing matrix. The mixing matrix may be adjusted, for example, between chirped repetitively pulsed optical signals. Increasing the number of mixing matrices may increase the resolution of the representation of the received signal obtained by device **100**. Spatial light modulator **150** may be used to bin the pixels together to vary the

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bandwidth of the received signal. Spatial light modulator **150** may adjust the number of channels (M), the number of pixel columns (N), and/or the number of pixels utilized in the mixing relative to the bandwidth of the received signal.

Optical Digital Signal

FIG. **10** schematically illustrates exemplary device **1000** for obtaining an electronic digital representation of an optical digital signal using optical-domain processing, according to some embodiments of the present invention. Device **1000** may be used for direct digital demodulation, i.e., converting an optical digital signal into an electronic digital signal. Device **1000** includes spatially dispersive element **1400**, spatial light modulator **1500**, optical sensor **1600**, and signal recovery processor **1700**. In some embodiments, device **1000** includes housing **1001** configured to hold at least spatially dispersive element **1400**, spatial light modulator **1500**, optical sensor **1600**, and signal recovery processor **1700** as illustrated in FIG. **10**. In other embodiments, device **1000** includes more than one housing (not shown), each housing configured to hold at least one structure in device **1000**.

Optical digital signal generator **1300** may generate an optical digital signal, such as an optical time division multiplexed signal. The modulation characteristics of the optical digital signal may be unknown. Optical digital signal generator **1300** may be remote from device **1000** and coupled to device **1000** using any suitable means, e.g., a fiber optic cable.

FIG. **11** is a plot illustrating a temporal intensity profile of an exemplary optical digital signal. The optical digital signal has n sequential pulses each at a different wavelength and each carrying an independent data stream as a function of time. The shorter wavelengths are represented by light gray and the longer wavelength frequencies are represented by dark gray. In this example, $\lambda_n > \lambda_{n-1} > \dots > \lambda_7 > \lambda_6 > \lambda_5 > \lambda_4 > \lambda_3 > \lambda_2 > \lambda_1$ and the modulation format of the signal is on/off keying as represented by pulses $\lambda_1, \lambda_3, \lambda_4, \lambda_6,$ and λ_n being on and $\lambda_2, \lambda_5, \lambda_7,$ and λ_{n-1} being off. Although not shown in this example, the wavelengths of the sequential pulses may vary in time based on the optical digital signal.

Referring back to FIG. **10**, after the optical digital signal is generated by optical digital signal generator **1300**, the optical digital signal is received by device **1000**, for example by connecting a fiber optic cable from digital signal generator **1300** to device **1000**, e.g., to spatially dispersive element **1400**. In some embodiments, optical signal receiver **1300** is disposed on device **1000**, e.g., a fiber optic cable port disposed on device **1000**. In other embodiments, the optical digital signal receiver is disposed outside of device **1000** and operatively coupled to device **1000** such that the optical digital signal may be transmitted to spatially dispersive element **1400**. Spatially dispersive element **1400** may spatially disperse frequencies in the received signal and may operate in substantially the same manner as spatially dispersive element **140** of FIG. **1**.

FIG. **12** illustrates exemplary dispersed optical frequencies in the optical digital signal of FIG. **11** after traveling through or reflecting from spatially dispersive element **1400**. The frequencies are dispersed such that shorter wavelength frequencies, represented by light gray, are disposed on one end of the dispersed signal relative to the x-axis, and the wavelength of the frequencies increases along the x-axis up to longer wavelength frequencies, represented by dark gray. In this example, the pulses are ordered $\lambda_n > \lambda_{n-1} > \dots > \lambda_7 > \lambda_6 > \lambda_5 > \lambda_4 > \lambda_3 > \lambda_2 > \lambda_1$. The wavelength of the dispersed signal remains uniform relative to the y-axis.

Referring back to FIG. **10**, spatial light modulator **1500** may mix the dispersed optical frequencies by imposing a mixing matrix on an optical intensity of the dispersed optical

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frequencies. Spatial light modulator **1500** may operate in substantially the same manner as spatial light modulator **150** of FIG. **1**.

Optical sensor **1600** may obtain an electrical representation of the mixed dispersed optical frequencies. Optical sensor **1600** may operate in substantially the same manner as optical sensor **160** of FIG. **1**.

Signal recovery processor **1700** may obtain a digital representation of the received signal based on the electrical representation and the mixing matrix. Further, signal recovery processor **1700** may determine a modulation format of the digital representation and may demodulate the digital representation based on the modulation format. Signal recovery processor **1700** may operate in substantially the same manner as signal recovery processor **170** of FIG. **1**. Non-limiting examples of digital modulation formats include phase-shift keying, binary phase modulation, frequency-shift keying, amplitude shift-keying, on/off keying, quadrature amplitude modulation, continuous phase modulation, orthogonal frequency-division multiplexing modulation, wavelet modulation, Trellis coded modulation, direct-sequence spread spectrum, chirp spread spectrum, frequency-hopping spread spectrum, and pulse position modulation.

