

[54] BAND-GAP REFERENCE CIRCUIT FOR USE WITH CMOS IC CHIPS

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[51] Int. Cl.⁴ G05F 3/20

[52] U.S. Cl. 323/313; 323/316; 323/907

[58] Field of Search 323/313-316, 323/907; 307/296 R, 297

[56] References Cited

U.S. PATENT DOCUMENTS

4,263,519 4/1981 Schade, Jr. 323/314 X
4,317,054 2/1982 Caruso et al. 323/313 X

Primary Examiner—Peter S. Wong

Attorney, Agent, or Firm—Parmelee, Bollinger & Bramblett

[57] ABSTRACT

A band-gap reference circuit having a pair of transistors operated at different current densities to produce a positive temperature coefficient (TC) signal proportional to the ΔV_{BE} of the two transistors and combined with a negative TC voltage derived from the V_{BE} of one of the transistors to produce a composite signal substantially invariant with temperature. The ΔV_{BE} signal component is increased in magnitude by connecting resistor string bias circuit to each of the transistors, to effectively multiply the V_{BE} of each transistor, and thereby multiply the ΔV_{BE} signal. The composite signal is sensed in the emitter circuits of the two transistors, so that it is unnecessary to access the collectors of the transistors, thereby making it readily possible to use the circuit with CMOS IC devices.

10 Claims, 5 Drawing Figures

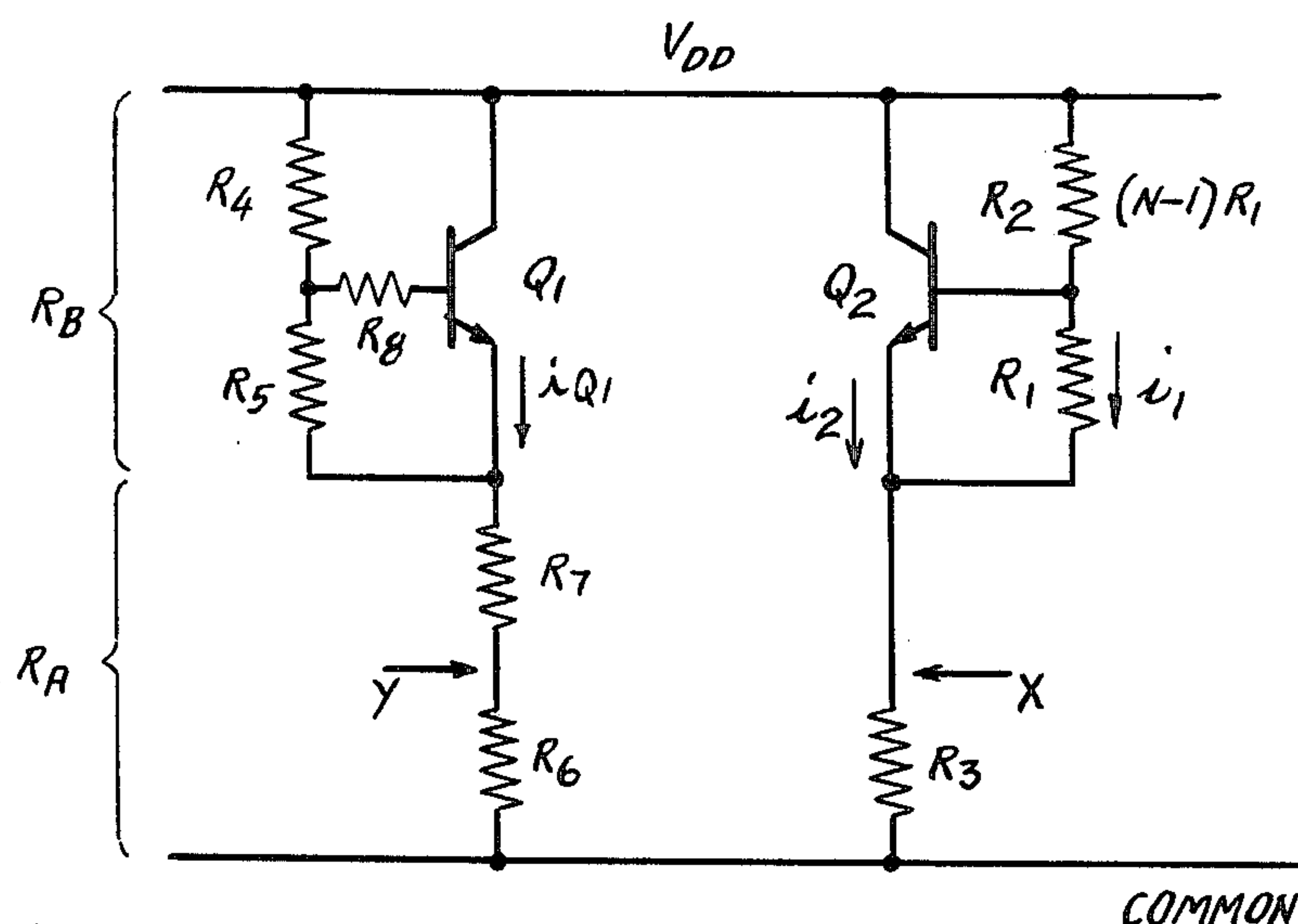


Fig. 1.

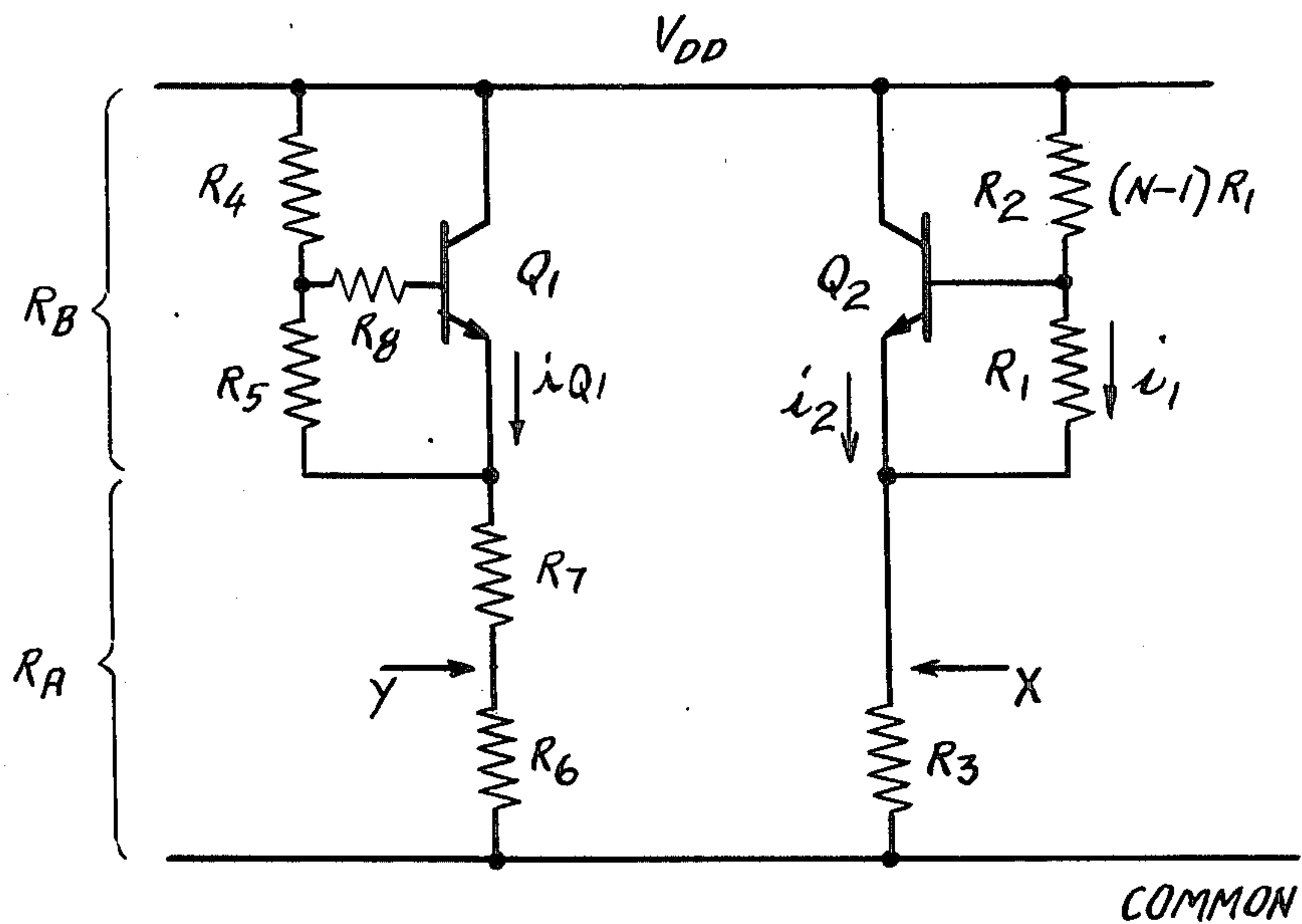


Fig. 2.