FIG. **13** illustrates an exemplary apparatus **1301** for obtaining a representation of an optical digital signal that is a variation of apparatus **800** from FIG. **8**. Apparatus **1301** is similar to apparatus **800** except apparatus **1301** includes input optical digital signal **1310** and does not include mode-locked laser **810**, chirped FBG **815**, or MZM **820** which receives analog signal **830**. Optical digital signal **1310** may be a signal that resides on a periodically chirped optical carrier, e.g., an optical time division multiplexed signal.

Method

FIG. **14** illustrates an exemplary method **1401** for obtaining a representation of a signal, according to some embodiments of the present invention. First, at step **1410**, a signal is received. The signal may be a radio-frequency signal, which may be analog or digital, or an optical digital signal, and may reside on a periodically chirped optical carrier. The signal may be received in a manner discussed above with respect to FIG. **1** and FIG. **10**, for example.

Next, at step **1420**, an optical-domain representation of the received signal is obtained. For example, as described above with reference to FIGS. **1** and **9**, the received signal may be an RF signal that may be imposed on a periodically chirped optical carrier, e.g., in the form of an intensity modulation or a phase modulation of the carrier. Such a modulation of the optical carrier may be considered to provide an optical-domain representation of the received signal. Or, for example, as described above with reference to FIG. **10**, the received signal may be an optical digital signal. In such an embodiment, the received signal is already in the optical domain and may be used "as is," in which case no action need be taken to obtain an optical-domain representation of the received signal.

Next, at step **1430**, different frequencies in the optical-domain representation of the signal are spatially dispersed. The spatially dispersing may include producing a time/wavelength to space mapping of the optical-domain representation. The different frequencies may be dispersed up to the size of the corresponding spatial light modulator for mixing. In some embodiments, the spatially dispersing includes using diffraction grating or a prism.

Then, at step **1430**, the dispersed optical frequencies are mixed. The mixing may include imposing a mixing matrix on an optical intensity of the dispersed optical frequencies. For example, as discussed above with respect to FIGS. **6A-6B**, a spatial light modulator of size $M \times N$ may be used to impose a

mixing matrix. The spatial light modulator may have M channels and N pixel columns defining individual pixels that may be independently adjustable so as to select a particular mixing matrix and to prevent or reduce light transmission of different portions of the dispersed optical frequencies. The mixing preferably is performed so as to avoid blocking an entire column of pixels (N) at one time. The mixing may include programming and/or reprogramming the pixels so as to alter the mixing matrix. In some embodiments, the mixing includes using a spatial light modulator.

Then, at step **1440**, an electrical representation of the mixed dispersed optical frequencies is obtained. The mixed dispersed optical frequencies may be converted from light to current/voltage to obtain the electrical representation. Obtaining the electrical representation may include integrating the mixed dispersed optical frequencies in time. Further, obtaining the electrical representation may include low-pass filtering the mixed dispersed optical frequencies. In some embodiments, obtaining an electrical representation includes using a photodiode. In some embodiments, an array of photodiodes, e.g., an array of M×1 photodiodes, are used corresponding to the number of channels (M) in the spatial light modulator.

Next, at step **1450**, a digital representation of the originally received signal is obtained based on the electrical representation and the mixing matrix. Step **1450** may include converting the electrical representation from an analog representation (e.g., a signal produced by the optical sensor) into a digital representation (e.g., using an ADC), and recovering a digital representation of the signal based on the digital representation from the ADC and the mixing matrix. In some embodiments, obtaining the digital representation includes storing the digital representation of the signal in a memory device. In some embodiments, an array of ADCs, e.g., an array of M×1 ADCs, are used corresponding to the number of channels (M) in the spatial light modulator. The processing may include using a dedicated circuit or a computer. The processing may include running a suitable program for signal recovery in software such as Matlab® (The MathWorks, Inc., Natick, Mass.) or Mathematica® (Wolfram Research, Champaign, Ill.). Once the digital representation of the signal is obtained, the representation may be suitably analyzed.

Method **1401** may further include, at step **1460**, determining a modulation format of the digital representation. The modulation format may be determined, for example, using suitable computer software. Non-limiting examples of modulation formats include amplitude modulation, double-sideband modulation, single-sideband modulation, vestigial sideband modulation, quadrature amplitude modulation, angle modulation, frequency modulation, phase modulation, phase-shift keying, binary phase modulation, frequency-shift keying, amplitude shift-keying, on/off keying, continuous phase modulation, orthogonal frequency-division multiplexing modulation, wavelet modulation, Trellis coded modulation, direct-sequence spread spectrum, chirp spread spectrum, frequency-hopping spread spectrum, and pulse position modulation. Previously-known demodulation techniques may require prior knowledge of the type of modulation used to encode a signal; for example, previously-known demodulation phase-shift keying may require the use of an interferometer to determine the phase of incoming optical pulses. By contrast, aspects of the present invention instead provide a digitized representation of the received signal to suitable software that may be configured to determine the particular type of modulation being used to encode a signal, thus providing substantially more flexibility than previously-known demodulators.