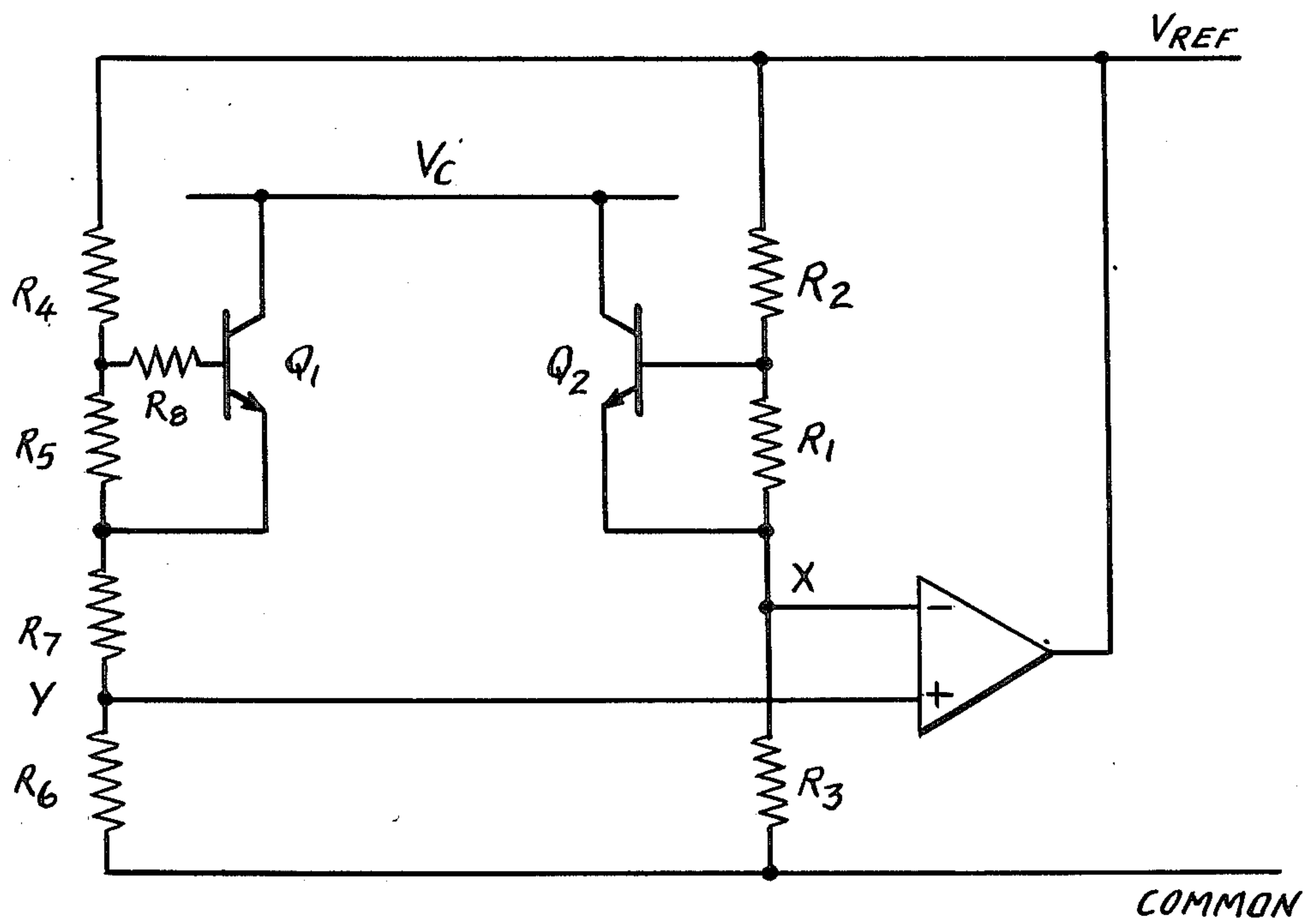


Fig. 3.

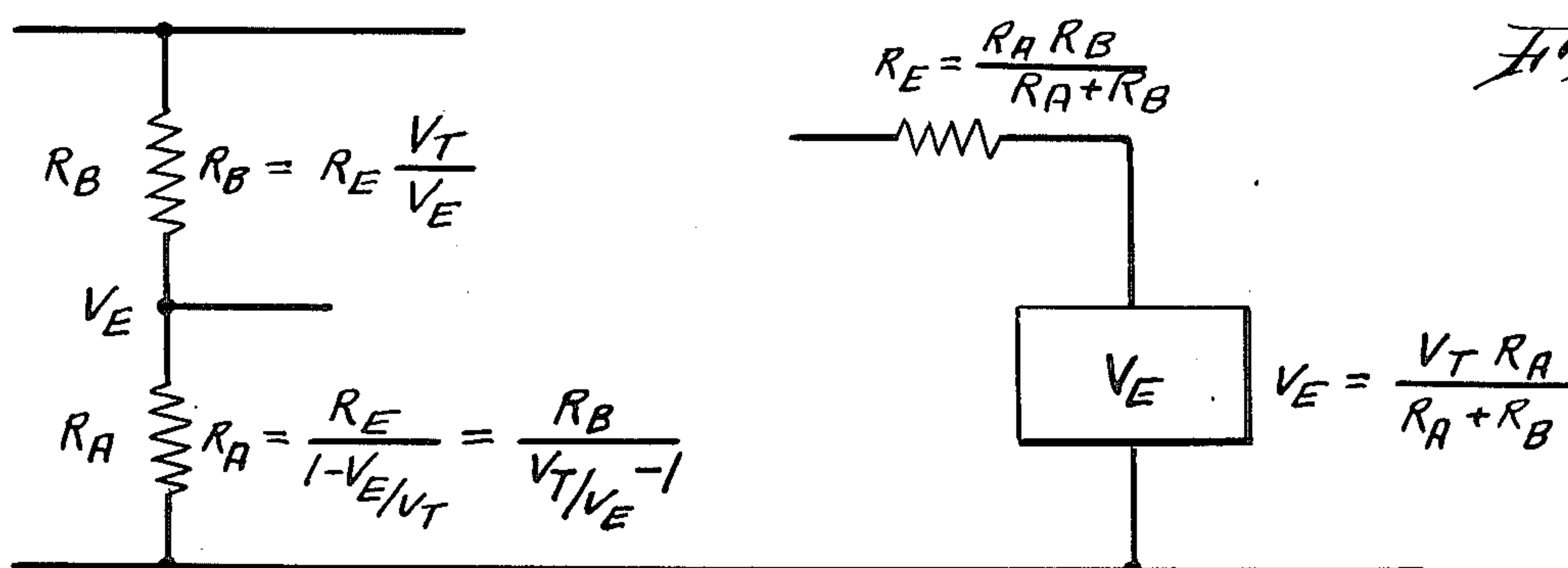
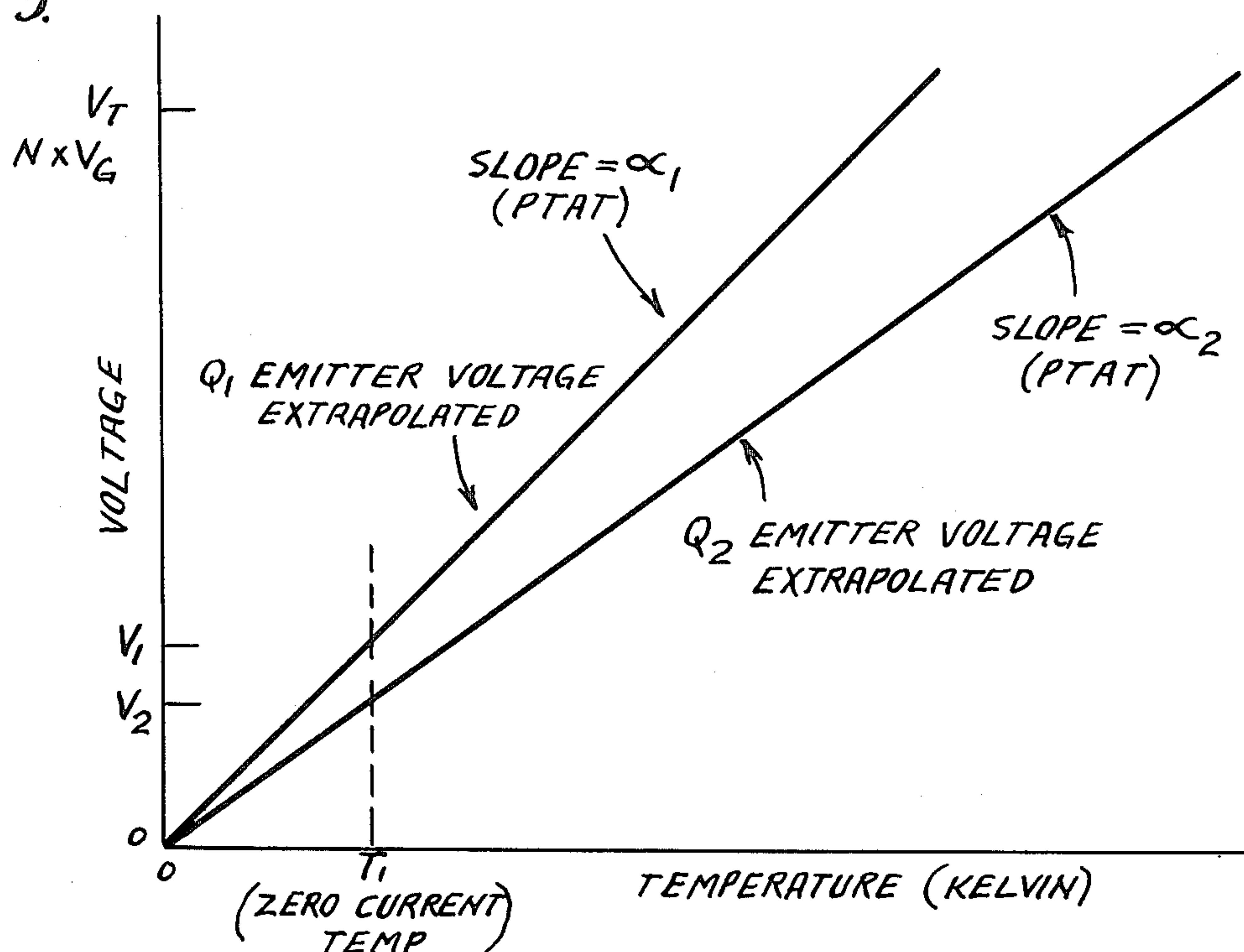
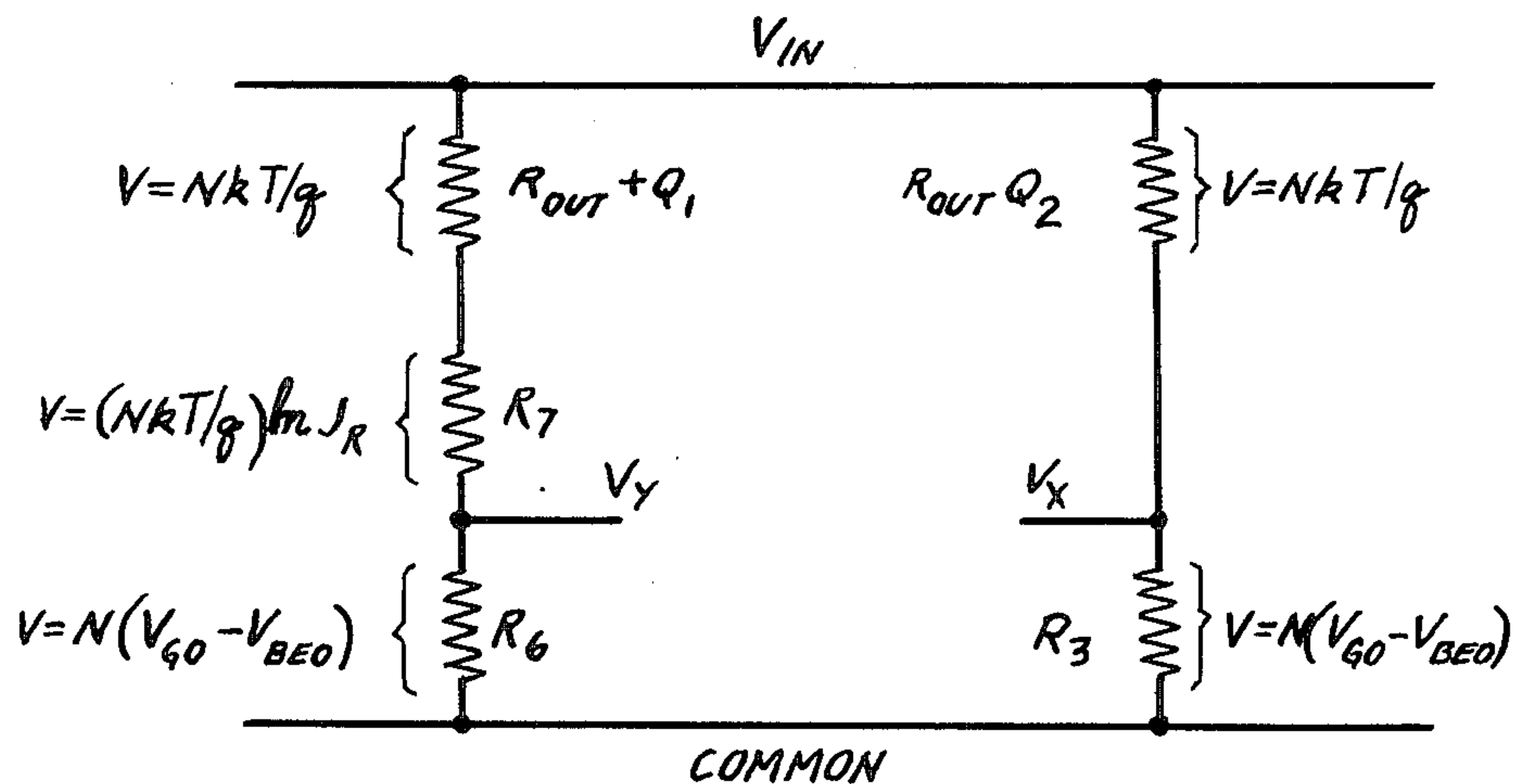


Fig. 4.

Fig. 5.



BAND-GAP REFERENCE CIRCUIT FOR USE WITH CMOS IC CHIPS

BACKGROUND OF THE INVENTION

1. Field of the Invention

This invention relates to reference circuits of the band-gap type. Such circuits are generally used as voltage references, but do find other applications such as threshold detectors. The present invention particularly relates to band-gap circuits which are suited for use with CMOS integrated-circuit (IC) chips.