Then, at step **1470**, the digital representation may be demodulated based on the modulation format using, e.g., suitable computer software. In some embodiments, determining the modulation format and demodulating the determined modulation format may occur after converting the electrical representation of the mixed dispersed optical frequencies into a digital representation. As such, the received signal may be digitized and then demodulated with, for example, suitable high speed digital demodulation software.

Method **1401** may further include displaying the digital representation of the received signal to a user, e.g., using a suitable display device, such as an LCD or LED display.

In some embodiments, a chirped repetitively pulsed optical signal is generated. As discussed with respect to FIG. 1, generating the chirped repetitively pulsed optical signal may include using a laser configured to generate a suitable optical pulse, e.g., a mode-locked laser, fiber laser, titanium-doped sapphire (Ti:Sapphire) solid-state laser, or dye laser. Generating the chirped repetitively pulsed optical signal may include chirping the pulse generated by the laser, e.g., using a grating, a fiber Bragg grating (FBG), dispersion compensating fiber (DCF), or standard optical fiber. Generating the chirped repetitively pulsed optical signal may further include calibrating the grating to eliminate timing errors in the chirped repetitively pulsed optical signal.

In some embodiments, the chirped repetitively pulsed optical signal is modulated. The modulation includes imposing an analog signal on the chirped repetitively pulsed optical signal. Modulating the chirped repetitively pulsed optical signal may include receiving an analog signal that is generated by a remote source. Once the analog signal is received, it may be imposed on the chirped repetitively pulsed optical signal using a modulator such as an intensity modulator, e.g., MZM such as described above, or a phase modulator such as described below. The modulating of the chirped repetitively pulsed optical signal may result in the modulated chirped repetitively pulsed optical signal having varying intensities over time based on the imposed analog signal. Further, the modulated chirped repetitively pulsed optical signal may have varying wavelengths over time based on how the chirped repetitively pulsed optical signal was generated.

Examples

The functionality of devices **100**, **1000** and method **1401** for obtaining a representation of a received signal may be illustrated by way of Examples, which were numerically calculated using Mathematica® (Wolfram Research, Champaign, Ill.). FIG. **15A** is a plot illustrating the intensity of a simulated analog radio-frequency signal, e.g., a signal received by system **100** illustrated in FIG. **1**. In FIGS. **15A-17B**, time is normalized to one period of operation of device **100**, e.g., the temporal spacing between t_2 and t_1 illustrated in FIG. **2A**.

FIG. **15B** is three plots illustrating the intensity of three signals over normalized time after simulated transmission through separate channels of a mixing matrix. The mixing matrix included randomly placed squares with light transmission coefficients of 1 (full transmission) and $\frac{1}{2}$ (partial blockage). In this Example, spatial light modulator **150** included an equal number of channels (M) and columns of pixels (N).

FIG. **15C** is a plot illustrating the simulated digital representation of the analog signal of FIG. **15A** as digitized by device **100**. The simulated digital signal of FIG. **15C** was calculated at optical sensor **160** by integrating the signals of FIG. **15B** over the period of operation for each of the channels (M) of spatial light modulator **150**, digitized using low-rate

ADCs, and then, because $M=N$, multiplying this M -dimensional vector by the inverse of the mixing matrix.

FIG. 15D is a plot illustrating the difference, referred to as error, between the simulated signal intensity of the digital representation in FIG. 15C and the simulated signal as input to device 100. As can be seen from FIG. 15D, the simulated digital representation obtained using system 100 includes significantly more data points than the simulated signal as input to the device.

FIG. 16A is a plot illustrating the simulated intensity of an exemplary square-wave (digital) radio-frequency signal over time, e.g., a signal received by device 100 illustrated in FIG. 1. This Example illustrates a signal employing on/off keying modulation over several periods of a time-division multiplexed signal (TDM). The digitization of the signal using device 100 was simulated. The period of device 100 was set to an integral number of communications bits and aligned with the communications bits using a simulated optical delay line. The digital signal was calculated by integrating the simulated signals from channels (M) of spatial light modulator 150 over the period of operation for each of the channels (M) and then, because $M=N$, multiplying this M -dimensional vector by the inverse of the mixing matrix.

FIG. 16B is a plot illustrating the difference, referred to as error, between the signal intensity of the simulated digital representation of the received signal as digitized by device 100, and the simulated digital representation of the received signal as digitized as input to device 100. As may be seen in FIG. 16B, the error is relatively small, between approximately 1×10^{-13} and -4×10^{-13} .