2. Description of the Prior Art

Band-gap voltage regulators have been used for a number of years for developing reference voltages which remain substantially constant in the face of temperature variations. Such circuits generally develop a voltage proportional to the difference between base-to-emitter voltages (ΔV_{BE}) of two transistors operated at different current densities. This voltage will have a positive temperature coefficient (TC), and is combined with a V_{BE} voltage having a negative TC to provide the output signal which varies only a little with temperature changes. Reissue U.S. Pat. RE. No. 30,586 (A. P. Brokaw) shows a particularly advantageous band-gap voltage reference requiring only two transistors.

Band-gap reference circuits have primarily been employed in bipolar ICs. Efforts have been made to adapt such references for CMOS ICs, but significant problems have been encountered in those efforts. As a result, the devices proposed for CMOS have suffered important defects, particularly undue complexity.

One serious problem results from the fact that the ΔV_{BE} voltage is quite small (e.g. less than 100 mV), so that it must be amplified quite a bit to reach a value suitable for reference purposes. Such amplification is inherent in a band-gap circuit such as shown in U.S. Pat. RE. No. 30,586 referred to above, because the ΔV_{BE} signal is taken from the collectors of the two transistors. In a CMOS chip made by the usual processes, however, the bipolar transistors available for voltage reference purposes are parasitic transistors, the collectors of which cannot be independently accessed for voltage sensing purposes. In such devices, therefore, the ΔV_{BE} voltage will not automatically be amplified by the transistors from which it is developed.

Moreover, the MOS amplifiers on a CMOS chip have relatively large offset voltages, so that the offset after substantial amplification will show up as a large error compared to the ΔV_{BE} signal component. For example, to develop a reference voltage of around 5 volts, a 20 mV offset in an amplifier (or comparator) could show up as a 0.5 volt error referred to output or threshold.

Proposals have been made to solve this problem, including various compensation arrangements. However, the resulting devices have been too complex to provide a really satisfactory solution to the problem.

SUMMARY OF THE INVENTION

In a preferred embodiment of the invention to be described hereinafter, two transistors are operated at different current densities to produce a ΔV_{BE} signal. This signal is detected at the emitter circuits of the transistors. Resistor-string V_{BE} multiplier circuits are connected to the bases of both transistors. This multiplies not only the V_{BE} voltages but also the ΔV_{BE} signal. This arrangement makes it possible to produce an

effective ΔV_{BE} of over 400 mV with a very simple circuit adapted for use with CMOS chips.

Still other objects, aspects and advantages of the invention will in part be pointed out in, and in part apparent from, the following description of preferred embodiments considered together with the accompanying drawings.

BRIEF DESCRIPTION OF THE DRAWINGS

FIG. 1 is a circuit diagram showing an embodiment of the invention used for threshold detection;

FIG. 2 is a circuit diagram showing another embodiment of the invention for use as a voltage reference;

FIG. 3 is a graph to aid in explaining the operation of the invention;

FIG. 4 shows an equivalent circuit based on Thevenin's theorem; and

FIG. 5 is another circuit diagram illustrating aspects of the operation of the circuitry.

DETAILED DESCRIPTION OF PREFERRED EMBODIMENTS OF THE INVENTION

Referring first to FIG. 1, the threshold detector comprises a pair of transistors Q_1 and Q_2 operated at different current densities. For that purpose, the transistor emitter areas will be unequal in a predetermined ratio ($n:a$). The collectors of the transistors are connected directly to the supply line V_{DD} and the emitters are connected to common through respective resistor circuits R_3 and R_6 , R_7 .

The bases of the transistors Q_1 and Q_2 are connected to respective resistor strings R_4/R_5 and R_1/R_2 between the collector and emitter of each transistor, with the ratio R_1 to R_2 matched to the ratio of R_5 to R_4 . Such resistor arrangement provides in known fashion for V_{BE} multiplication proportional to the ratio of resistor values. For example, with V_{BE2} appearing across resistor R_1 (and assuming the base current of Q_2 is not significant) the voltage across R_2 will be $(R_2/R_1) V_{BE2}$.

Thus the total voltage from the top of R_1 to the emitter of Q_2 will be $(1 + R_2/R_1) (V_{BE2})$ or NV_{BE2} , with N defined as $1 + R_2/R_1$. Similarly, the voltage from the top of R_4 to the emitter of Q_1 will be N times V_{BE1} . This latter voltage will be different from the corresponding voltage at Q_2 , however, since Q_1 will operate at a different current density and will have a different V_{BE} at the design center condition.

With properly selected circuit values and using transistors which maintain their logarithmic V_{BE} performance over the full temperature and current ranges expected, the circuit will produce between the points X—Y a differential voltage which passes through zero when the supply voltage V_{DD} reaches a predetermined voltage V_T . Increasing V_{DD} above V_T makes X—Y go positive; decreasing it makes X—Y go negative. By connecting a comparator to the points X—Y, the circuit becomes an effective threshold detector. Moreover, the threshold set value V_T will be substantially unaffected by temperature changes.

In selecting the circuit values, the following procedure may be followed:

V_T Choose V_T , the voltage to be detected on V_{DD}

V_G Determine V_G , the effective band-gap voltage for the actual devices to be used. (This is determined by the nominal temperature slope extrapolated to 0° K.)

N Calculate $N = V_T/V_G$

i_2 Choose i_2 , the nominal operating current for Q_2 at the design center temperature with $V_{DD}=V_T$.

i_1 Choose the current in the R_1, R_2 string (neglect base current) at the design center condition.

V_{BEO} Determine V_{BEO} , the nominal base emitter voltage present on Q_2 when biased by i_2 at the design center. (Collector base voltage will be about $(N-1)V_{BEO}$).

J_R Choose $J_R=J_2/J_1$ the actual current density ratio to be maintained between Q_2 and Q_1 .

I_R Choose $I_R=i_2/i_{Q1}$ the ratio of currents to be maintained in Q_2 and Q_1 . Implicit in I_R and J_R is $n_a:a$, the emitter area ratio of the devices.

$$A_R \text{ Calculate } A_R = 1 + \frac{(kT/q)\ln J_R}{V_G - V_{BEO}}$$

Then:

$$R_1 = V_{BEO}/i_1$$

$$R_2 = (N-1) R_1$$

$$R_3 = (V_T - N V_{BEO})/(i_2 + i_1)$$

$$R_4 = I_R R_2$$

$$R_5 = I_R R_1$$

$$R_6 = \frac{R_4 + R_5}{\frac{R_1 + R_2 + R_3}{R_3} - A_R}$$

$$R_7 = (A_R - 1) R_6$$

$$R_8 = \frac{R_4}{N} \left[\frac{1}{1 + \frac{kT/q}{(V_G - V_{BEO})}} - \frac{1}{A_R + \frac{kT/q}{(V_G - V_{BEO})}} \right]$$

The current chosen for the R_1, R_2 string relates to error due to base current and β . The smaller the standing current in R_1 , the larger the effect of the actual base current of Q_2 will be in R_2 . This error can be compensated, but the smaller it is, the less residue there will be after compensation.

The bias in the R_1/R_2 string shows up at the emitter Q_2 and disturbs the PTAT current which ordinarily flows in band-gap transistors. In ordinary circuits, the current in the transistor would be the total emitter-resistor (R_3) current. In this circuit, the current in R_1 also flows in R_3 . As a result, if the voltage at the emitter of Q_2 is proportional-to-absolute-temperature (PTAT) with respect to common, the current in Q_2 will not be PTAT. This can be treated by noting that the Thevenin equivalent (see also FIG. 4) of the drive to the Q_2 emitter can be calculated in the absence of Q_2 as a voltage proportional to V_{DD} and scaled by $R_3/(R_1+R_2+R_3)$ and a source impedance $(R_1+R_2)R_3/(R_1+R_2+R_3)$. In this circuit, the voltage across R_3 is approximately PTAT and the emitter current of Q_2 is a somewhat "stronger" function of absolute temperature.

Once i_1 has been selected, R_1 is given by $R_1 = V_{BEO}/i_1$ where V_{BEO} is the nominal value for Q_2 under the temperature and emitter current conditions assumed for the design center. Next, the determination

of the V_{BE} multiplication factor N is in accordance with the principles described hereafter.

It is known that the base-emitter voltage can be determined as follows:

$$V_{BE} = V_{GO} - (V_{GO} - V_{BEO})T/T_0 + (kT/q)\ln I/I_0 + (mkT/Q)\ln T_0/T$$

For analysis purposes, it is appropriate to neglect the current-dependent terms, so that V_{BE} will be set equal to $V_{GO} - (V_{GO} - V_{BEO})T/T_0$. Thus a component of V_{BE} rises with falling temperature to the value of V_{GO} (the extrapolated band-gap voltage) when $T=0$ Kelvin. Extrapolating this behavior for V_{BE2} , the voltage across R_1 will be V_{GO} at 0 and the voltage from V_{DD} to the Q_2 emitter will be $N V_{GO}$ where

$$N = 1 + R_2/R_1.$$

With V_{DD} equal to the desired V_T at the design center, and placing $N = V_T/V_{GO}$, the emitter of Q_2 will be at 0 volts at 0 Kelvin. (In this expression, V_G represents the value of V_{GO} for the particular transistor characteristic involved, with the temperature behavior of V_{BE} linearized around room temperature.) The transistor current is proportional to temperature, but with an offset to some positive temperature. That is, if the emitter voltage of Q_2 behaved at low temperatures as the extrapolation from room temperature in FIG. 3 indicates, the current would go through zero and reverse as the emitter voltage crossed the open circuit voltage. The temperature at which this happens is the offset. For temperatures far above the offset, emitter current rises a bit faster than PTAT. N can be selected so that the behavior of the Q_2 emitter voltage will be as shown in FIG. 3.

The current in Q_1 is maintained as a constant fraction of that in Q_2 . This may not be necessary for satisfactory operation but it linearizes a ΔV_{BE} so as to permit simplified analysis.

With the current density in Q_1 a fixed fraction of that in Q_2 , Q_1 's emitter voltage can also be extrapolated to zero at 0 Kelvin, with the same N factor in its base circuit. At any other temperature, the extrapolated emitter voltage of Q_1 will be higher than Q_2 due to Q_1 's lower current density. The voltage at Q_1 emitter is tapped by the divider R_6 and R_7 to produce a voltage equal to the Q_2 emitter voltage. Since the voltages at the emitter are PTAT (if $V_{DD}=V_T$), a fixed fraction of the Q_1 emitter voltage will equal the Q_2 emitter voltage.

If V_{DD} changes from V_T , however, these voltages will not stay equal. For example, consider that if V_{DD} goes up a little, the two emitter voltages will follow V_{DD} with almost unity gain, since the transistors act somewhat like emitter followers driven by V_{DD} . Therefore the voltage changes at the two emitters will be near equal. However, the voltage change at Y will be attenuated by the voltage divider R_6, R_7 . So, if V_{DD} goes up, the voltage at X will rise more than the voltage at Y .

Once N is determined, R_2 is easily calculated as $(N-1)R_1$. Moreover, the emitter voltage of Q_2 will be $V_T - N V_{BEO}$ at the design center, and the current in R_3 will simply be the current from R_1 plus the emitter current of Q_2 . This ratio gives the value for R_3 .

Once these three resistances are known, the Thevenin equivalent can be worked out as illustrated in FIG. 4. The open circuit voltage (see FIG. 3) V_2 will be $V_T R_3/(R_1 + R_2 + R_3)$ and the source resistance R_{E2} will

be $(R_1 + R_2)R_3/(R_1 + R_2 + R_3)$. The corresponding temperature, T_1 , is the temperature at which the emitter current of Q_2 would fall to zero if the voltage followed the extrapolation all the way down. At higher temperatures, the emitter current will increase in proportion to temperature (not absolute temperature however). If the current in Q_1 is to be proportional, it must fall to zero at T_1 also. Since Q_1 operates at a different current density (in the limit as i goes to zero), the voltage at Q_1 's emitter will be different from Q_2 's.