FIG. 17A is a plot illustrating the simulated intensity of an exemplary optical digital signal over time, e.g., a signal received by device 1000 illustrated in FIG. 10. In this Example, the signal was sparse, as illustrated by the presence of only 3 non-zero pulses in the signal. An example of a sparse signal is a signal used in high order pulse position modulation. The digitization of the sparse signal was simulated. The digital signal was calculated at optical sensor 160 by integrating the simulated signals from channels (M) of spatial light modulator 150 over the period of operation for each of the channels (M). In this example, $M \neq N$ (M was 30 and N was 10), so the mixing matrix did not have an inverse; therefore signal recovery proceeded to a processor configured to run a program for signal recovery for compressing sensing in suitable software, e.g., Matlab® (The MathWorks, Inc., Natick, Mass.) or Mathematica® (Wolfram Research, Champaign, Ill.). Specifically, the L1Packv2 Mathematica® package disclosed by Loris was used.

FIG. 17B is a plot illustrating the difference, referred to as error, between the simulated signal intensity of the digital representation of the received sparse signal as digitized by device 1000 and the simulated signal intensity of the sparse signal of FIG. 17A as input to device 1000. As may be seen in FIG. 17B, the error is relatively small, between approximately 1×10^{-14} and -1.5×10^{-14} .

Alternative Embodiments

While preferred embodiments of the invention are described herein, it will be apparent to one skilled in the art that various changes and modifications may be made. The appended claims are intended to cover all such changes and modifications that fall within the true spirit and scope of the invention.

What is claimed:

1. A device for obtaining a digital representation of a received signal, the device comprising:

a spatially dispersive element configured to spatially disperse optical frequencies in an optical-domain representation of the received signal;

a spatial light modulator configured to mix the dispersed optical frequencies by imposing a mixing matrix on an optical intensity of the dispersed optical frequencies;

an optical sensor configured to obtain an electrical representation of the mixed dispersed optical frequencies; and

a signal recovery processor configured to obtain a digital representation of the received signal based on the electrical representation and the mixing matrix.

2. The device of claim 1, wherein the signal recovery processor is further configured to determine a modulation format of the digital representation.

3. The device of claim 2, wherein the signal recovery processor is further configured to demodulate the digital representation based on the modulation format.

4. The device of claim 1, wherein the received signal comprises an optical digital signal.

5. The device of claim 1, wherein the received signal comprises an analog radio-frequency signal.

6. The device of claim 5, further comprising a chirped optical source configured to generate a chirped repetitively pulsed optical signal and an optical modulator configured to impose the analog radio-frequency signal on the chirped repetitively pulsed optical signal.

7. The device of claim 6, wherein the chirped optical source comprises a laser.

8. The device of claim 6, wherein the chirped optical source comprises a dispersive optical element.

9. The device of claim 5, further comprising an analog signal receiver operatively coupled to the optical modulator, the analog signal receiver configured to receive the analog radio-frequency signal.

10. The device of claim 6, wherein the optical modulator comprises an intensity modulator.

11. The device of claim 6, further comprising a splitter, wherein the optical modulator comprises a phase modulator and the chirped repetitively pulsed optical signal is divided into a first portion and a second portion, the first portion traveling to the phase modulator and the second portion traveling to the splitter,

the splitter configured to split the second portion of the chirped repetitively pulsed optical signal based on the mixing matrix and transmit the split second portion of the chirped repetitively pulsed optical signal to interfere with the mixed dispersed optical frequencies of the first portion of the chirped repetitively pulsed optical signal from the spatial light modulator.

12. The device of claim 1, wherein the spatially dispersive element comprises a diffraction grating.

13. The device of claim 1, wherein the spatially dispersive element comprises a wavelength division demultiplexer.

14. The device of claim 1, wherein the spatial light modulator comprises channels and columns of pixels, each pixel being independently adjustable.

15. The device of claim 1, wherein the optical sensor comprises an array of photodiodes.

16. The device of claim 1, wherein the signal recovery processor comprises an analog-to-digital converter.

17. The device of claim 1, further comprising a display unit configured to display the digital representation of the received signal.

18. A method for obtaining a digital representation of a received signal, the method comprising:
obtaining an optical-domain representation of the signal;

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spatially dispersing optical frequencies in the optical-domain representation;
mixing the dispersed optical frequencies by imposing a mixing matrix on an optical intensity of the dispersed optical frequencies;
obtaining an electrical representation of the mixed dispersed optical frequencies; and
obtaining a digital representation of the signal based on the electrical representation and the mixing matrix.

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19. The method of claim **18**, further comprising determining a modulation format of the digital representation.

20. The method of claim **19**, further comprising demodulating the digital representation based on the modulation format.

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