To find this voltage, reference may be made to FIG. 3 where it is seen that both emitter voltages are PTAT. That is, the emitter voltages are proportional to temperature by some constant $\alpha = N(V_G - V_{BE0})/T_0$. At temperature T_1 the voltage is just αT_1 so that the ratio of V_1/V_2 is just the ratio α_1/α_2 . Using the subscripted Q numbers:

$$\begin{aligned}\alpha_1/\alpha_2 &= (N(V_G - V_{BE10})/T_0)/(N(V_G - V_{BE20})/T_0) \\ &= (V_G - V_{BE10})/(V_G - V_{BE20})\end{aligned}$$

The ratio of the emitter currents will be held constant and the area ratio will remain fixed so that the current density ratio J_R will also be fixed. As a result:

$$V_{BE1} = V_{BE2} - (kT/q) \ln J_R$$

at all temperatures so that A_R , the ratio of the α 's is given by:

$$A_R \alpha_1/\alpha_2 = 1 + (kT/q) \ln J_R / (V_G - V_{BE0})$$

where V_{BE0} replaces V_{BE20} .

Then, $V_1 = A_R V_2$. That is, the open circuit voltage at Q_1 's emitter should be A_R times that for Q_2 .

The actual current in Q_1 at some temperature T above T_1 will be given by $\alpha_1 (T - T_1)/R_{E1}$, where R_{E1} is the equivalent source resistance, as in Q_2 it is given by $\alpha_2 (T - T_1)/R_{E2}$.

To maintain J_R constant, with a constant emitter area ratio, I_R the ratio of emitter currents must be constant. Thus:

$$\alpha_1 (T - T_1) I_R / R_{E1} = \alpha_2 (T - T_1) / R_{E2}$$

and:

$$R_{E1} = I_R (\alpha_1/\alpha_2) R_{E2} = I_R A_R R_{E2}$$

FIG. 4 includes expressions to derive resistor values for a divider from their desired Thevenin equivalent. Given the desired V_2 as V_E and R_{E1} as R_E , the value of $R_B = (R_4 + R_5)$ and $R_A = (R_6 + R_7)$ can be found:

$$R_B = R_{E1} V_T / V_1$$

but,

$$R_{E1} = I_R A_R R_{E2} \text{ and } V_1 = A_R V_2$$

so:

$$R_B = I_R R_{E2} V_T / V_2$$

By applying the expressions of FIG. 4 to R_1 and R_2 :

$$R_1 + R_2 = R_{E2} V_T / V_2$$

and:

$$R_B = I_R (R_1 + R_2)$$

Since the ratio between R_5 and R_4 should be the same, $(N-1)$, as between R_1 and R_2 it follows that:

$$R_4 = I_R R_2, \quad R_5 = I_R R_1$$

To get the lower half of the resistance at Q_1 's emitter, the expression from FIG. 4 can be employed:

$$R_A = \frac{R_B}{\frac{V_T}{V_E} - 1}$$

Substituting $V_1 = A_R V_2$ for the desired voltage V_E :

$$R_A = \frac{R_B}{\frac{V_T}{A_R V_2} - 1}$$

At balance, when $V_{DD} = V_T$ and $X - Y = 0$ the voltage at Y should equal the emitter voltage of Q_2 . That means that the voltage which appears across $R_6 + R_7 = R_A$ is A_R times the voltage on R_6 , or:

$$R_A = A_R R_6$$

and combining with the above:

$$R_6 = \frac{R_B}{\frac{V_T}{V_2} - A_R}$$

Substituting in the value just determined for R_B and the resistor ratio which gives V_T/V_2 gives the result:

$$R_6 = \frac{R_4 + R_5}{\frac{R_1 + R_2 + R_3}{R_3} - A_R}$$

Finally, since:

$$R_A = R_6 + R_7 = A_R R_6$$

Then:

$$R_7 = (A_R - 1) R_6$$

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The above analysis is substantially complete, neglecting only base current, V_{BE} curvature, and I_c being proportional to an offset temperature. The last two effects are fairly small and tend to oppose each other in any event.

Several of the external constraints make it desirable to use large values for R_1 and dependent resistances. In this case, low β transistors will produce an error in the threshold. Roughly, the base current of Q_2 flowing in R_2 will produce an extra drop which will add directly to V_T . The voltage on R_4 will be similarly affected by the base current of Q_1 to the extent that $\beta_2 = \beta_1$.

To the extent that the betas do not match, a further threshold offset will be produced. This is because a small difference voltage will be produced between X and Y which will have to be compensated by an additional change in V_T .

This effect can be exploited to make a first order compensation for the primary base current error. The addition of R_8 in the base circuit of Q_1 will drop the emitter voltage an extra NR_8i_{b1} . To balance this drop the threshold will have to come down by a factor related to the "gain" of the circuit, i.e. the change in voltage between X and Y as V_{DD} departs from V_T . The inverse of this gain times the NR_8i_{b1} factor should be made equal to the $R_2 i_{b2}$ term assumed to equal $R_4 i_{b1}$. That is:

$$R_8 = \frac{R_4 G}{N}$$

The gain factor G can be derived, approximately, from FIG. 5. By treating the transistors as their equivalent emitter source impedance driving point X and Y the small signal gain can be determined from the ratio of some voltages. On the right, the emitter impedance of Q_2 is approximated by NkT/qi_E . This impedance works against R_3 to attenuate at X signals applied to V_{in} which corresponds to V_{DD} . Since they share a common current, I_E , the ratio of these impedances is just the ratio of the respective voltage drops. On the left a similar situation exists for Q_1 except that there is an additional voltage drop across R_7 which further attenuates V_{in} at point balance and the voltage across R_7 is just $A_R - 1$ times that across R_6 (from the synthesis and the fact they share the same current). Then if $G = (V_X - V_Y)/V_{in}$

$$G = \frac{N(V_G - V_{BE0})}{NkT/q + N(V_G - V_{BE0})} - \frac{N(V_G - V_{BE0})}{NkT/q + N(A_R - 1)(V_G - V_{BE0}) + N(V_G - V_{BE0})}$$

$$G = \frac{1}{\frac{kT/q}{V_G - V_{BE0}} + 1} - \frac{1}{\frac{kT/q}{V_G - V_{BE0}} + A_R}$$

This expression, when multiplied by R_4/N gives the result shown for R_8 in the earlier listing.

By way of example, the following circuit values were determined by the procedures developed hereinabove:

$R_1 = 6.68K$
$R_2 = 19.33K$
$R_3 = 7.16K$
$R_4 = 193.3K$
$R_5 = 66.8K$
$R_6 = 76.2K$
$R_7 = 16.57K$
$R_8 = 11K$
$V_{DD} = 4.72 V$

The calculations for circuit values are based on the assumption that the transistors have the same beta, but the different current densities in the transistors results in slightly different betas. Because of this difference, and possibly other factors, the optimal circuit values, e.g. as determined by circuit simulation, may differ somewhat from those developed above.

Another embodiment of the invention is shown in FIG. 2. Here the circuit of FIG. 1 is operated closed loop to stabilize rather than detect a particular reference voltage. For this purpose there is provided an amplifier having its input connected to the output terminals X-Y. Any difference is amplified and applied to the V_{REF} line, which is the voltage to be stabilized. The amplifier

is connected for negative feedback so that V_{REF} will be driven to minimize the X-Y voltage difference.

The voltage V_C to which the transistor collectors are returned is independent of V_{REF} . This voltage V_C may be positive, negative, or the same as V_{REF} (and may even be different for the two transistors). It is an important advantage that the collectors are uncommitted. It is particularly advantageous because the substrate bipolar transistors (parasitic) developed in the usual CMOS processes can be employed as the reference circuit transistors. Although the circuit is shown implemented with NPN transistors, it could use PNP transistors, such as might be found on an N-well CMOS process.

The V_{REF} line can be biased beyond (i.e. positive in FIG. 2) the V_C line so that the circuit can actually control the regulation of a voltage beyond its supply rails. This arrangement would take advantage of thin film resistors and the fact that the V_{REF} voltage is divided down before being applied to the transistors, resulting in the multiplication of the ΔV_{BE} signal associated with the X-Y difference voltage. This circuit does not have the headroom problem in some previous proposals, and is not constrained to use integral multiples of the band gap. The amplifier can directly drive the V_{REF} terminal so that it not only stabilizes the loop voltage, but it also can provide a low impedance output.

Although preferred embodiments of the invention have been disclosed herein in detail, it is to be understood that this is for the purpose of illustrating the invention, and should not be construed as necessarily limiting the invention since those of skill in this art can readily make various changes and modifications thereto without departing from the scope of the invention as reflected in the claims hereof.

What is claimed is:

1. A band-gap reference circuit comprising:

first and second transistors operable at different current densities to produce a ΔV_{BE} signal as a function of temperature;

first and second V_{BE} multiplier circuits each connected to the base and emitter of a corresponding one of said transistors; and

output terminal means coupled to said transistors to develop a ΔV_{BE} signal multiplied in magnitude by said multiplier circuits.

2. A circuit as in claim 1, wherein each of said multiplier circuits comprises at least two series-connected resistors one of which is connected between the base and emitter of the corresponding transistor.

3. A circuit as in claim 2, including first and second resistor means connected between common and the emitter of a respective transistor;

one of said resistor means comprising at least two resistors forming a voltage divider to establish at the junction of said two resistors one terminal of said output terminal means.

4. A circuit as in claim 1, wherein each of said multiplier circuits includes first resistive means connected between the base of the corresponding transistor and a reference voltage, and second resistive means connected between the base and the emitter of the corresponding transistor.

5. A circuit as in claim 4, including first and second emitter resistor means each connected between a common line and the emitter of a corresponding transistor.

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6. A circuit as in claim 5, wherein one of said emitter resistor means comprises at least two series-connected resistors forming a voltage divider;
said output terminal means having one terminal at the junction between two of said series-connected resistors;
said output terminal means having a second terminal connected to the emitter resistor means.
7. A circuit as in claim 1, wherein said multiplier circuits are connected to a voltage reference line to produce current therethrough;
an amplifier having its input connected to said output terminal means to receive the signal therefrom; and means connecting the output of said amplifier to said voltage reference line in a negative feedback sense to stabilize the voltage of said line.
8. A circuit as in claim 7, wherein each of said multiplier circuits comprises a resistor string;

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one end of each string being connected to said voltage reference line;
the other end of each string being connected to the emitter of a respective one of said transistors;
the base of each of said transistors being connected to an intermediate junction of a corresponding one of said resistor strings.
9. A circuit as in claim 8, including two series resistors connected between common and the emitter of one of said transistors;
at least one resistor connected between common and the emitter of the other transistor;
said amplifier input being connected between the emitter of said other transistor and the junction of said two series resistors.
10. A circuit as in claim 7, wherein the collectors of said transistors are connected to voltages which are different from the voltage of said reference line.

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UNITED STATES PATENT AND TRADEMARK OFFICE
CERTIFICATE OF CORRECTION

PATENT NO. : 4,622,512

DATED : November 11, 1986

INVENTOR(S) : Adrian Paul Brokaw

It is certified that error appears in the above—identified patent and that said Letters Patent is hereby corrected as shown below:

Column 5, line 31 should read:

$$A_R = \alpha_1/\alpha_2 = 1 + (kT/q) \ln J_R / (V_G - V_{BEO})$$

Signed and Sealed this
Seventeenth Day of February, 1987

Attest:

DONALD J. QUIGG

Attesting Officer

Commissioner of Patents and Trademarks